

What does inelastic neutron scattering measure in quantum spin ice?

1st Asia Pacific Workshop on Quantum Magnetism

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Our recent works on quantum spin ice

Ce₂Sn₂O₇, symmetry enriched U(1) QSL and field-driven Anderson-Higgs transition
Y-D Li, [GC](#), PRB Rapid Comm, 95, 041106, (2017)

Quantum spin ice with [dipole-octupole doublet](#)
Y-P Huang, [GC](#), M Hermele, PRL 112, 167203, (2014)

Quantum spin ice on the breathing pyrochlore lattice.
L Savary, XQ Wang, HY Kee, YB Kim, Y Yu, [GC](#), PRB 94, 205107, (2016)

“Magnetic Monopole” condensation transition out of spin ice U(1) QSL: Pr₂Ir₂O₇
[GC](#), PRB 94, 205107, (2016)

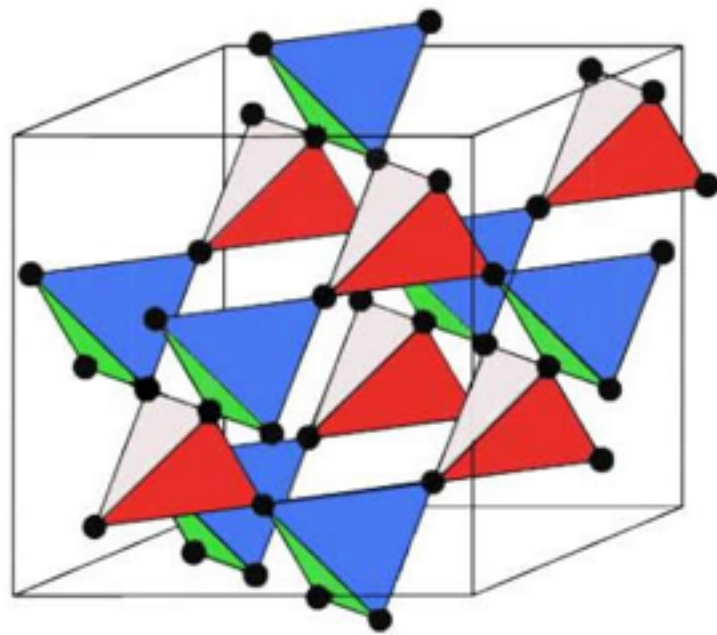
Spectral periodicity of spinon continuum in quantum spin ice

Gang Chen, PhysRevB, 96, 085136, (August 2017)

What does inelastic neutron scattering measure in quantum spin ice?

Gang Chen, arXiv:1706.04333

Pyrochlore spin ice



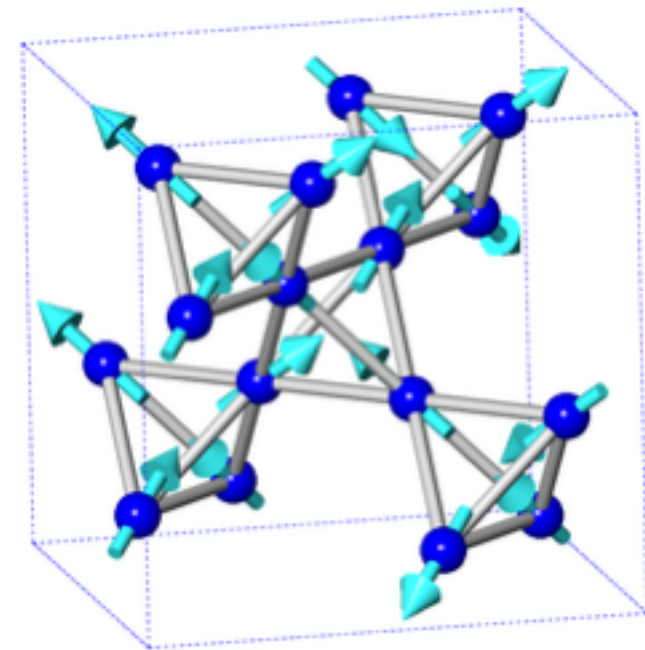
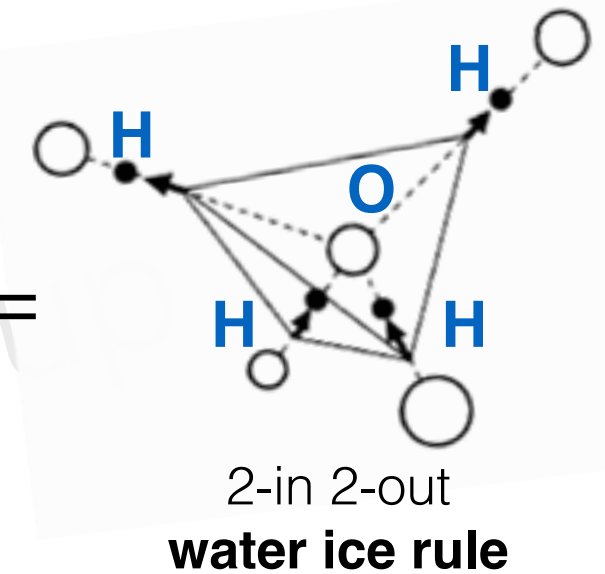
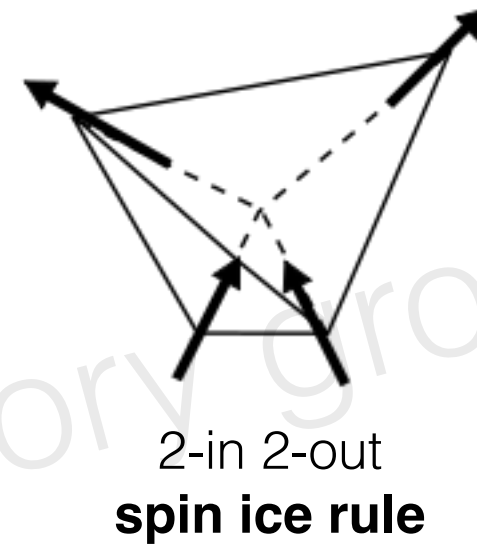
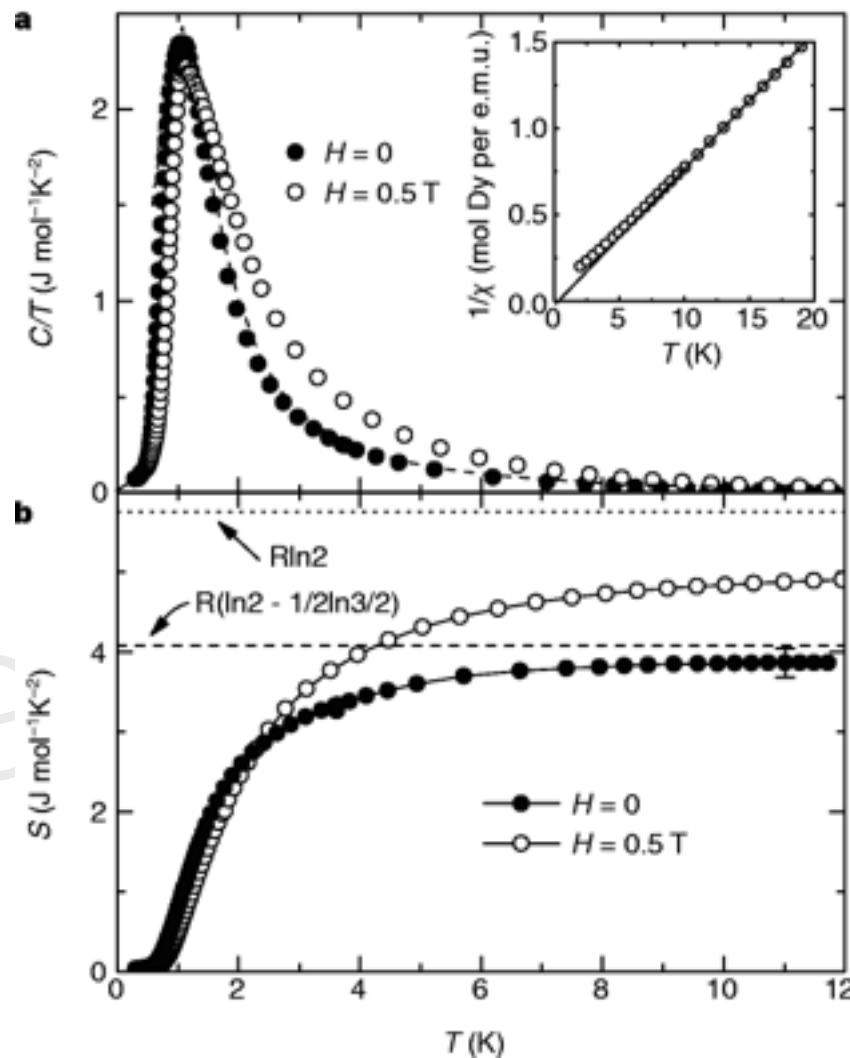
Rare Earth Elements																		by Geology.com						
H																							He	
Li	Be											B	C	N	O	F	Ne							
Na	Mg											Al	Si	P	S	Cl	Ar							
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr							
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe							
Cs	Ba	La-Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn							
Fr	Ra	Ac-Lr	Rf	Db	Sg	Bh	Hs	Mt																
Lanthanides																								
La Ce Pr Nd Pm Sm Eu Gd Tb Dy Ho Er Tm Yb Lu																								
Actinides																								
Ac Th Pa U Np Pu Am Cm Bk Cf Es Fm Md No Lr																								

$$H = J_{zz} \sum_{\langle i,j \rangle} S_i^z S_j^z + \text{dipolar}$$

Castelnovo, Gingras, Moessner, Sondhi, Schiffer,
Shannon, Moon, Kim, Savary, Balents,

Classical spin ice

Dy₂Ti₂O₇

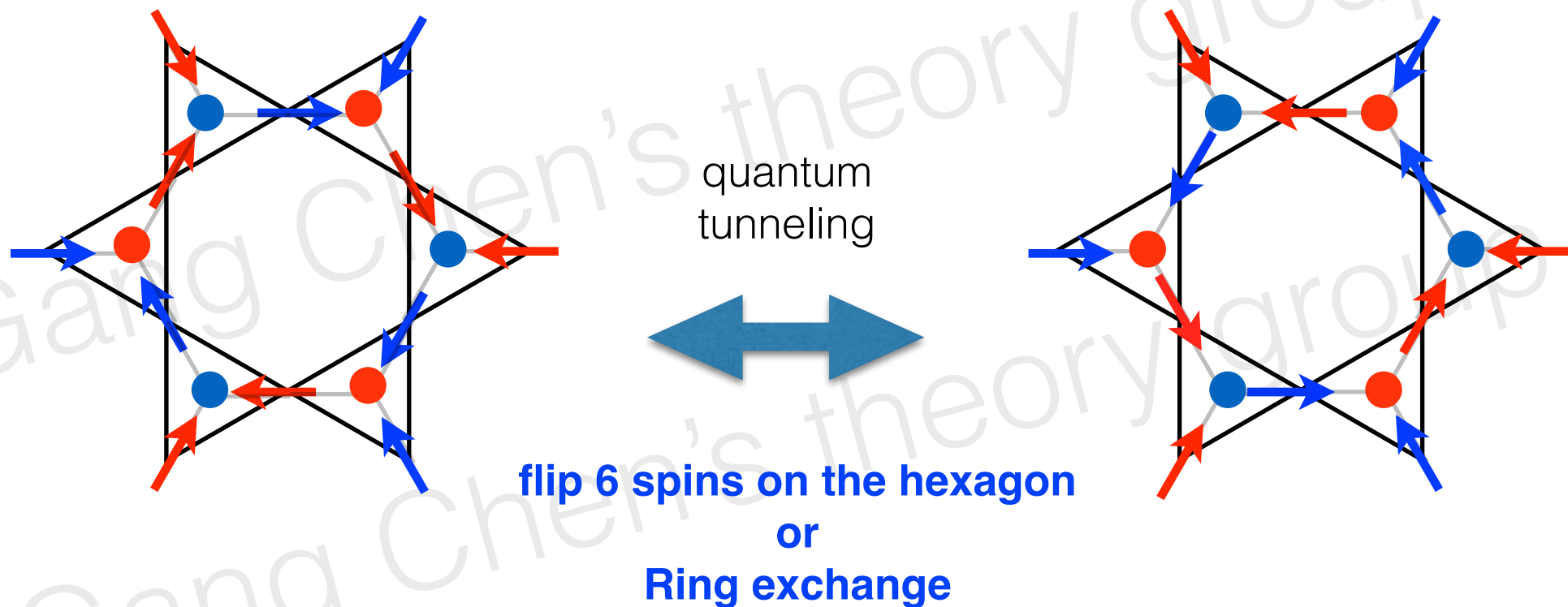


Pauling entropy in spin ice,
Ramirez, etc, Science 1999

U(1) quantum spin liquid

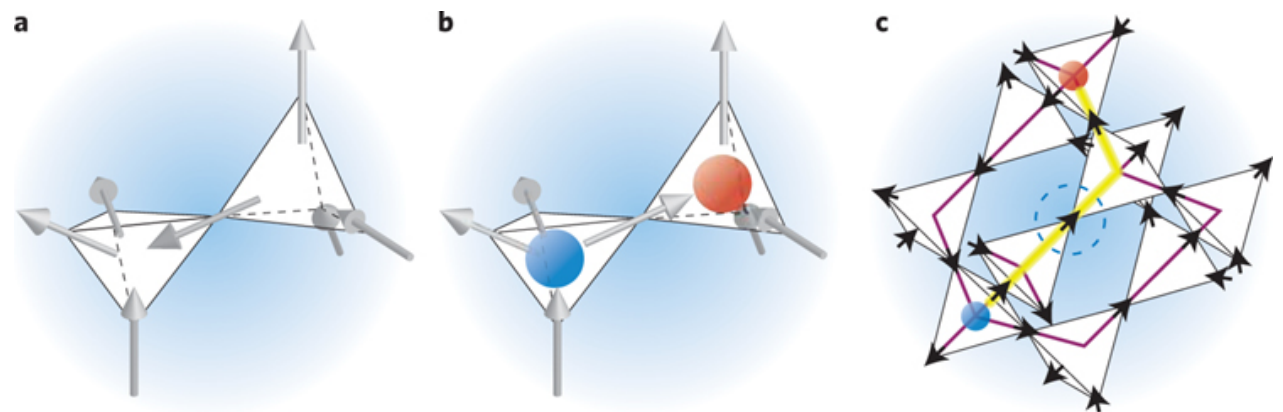
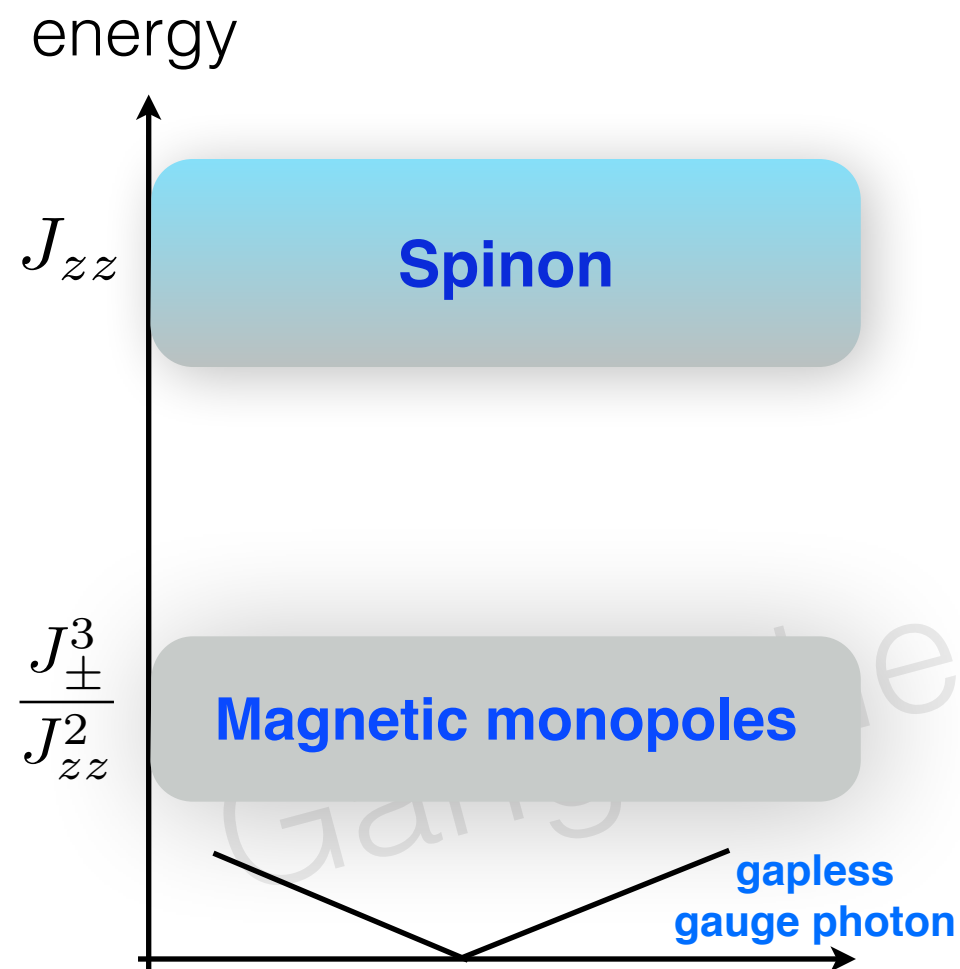
$$H = J_{zz} \sum_{\langle i,j \rangle} S_i^z S_j^z - J_{\pm} \sum_{\langle i,j \rangle} (S_i^+ S_j^- + S_i^- S_j^+) + \dots$$

Hermele, Fisher, Balents, Moessner, Isakov, YB Kim....



- Pretty much one can add any term to create **quantum** tunneling, as long as it is not too large to induce magnetic order, the **ground state** is a U(1) quantum spin liquid !

Excitations in the U(1) QSL

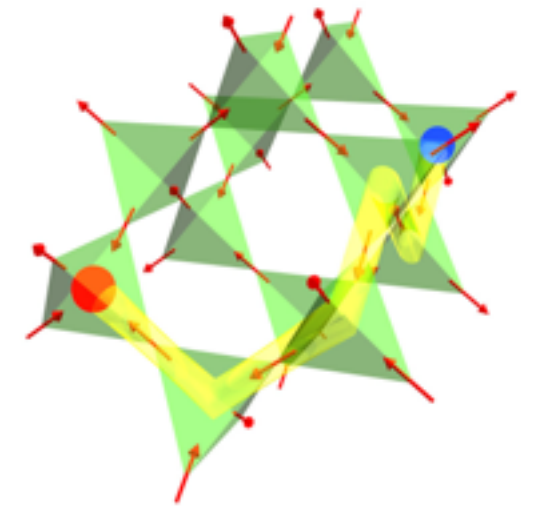


Figs from Moessner&Schiffer,2009

Spinon deconfinement

- No LRO, no symmetry breaking, **cannot** be understood in Landau's paradigm!
- The right description is in terms of fractionalization and emergent gauge structure.

Equivalence of “notations”



Excitations (notation 1)	Excitations (notation 2)	
Spinon	Magnetic monopole	} purely quantum, no classical analogue
“Magnetic monopole”	Electric monopole	
Gauge photon	Gauge photon	

↑ This talk

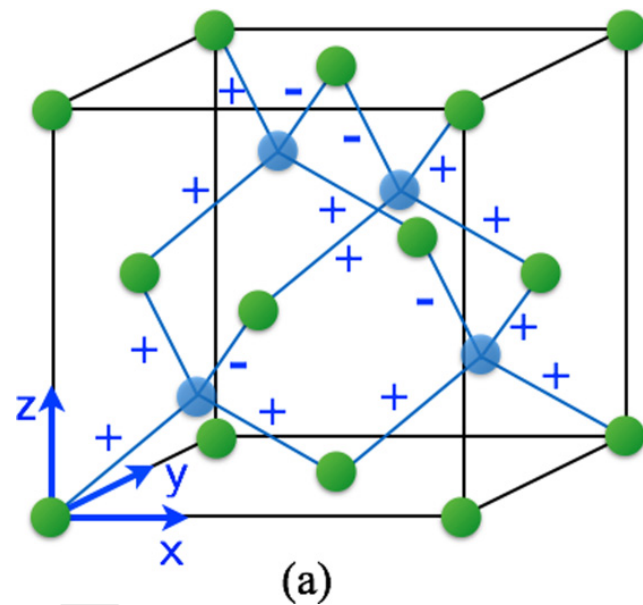
↑ Eun-Gook Moon’s talk

has classical analogue

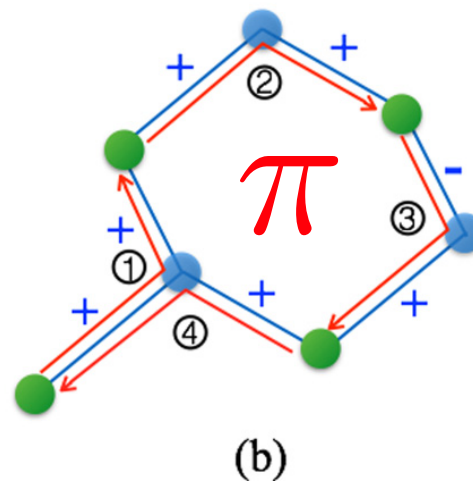
“Magnetic monopole” is probably closer in spirit to **Dirac’s monopole (1931)**.
One has to confirm that “magnetic monopole” is emergent excitation,
rather than a fictitious particle.

What piece of experimental info indicates these exotic and emergent particles?

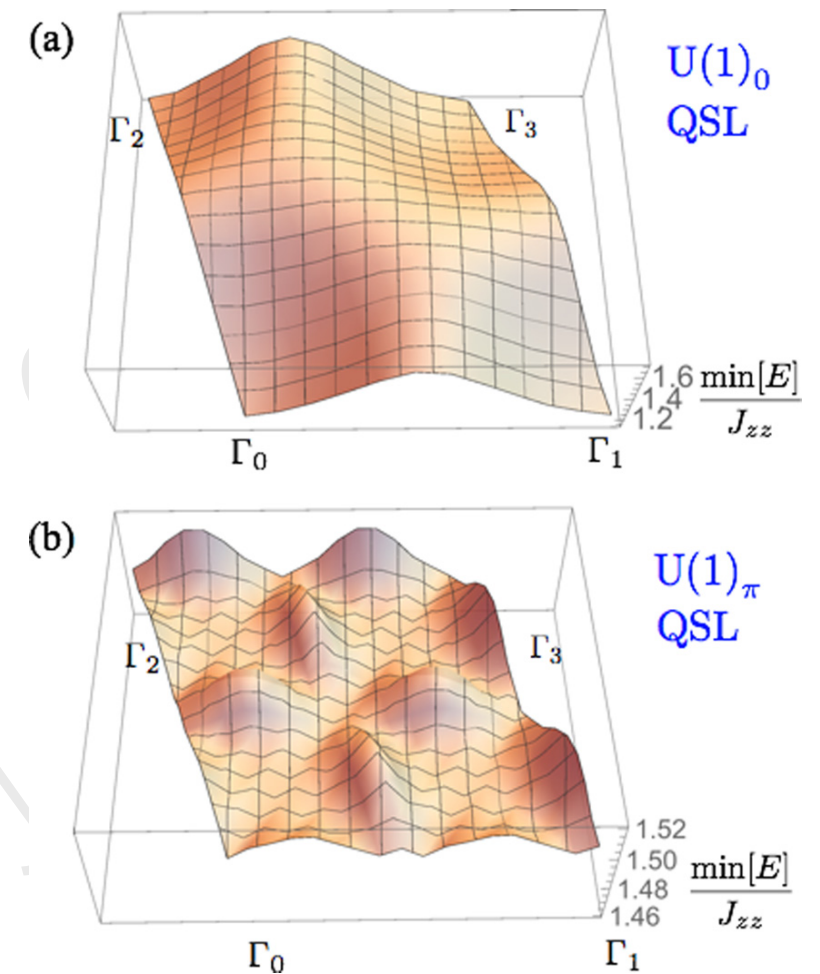
Spinon continuum: background flux and folded Brillouin zone



diamond lattice of
pyrochlore centers



Occasionally, the spinon experiences a **PI** background flux as it moves on the diamond hexagons.



Spectral periodicity of spinon
lower excitation edges:
Pi flux -> folded Brillouin zone

Sungbin Lee, S Onoda, Balents, PRB 2012

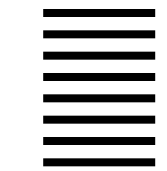
Gang Chen, PRB, 96, 085136, 2017

Kramers vs Non-Kramers doublet

Kramers doublet: e.g. Yb ion in Yb₂Ti₂O₇

Yb³⁺ ion: 4f¹³ has J=7/2 due to SOC.

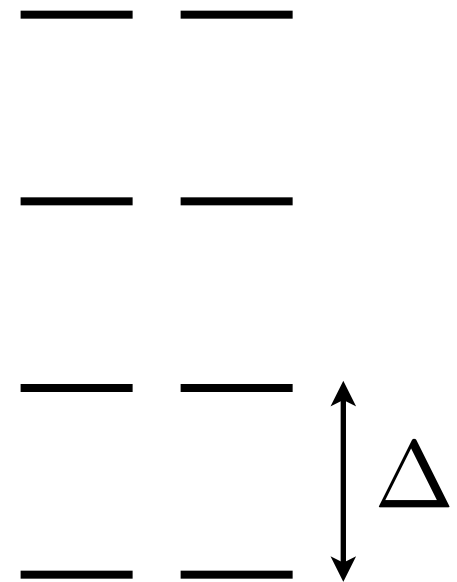
$$\mathcal{T} : S^x \rightarrow -S^x, S^y \rightarrow -S^y, S^z \rightarrow -S^z$$



J=7/2



CEF

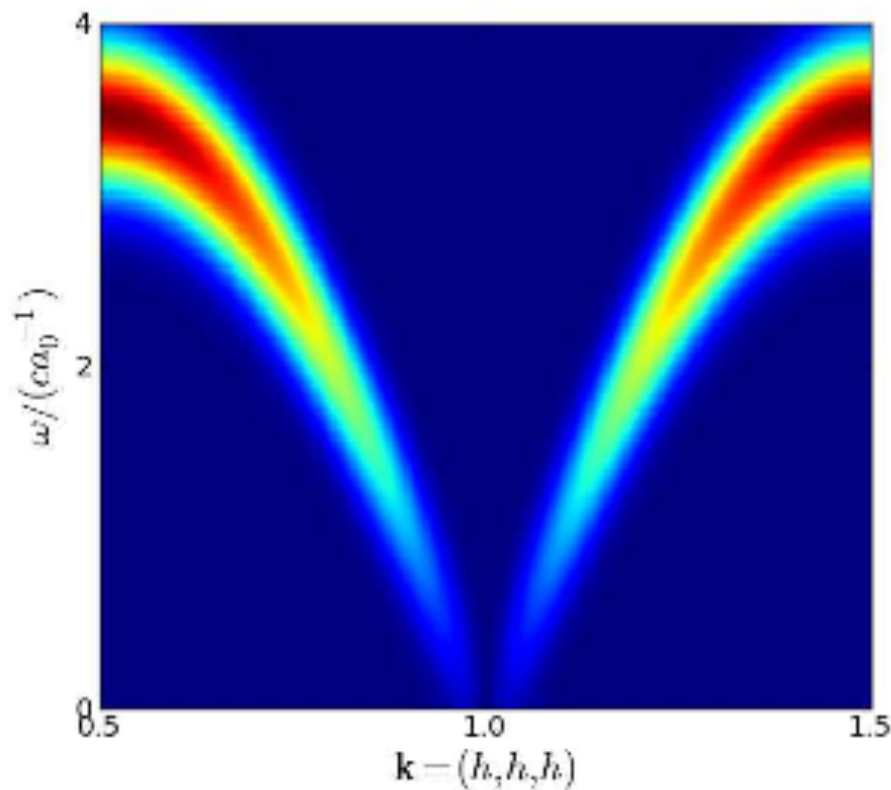


(unusual example is dipole-octupole doublet in Ce₂Sn₂O₇ and Nd₂Zr₂O₇),
YP Huang, [GC](#), Hermele, PRL 2014; YD Li, [GC](#), PRB2016, YD Li, [GC](#), PRB 2017

In contrast, the Tb ion in Tb₂Ti₂O₇, Pr ion in Pr₂Ir₂O₇, Pr₂Sn₂O₇, Pr₂Zr₂O₇, etc,
are **non-Kramers doublets**

$$\mathcal{T} : S^{x,y} \rightarrow S^{x,y}, S^z \rightarrow -S^z.$$

Emergent light: U(1) photon



$$I(\omega) \sim \omega$$

emergent U(1) photon in U(1) QSL

Hermele et al 2004
N Shannon et al 2012,
L Savary et al 2012

$$S_z \sim E \text{ (emergent electric field)}$$

Low energy theory

$$\text{Im}[E_{-\mathbf{k}, -\omega}^\alpha E_{\mathbf{k}, \omega}^\beta] \propto [\delta_{\alpha\beta} - \frac{k_\alpha k_\beta}{\mathbf{k}^2}] \omega \delta(\omega - v|\mathbf{k}|),$$

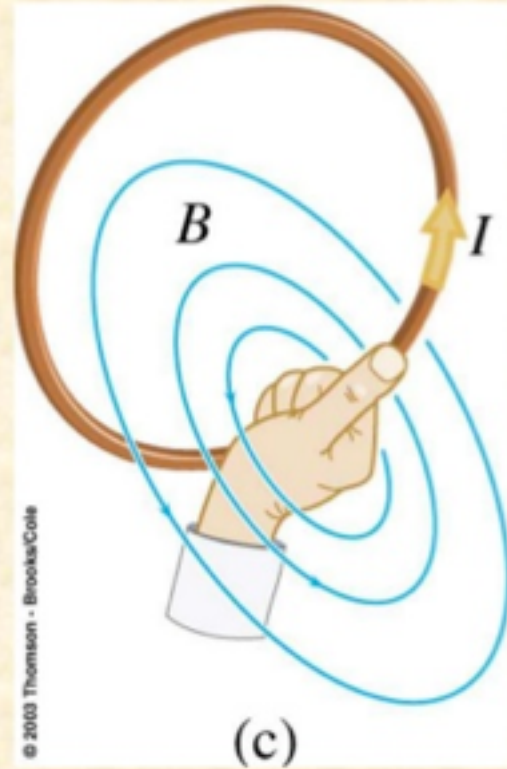
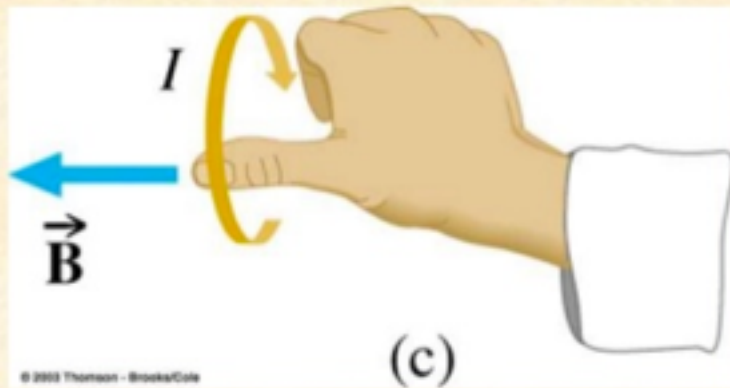
The well-known result of the photon modes in the INS measurement was obtained by considering the low-energy field theory that describes the long-distance quantum fluctuation within the spin ice manifold. The actual spin dynamics, that is captured by the S^z correlation in the INS measurement, operates in a broad energy scale up to the exchange energy and certainly contains more information than just the photon mode from the low-energy Maxwell field theory. What is the other informa-

Gang Chen, arXiv:1706.04333

Electromagnetic duality

For loop or coil of wire, can still use 1st RHR, but direction of current constantly changes.

Easier to use 2nd Right Hand Rule. Fingers curl in direction of current, thumb points to direction of magnetic field.

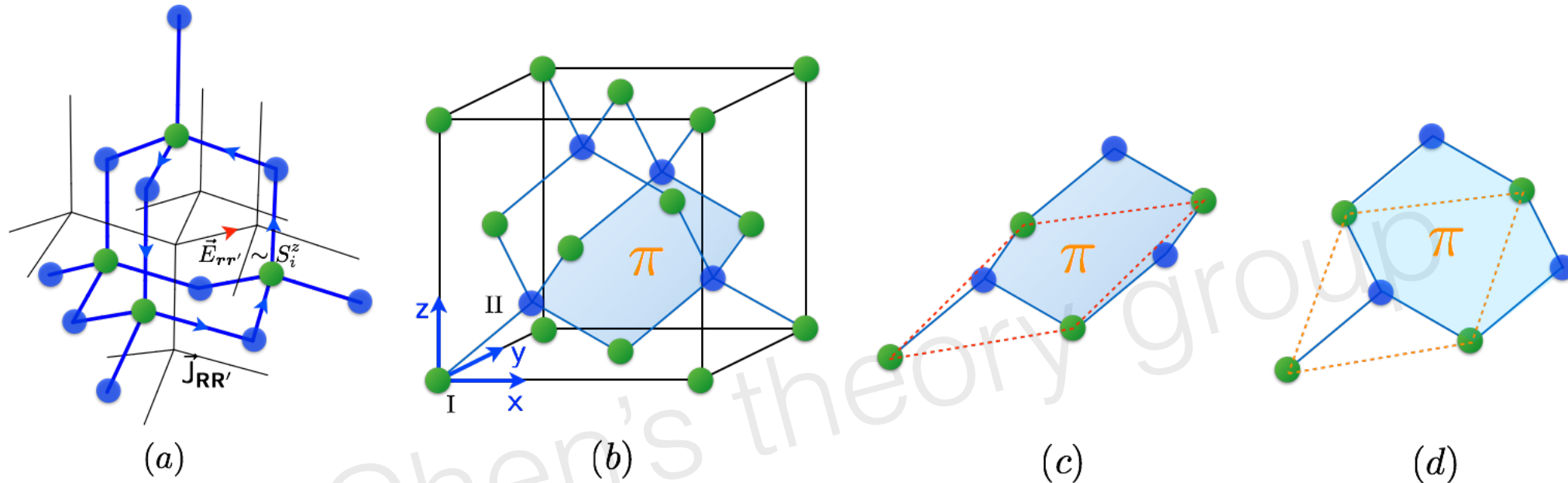


Duality

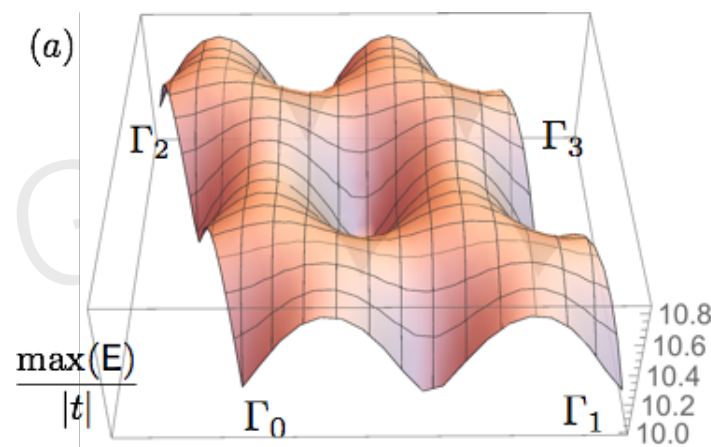
Electric loop current \rightarrow Magnetic field
Magnetic loop current \rightarrow Electric field

$$S_z \sim E \text{ (emergent electric field)}$$

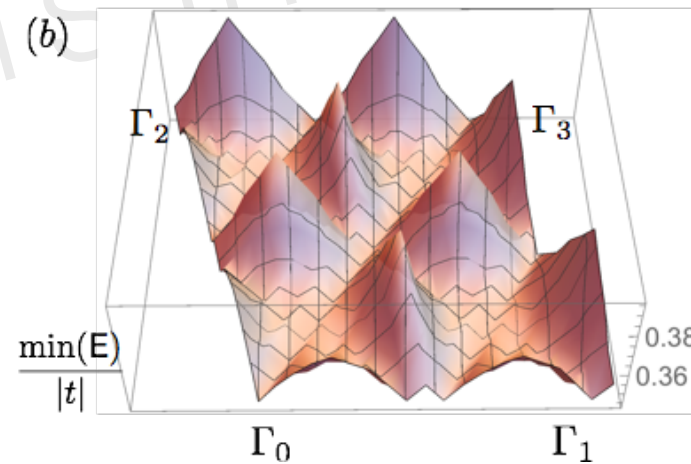
Sz correlation = monopole loop current correlation



$$H_{\text{dual}} = -t \sum_{\langle \mathbf{R}\mathbf{R}' \rangle} e^{-i2\pi\alpha_{\mathbf{R}\mathbf{R}'}} \Phi_{\mathbf{R}}^\dagger \Phi_{\mathbf{R}'} - \mu \sum_{\mathbf{R}} \Phi_{\mathbf{R}}^\dagger \Phi_{\mathbf{R}} + \frac{U}{2} \sum_{\square^*} (\text{curl} \alpha - \frac{\eta_{\mathbf{r}}}{2})^2 - K \sum_{\langle \mathbf{R}\mathbf{R}' \rangle} \cos B_{\mathbf{R}\mathbf{R}'} + \dots$$



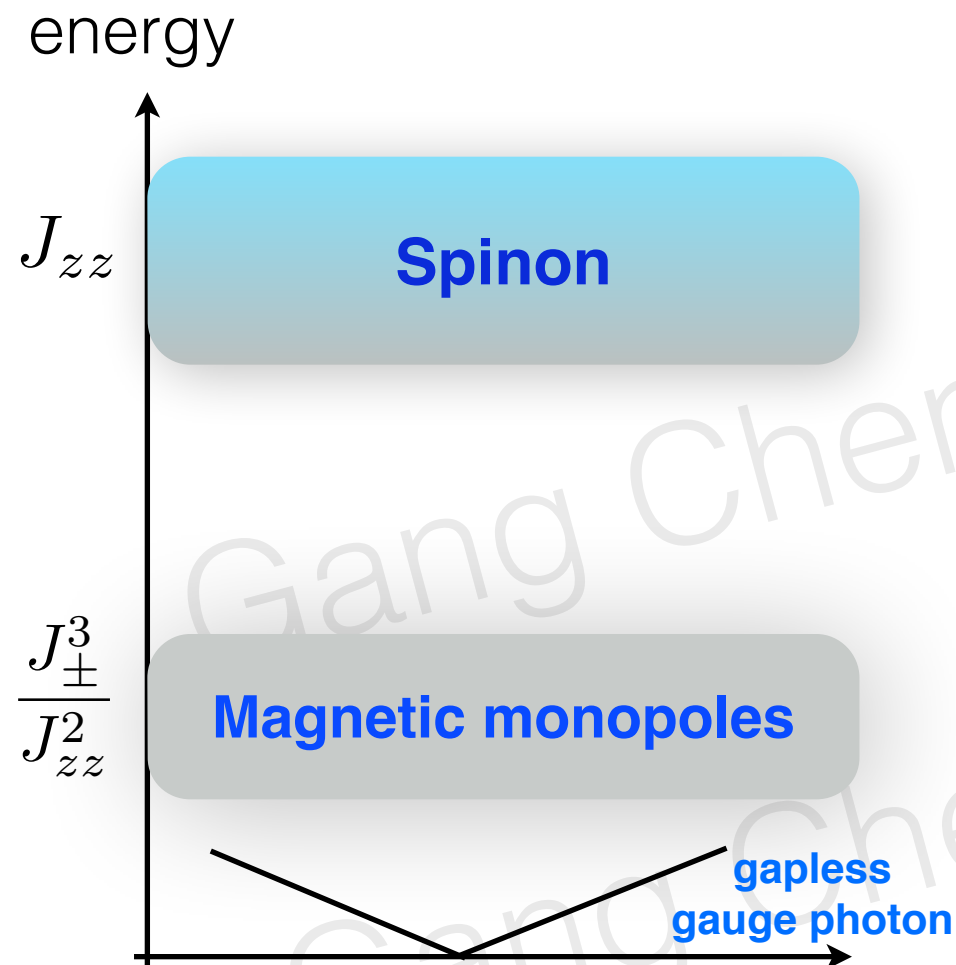
the upper edge



the lower edge

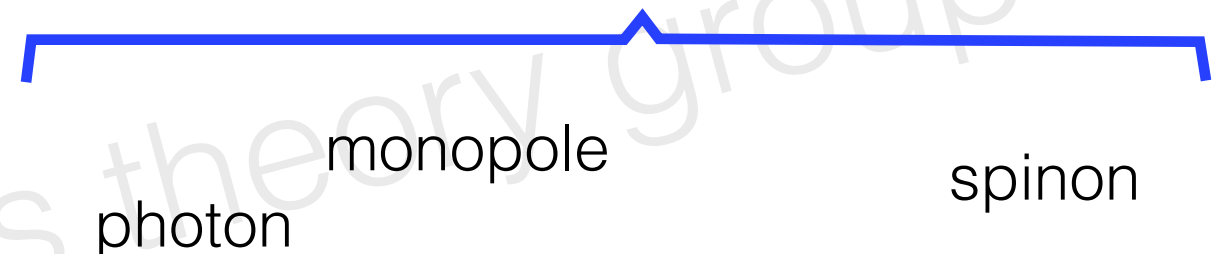
Monopole always experiences Pi flux

Suggestion 1: combine thermal transport with inelastic neutron



For **non-Kramers doublets** such as Pr ion in $\text{Pr}_2\text{Zr}_2\text{O}_7$ and Tb ion in $\text{Tb}_2\text{Ti}_2\text{O}_7$

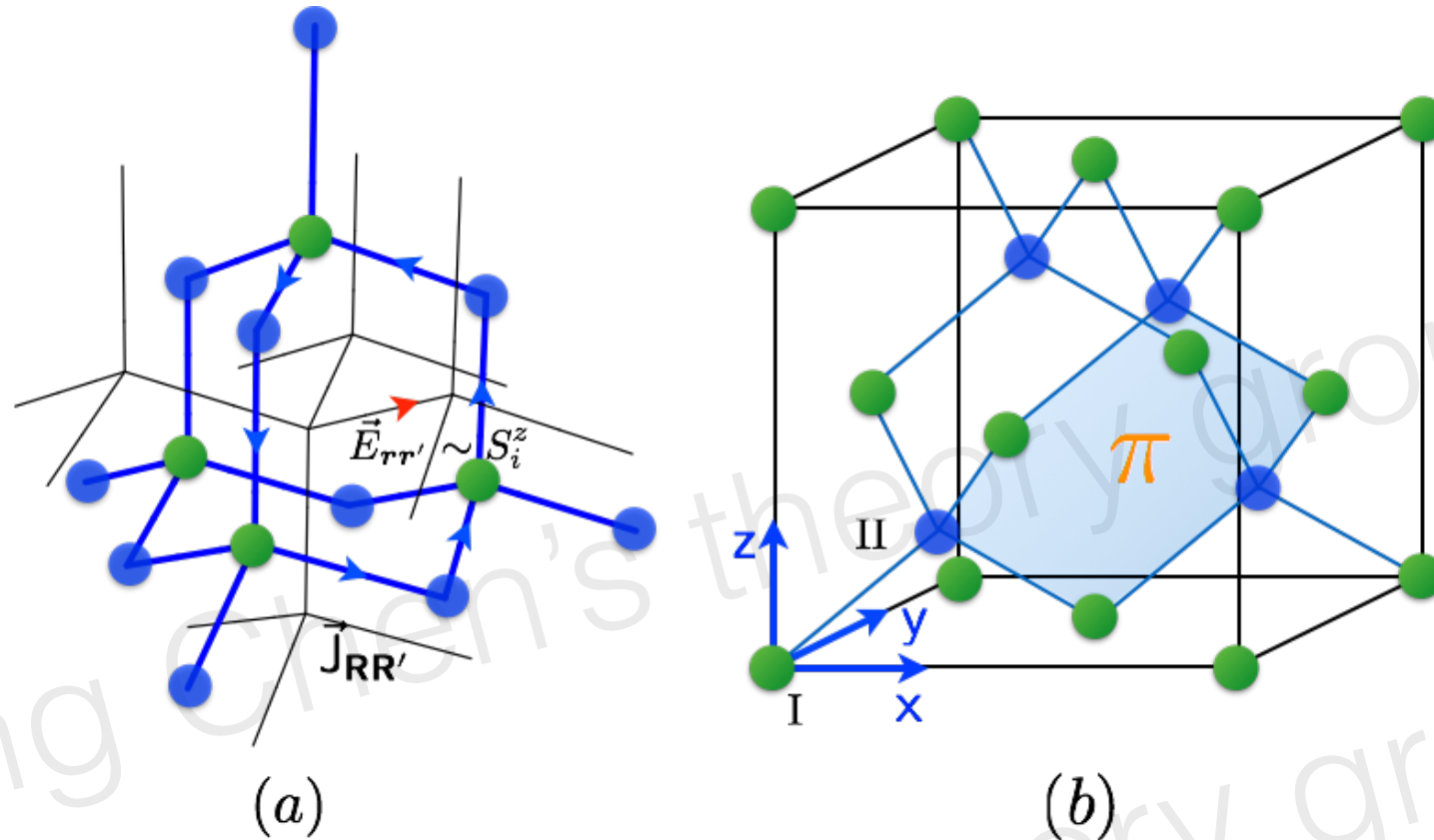
Visible in thermal transport



Visible in inelastic neutron scattering

energy

Suggestion 2: effect of the external magnetic field



$$H_{Zeeman} = \vec{B} \cdot \sum_i S_i^z \hat{z}_i$$

The weak magnetic field polarizes S_z slightly, and thus modifies the background electric field distribution. This further modulates monopole band structure, creating “**Hofstadter**” monopole band, which may be detectable in inelastic neutron.

Summary

1. We point out the existence of “magnetic monopole continuum” in the U(1) quantum spin liquid, and monopole is purely **quantum origin**.
2. We further point out that the “magnetic monopole” always experiences a π flux, and thus supports enhanced spectral periodicity with **folded Brillouin zone**.

In fact, continuum has been observed in $\text{Pr}_2\text{Hf}_2\text{O}_7$ (R. Sibille, et al, arXiv 1706.03604).

