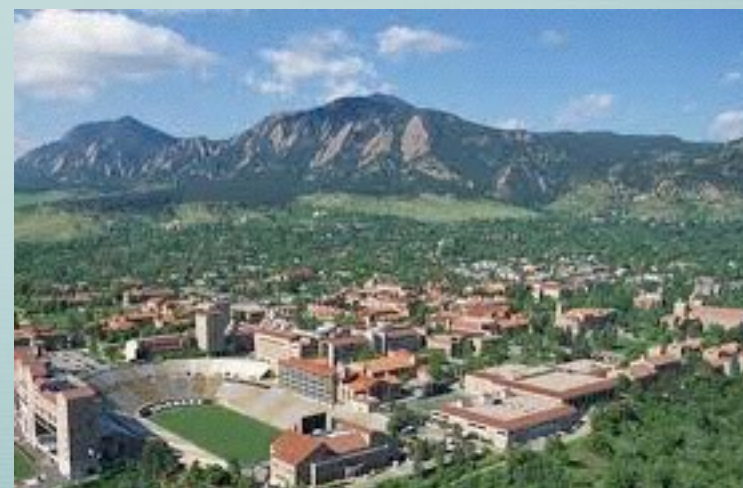


SPIN-ORBIT INTERACTION IN FRUSTRATED MAGNETIC SYSTEMS: APPLICATION TO DOUBLE PEROVSKITES

GANG CHEN

Physics Department & JILA, University of Colorado
Boulder



Collaborators

- * **Rodrigo Pereira** (University of Sao Paulo, Brazil) for an early work
- * **Leon Balents** (KITP, UCSB)

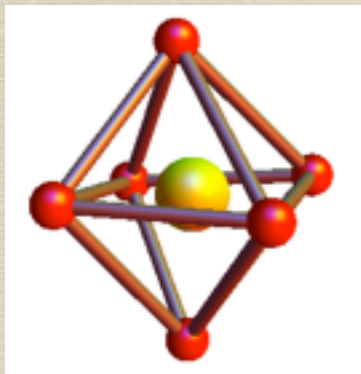
Chen, Pereira, Balents, PRB 2010
Chen, Balents (in preparation)

OUTLINE

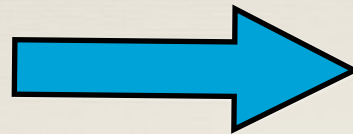
- * Introduction: Spin-orbit coupling and ordered double perovskites
- * Ground state phases
- * Finite temperature phases
- * Experiments and discussion

Motivation: Spin-orbit interaction on degenerate t_{2g} manifold

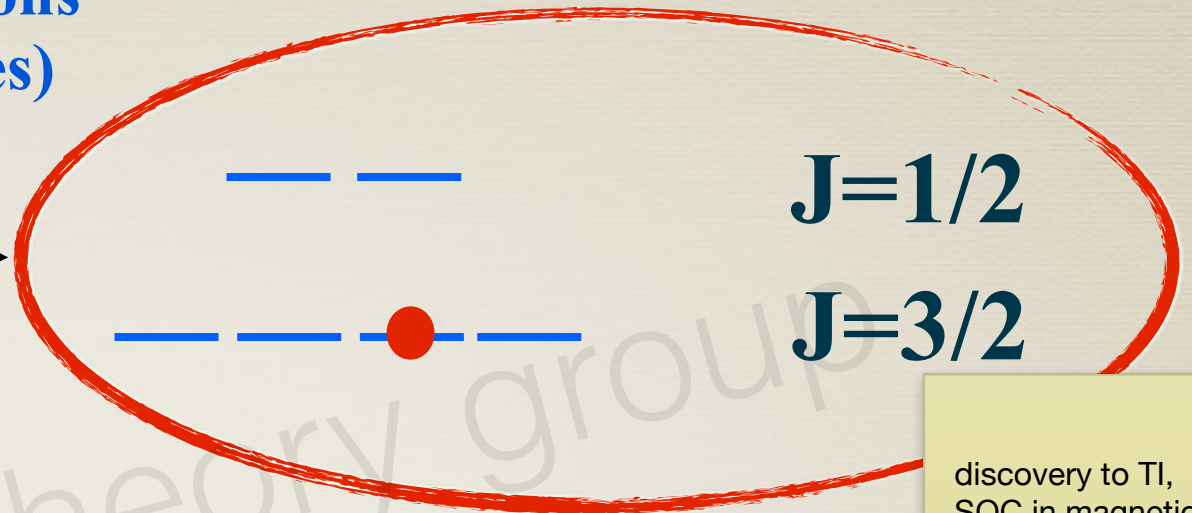
Consider well-localized 4d, 5d electrons
(maybe 3d electrons for certain cases)



$S = 1/2, l = 1$



SOC

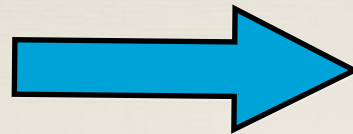
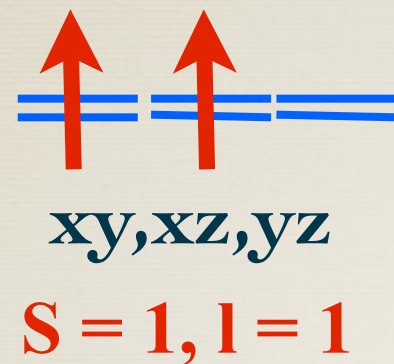
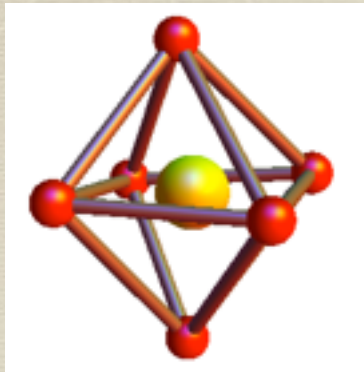


$$H_{SOC} = -\lambda \mathbf{l} \cdot \mathbf{S}$$

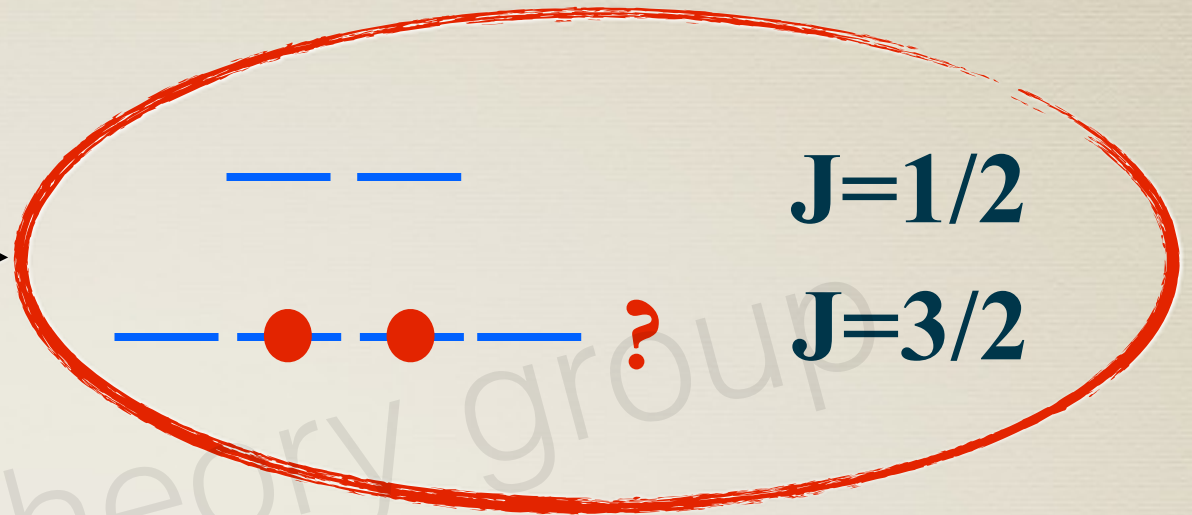
discovery to TI,
SOC in magnetic system
the systems described are
systems with heavy magnetic
ions, 4d or 5d. Consider an
octahedron

electron # per site	Local spin state	some compounds	Talks
1	$J=3/2$	next few sides	this talk

Spin-orbit interaction on degenerate **t_{2g}** manifold



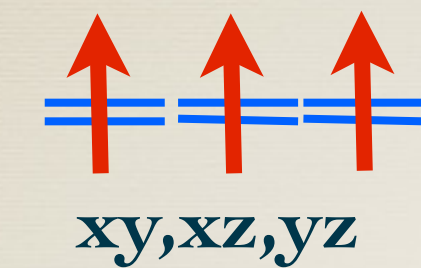
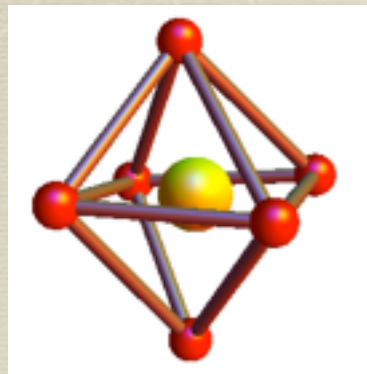
SOC



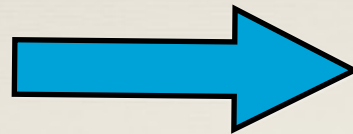
$$H_{SOC} = -\lambda \mathbf{l} \cdot \mathbf{S}$$

electron # per site	Local spin state	some compounds	Talks
1	J=3/2	next few sides	this talk
2	J=2	next few sides	this talk

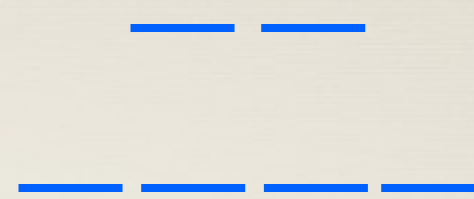
Spin-orbit interaction on degenerate t_{2g} manifold



$$S = 3/2, L = 0$$



SOC



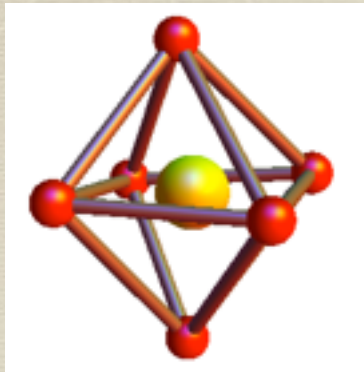
$$J = 1/2$$

$$J = 3/2$$

$$H_{SOC} = -\lambda \mathbf{L} \cdot \mathbf{S}$$

electron # per site	Local spin state	some compounds	Talks of the conference
1	$J=3/2$	next few sides	this talk
2	$J=2$	next few sides	this talk
3	$S=3/2$	SCGO, $ZnCr_2O_4$, etc	Nenert
4	$J=0$		

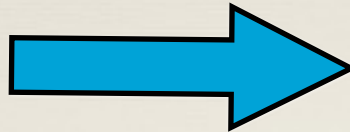
Spin-orbit interaction on degenerate t_{2g} manifold



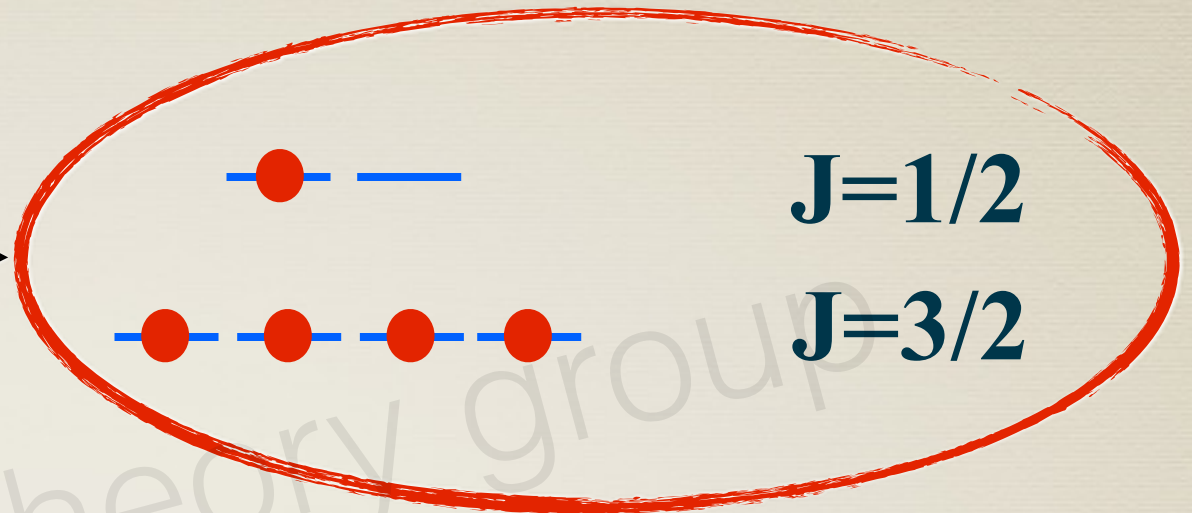
$\equiv \equiv \equiv$

xy, xz, yz

$S=1/2, l=1$



SOC

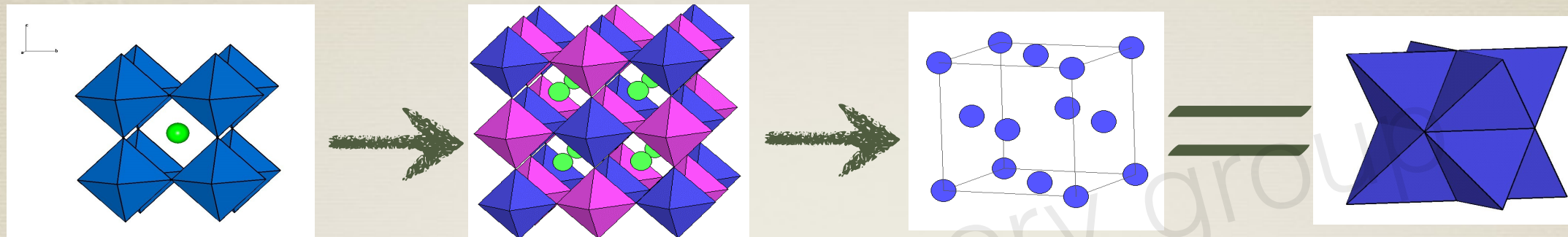


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4	$J=0$		
5	$J=1/2$	Iridates	Takayama, Jiang

Ordered double perovskites

FCC ordered double perovskites $A_2B'B'O_6$



Interplay between geometrical frustration and strong SOC

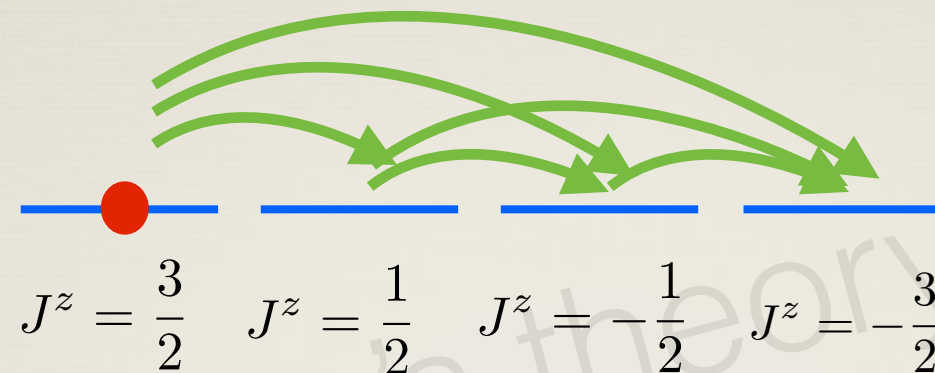
Compound	B' config.	crystal structure	θ_{CW}	$\mu_{eff}(\mu_B)$	magnetic transition	frustration parameter f
Ba_2YMoO_6	$Mo^{5+}(4d^1)$	cubic	-91K	1.34	PM down to 2K	$f \gtrsim 45$
Ba_2YMoO_6	$Mo^{5+}(4d^1)$	cubic	-160K	1.40	PM down to 2K	$f \gtrsim 80$
Ba_2YMoO_6	$Mo^{5+}(4d^1)$	cubic	-219K	1.72	PM down to 2K	$f \gtrsim 100$
La_2LiMoO_6	$Mo^{5+}(4d^1)$	monoclinic	-45K	1.42	PM to 2K	$f \gtrsim 20$
Sr_2MgReO_6	$Re^{6+}(5d^1)$	tetragonal	-426K	1.72	spin glass, $T_G \sim 50K$	$f \gtrsim 8$
Sr_2CaReO_6	$Re^{6+}(5d^1)$	monoclinic	-443K	1.659	spin glass, $T_G \sim 14K$	$f \gtrsim 30$
Ba_2CaReO_6	$Re^{6+}(5d^1)$	cubic to tetragonal (at $T \sim 120K$)	-38.8K	0.744	AFM $T_c = 15.4K$	$f \sim 2$
Ba_2LiOsO_6	$Os^{7+}(5d^1)$	cubic	-40.48K	0.733	AFM $T_c \sim 8K$	$f \gtrsim 5$
Ba_2NaOsO_6	$Os^{7+}(5d^1)$	cubic	-32.45K	0.677	FM $T_c \sim 8K$	$f \gtrsim 4$
Ba_2NaOsO_6	$Os^{7+}(5d^1)$	cubic	$\sim -10K$	~ 0.6	FM $T_c = 6.8K$	$f \gtrsim 4$

One electron per site: Chen, Pereira and Balents, PRB 2010

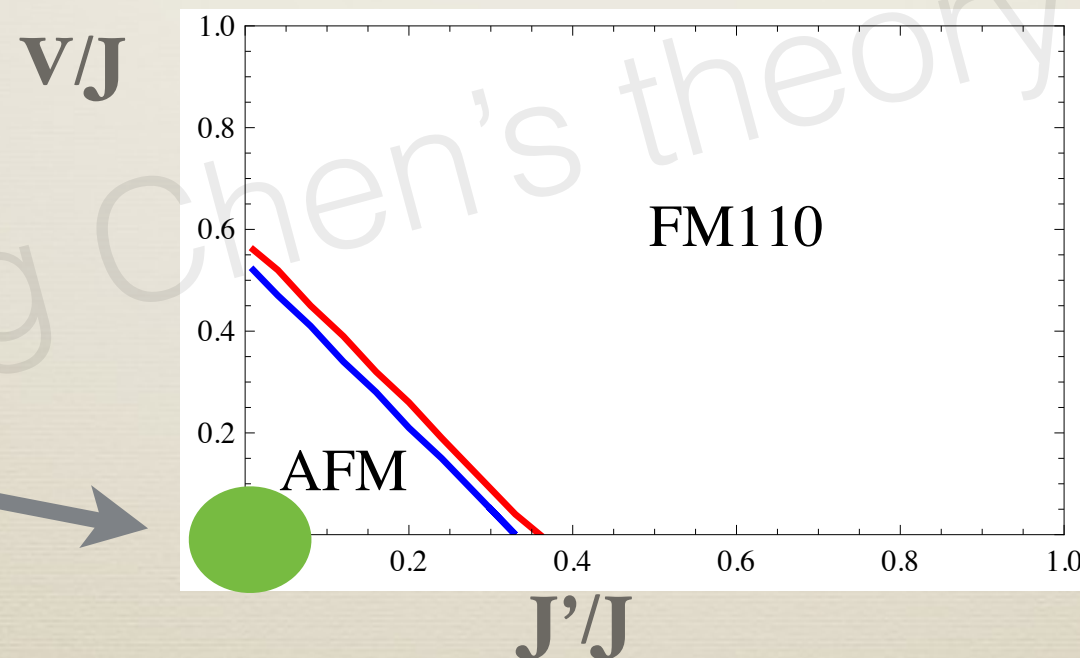
Erickson, et al PRL 2007
M. A. de Vries, et al PRL (2010).
T. Aharen, et al PRB (2010).
E. J. Cussen, et al, Chem. Mater(2006).
C. R. Wiebe, et al PRB (2003).
C. Wiebe, et al PRB (2002).
K. Yamamura, et al JSSC (2006).

Predictions for 1 electron case: $J=3/2$

$$H \sim \mathbf{J}_i \cdot \mathbf{J}_j + J_i^2 J_j^2 + J_i^3 J_j^3 + J_i J_j^3 + J_i^3 J_j$$



Enhanced quantum fluctuation!



Possible QSL

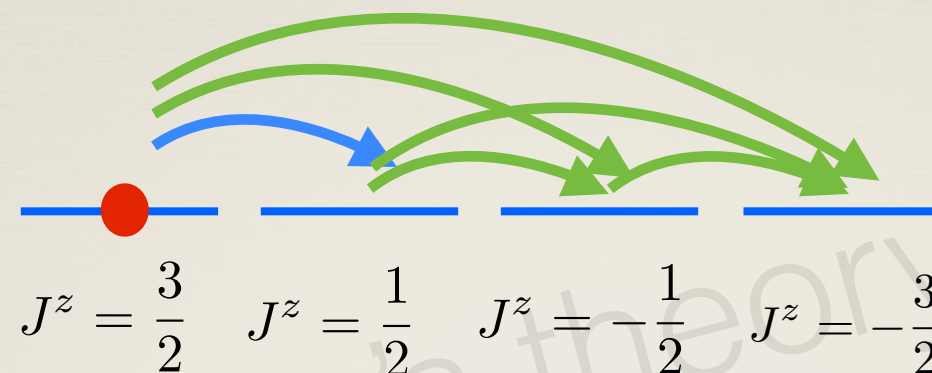
Might be relevant for
Ba₂YMoO₆

J is AFM exchange, J' is FM exchange, V is electric quadrupolar interaction

Chen, et al, PRB 2010

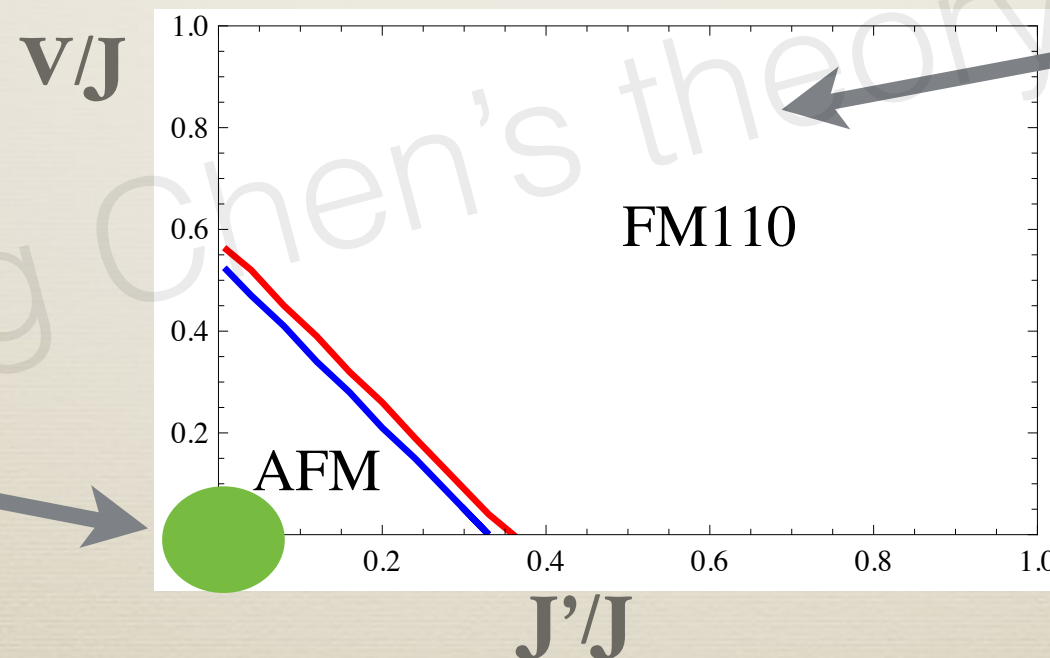
Predictions for 1 electron case: $J=3/2$

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non-heisenberg like hamiltonian;
biquadratic, bicubic, magnetic quadrupole,
octupole moment
enhanced quantum fluctuation;
linear spin wave theory

Enhanced quantum fluctuation!



**Magnetic
multipole order:
Octupole, Quadrupole**

$$\langle J_i^\mu J_i^\nu J_i^\rho \rangle, \quad \langle J_i^\mu J_i^\nu \rangle$$

FM state is observed in
Ba₂NaOsO₆

Chen, et al, PRB 2010

Carlo, et al, ArXiv 1105.3457

Aharen, et al, PRB 2010

M. A. de Vries, et al PRL (2010)

Erickson, et al PRL 2007

Possible QSL

Might be relevant for
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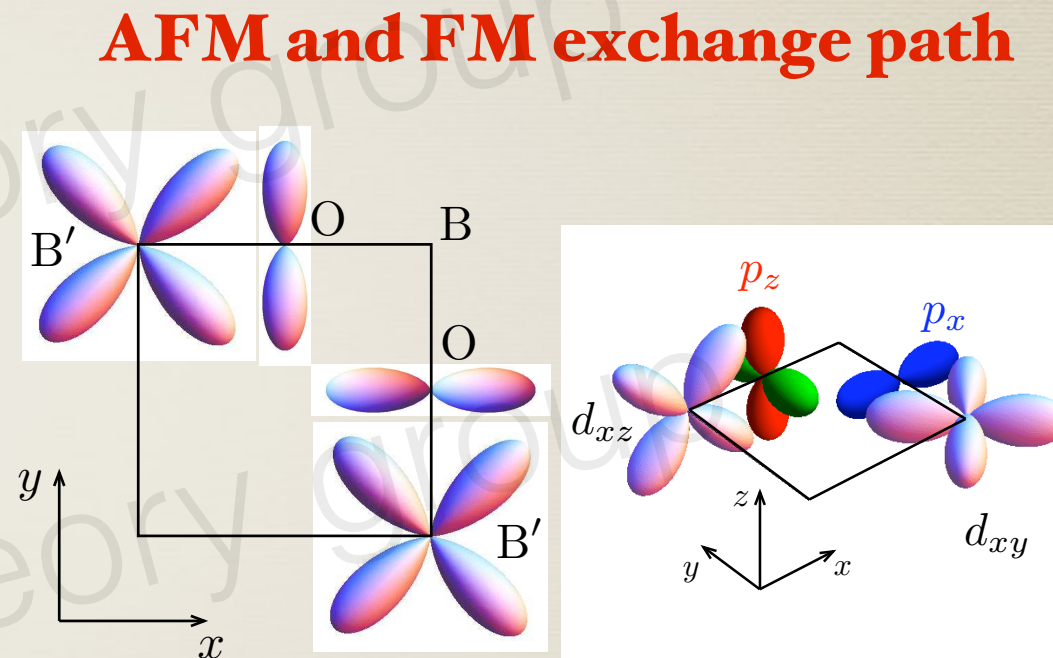
2 electron case: J=2

Re^{5+} , Os^{6+} in Ba_2CaOsO_6 , La_2LiReO_6 , Ba_2YReO_6

Exchange interaction

$$\mathcal{H}_{\text{ex-1}}^{\text{XY}} = J \sum_{\langle ij \rangle} \left(\mathbf{S}_{i,xy} \cdot \mathbf{S}_{j,xy} - \frac{1}{4} n_{i,xy} n_{j,xy} \right)$$

$$\mathcal{H}_{\text{ex-2}}^{\text{XY}} = -J' \sum_{\langle ij \rangle} \left[\mathbf{S}_{i,xy} \cdot (\mathbf{S}_{j,yz} + \mathbf{S}_{j,xz}) + \frac{3}{4} n_{i,xy} (n_{j,yz} + n_{j,xz}) + \langle i \leftrightarrow j \rangle \right]$$



$S_{i,xy}$ and $n_{i,xy}$ denote the electron spin residing on xy orbital and orbital occupation number for single electron xy orbital at site i, respectively.

Electric quadrupolar interaction: non-trivial after projection

$$\mathcal{H}_{\text{quad}}^{\text{XY}} = \sum_{\langle ij \rangle \in \text{XY}} \left[-\frac{4V}{3} (n_{i,xz} - n_{i,yz})(n_{j,xz} - n_{j,yz}) + \frac{9V}{4} n_{i,xy} n_{j,xy} \right]$$

2 electron case: J=2

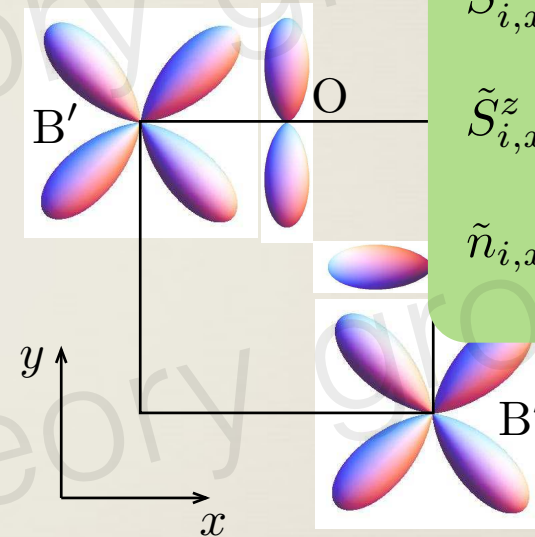
Re^{5+}, Os^{6+} in Ba_2CaOsO_6 , La_2LiReO_6 , Ba_2YReO_6

Exchange interaction

$$\mathcal{H}_{\text{ex-1}}^{\text{XY}} = J \sum_{\langle ij \rangle} \left(\mathbf{S}_{i,xy} \cdot \mathbf{S}_{j,xy} - \frac{1}{4} n_{i,xy} n_{j,xy} \right)$$

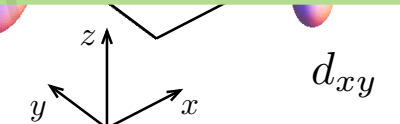
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AFM and



Projection to J=2

$$\begin{aligned} \tilde{S}_{i,xy}^x &= -\frac{1}{12} j_i^x + \frac{1}{12} (j_i^x)^3, \\ \tilde{S}_{i,xy}^y &= -\frac{1}{12} j_i^y + \frac{1}{12} (j_i^y)^3, \\ \tilde{S}_{i,xy}^z &= -\frac{1}{12} j_i^z + \frac{1}{12} (j_i^z)^3, \\ \tilde{n}_{i,xy} &= \frac{1}{3} + \frac{1}{6} (j_i^z)^2, \end{aligned}$$



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$$\mathcal{H}_{\text{quad}}^{\text{XY}} = \sum_{\langle ij \rangle \in \text{XY}} \left[-\frac{4V}{3} (n_{i,xz} - n_{i,yz})(n_{j,xz} - n_{j,yz}) + \frac{9V}{4} n_{i,xy} n_{j,xy} \right]$$

Frustration comes from anisotropic nature of orbital orientation.

2 electron case: J=2

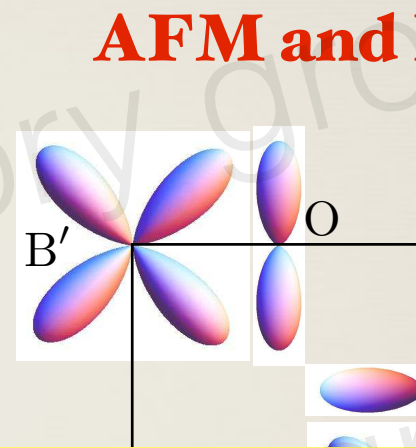
Re^{5+}, Os^{6+} in Ba_2CaOsO_6 , La_2LiReO_6 , Ba_2YReO_6

Projection to J=2

Exchange interaction

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$$\begin{aligned} \tilde{S}_{i,xy}^x &= -\frac{1}{12} j_i^x + \frac{1}{12} (j_i^x)^3, \\ \tilde{S}_{i,xy}^y &= -\frac{1}{12} j_i^y + \frac{1}{12} (j_i^y)^3, \\ \tilde{S}_{i,xy}^z &= -\frac{1}{12} j_i^z + \frac{1}{12} (j_i^z)^3, \\ \tilde{n}_{i,xy} &= \frac{1}{3} + \frac{1}{6} (j_i^z)^2, \end{aligned}$$

Intrinsic Frustration (not due to geometry!)

e.g. **SU(N) Heisenberg model** and **Chiral spin liquid** on square lattice and spin ladders (see **my poster**)

Occupation number for single electron xy orbital at site i, respectively.

Electric quadrupolar interaction: non-trivial after projection

$$\mathcal{H}_{\text{quad}}^{\text{XY}} = \sum_{\langle ij \rangle \in XY} \left[-\frac{4V}{3} (n_{i,xz} - n_{i,yz})(n_{j,xz} - n_{j,yz}) + \frac{9V}{4} n_{i,xy} n_{j,xy} \right]$$

Ground state phase diagram: $J=2$

- * Uniform state: FM111
- * 2-sublattice state($\mathbf{P}=2\mathbf{P}_i[001]$): AFM100, FM110, “*” phase, Quadrupole phase
- * Four-sublattice AFM state: Δ

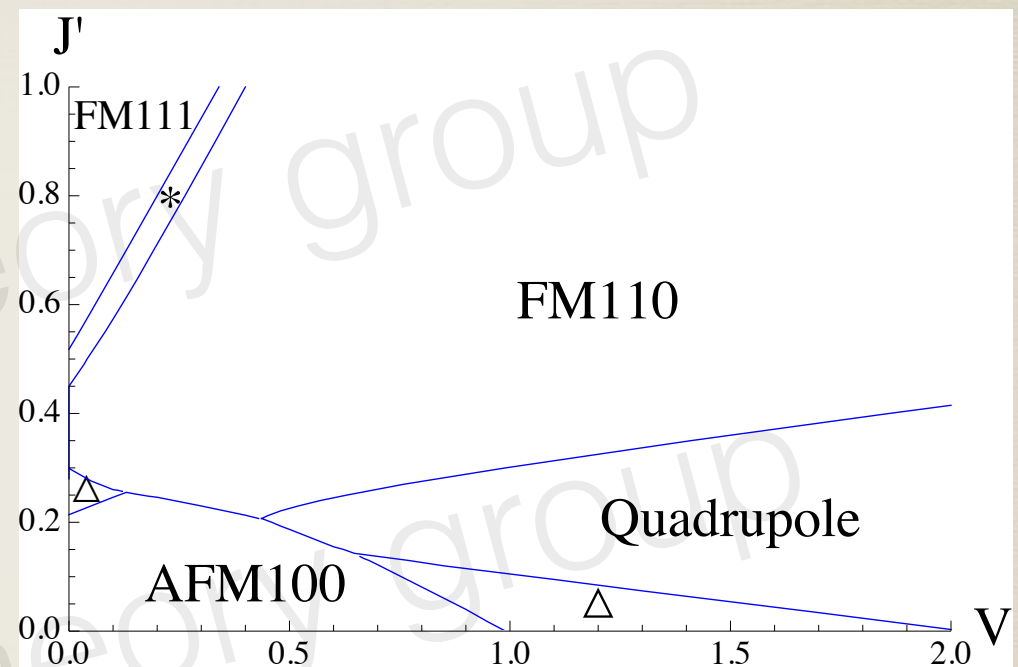
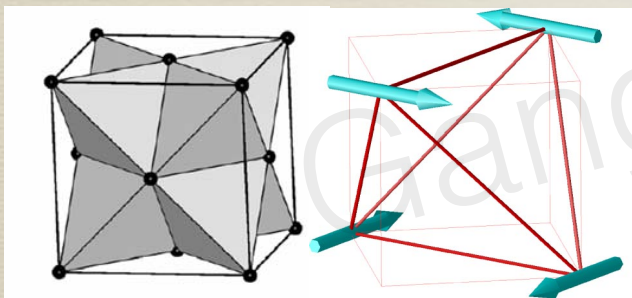


FIG. 1. (Color online) Ground state phase diagram. “ Δ ” phase is a four-sublattice AFM phase; “*” phase is an intermediate ferromagnetic phase between FM110 and FM111 phase. $J = 1$ in the phase diagram.



These variational states are found to be stable by linear flavor wave theory.

orbital-orbital interaction favors a non-collinear spin structure

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Quadrupole phase
- * Four-sublattice AFM state: Δ

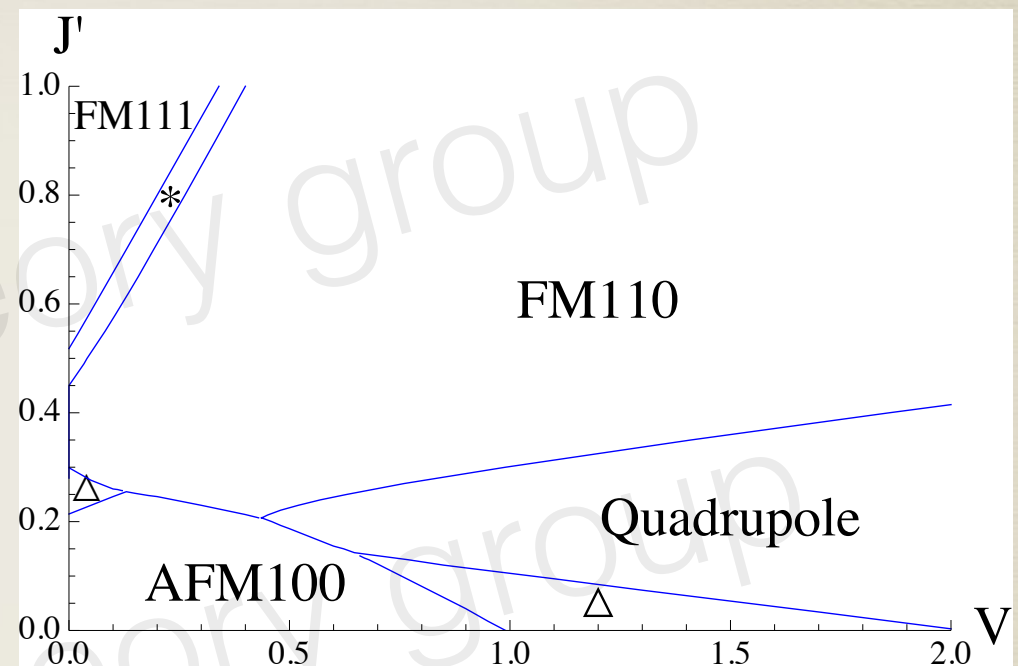
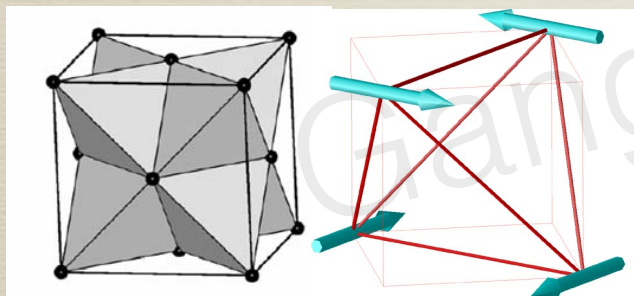


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e.g. the wavefunction of A/B sublattice of the Quadrupole phase is

$$|A\rangle = \frac{1}{2}|j^z = 2\rangle + \frac{1}{\sqrt{2}}|j^z = 0\rangle + \frac{1}{2}|j^z = -2\rangle$$

$$|B\rangle = \frac{1}{2}|j^z = 2\rangle - \frac{1}{\sqrt{2}}|j^z = 0\rangle + \frac{1}{2}|j^z = -2\rangle$$

Preserve time reversal symmetry, no magnetic dipolar order but a **spin nematic order**!

Magnetic multipole order: dipole, quadrupole, octupole!

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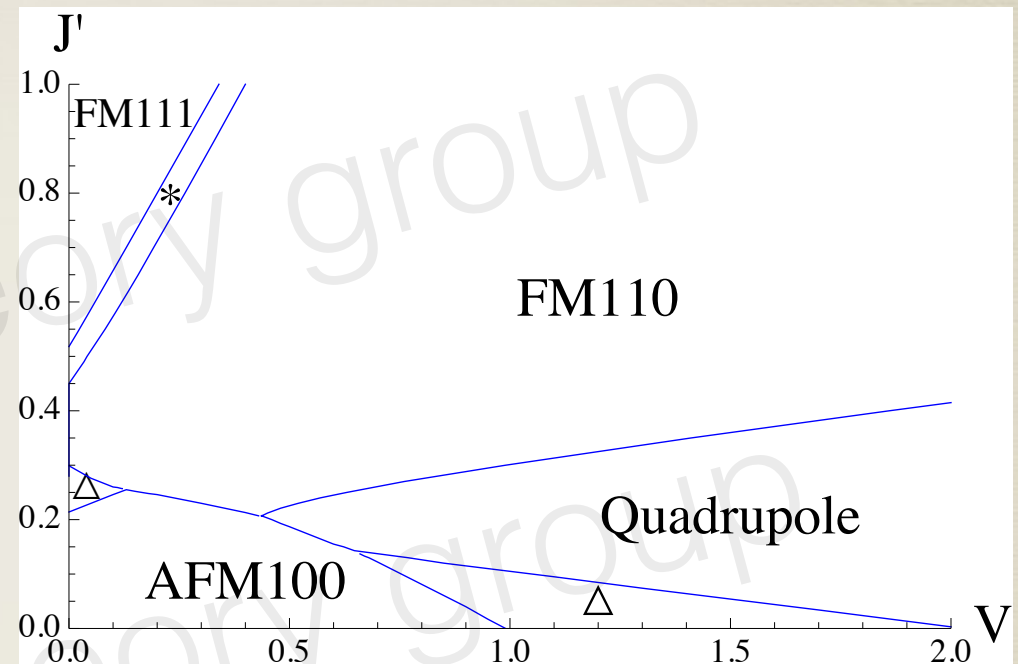
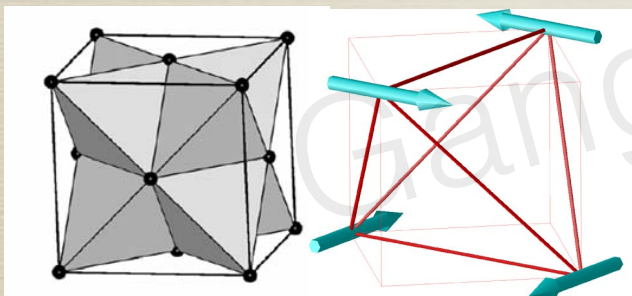


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Also seen in
NiGa₂S₄!

Preserve time reversal symmetry, no magnetic dipolar order but a **spin nematic order!**

Magnetic multipole order: dipole, quadrupole, octupole!

Finite temperature phases

- * Numerical calculation from MFT suggests that there exists a **spin-nematic phase** (which preserves **time reversal symmetry**) in the intermediate-temperature for some region of the phase diagram.

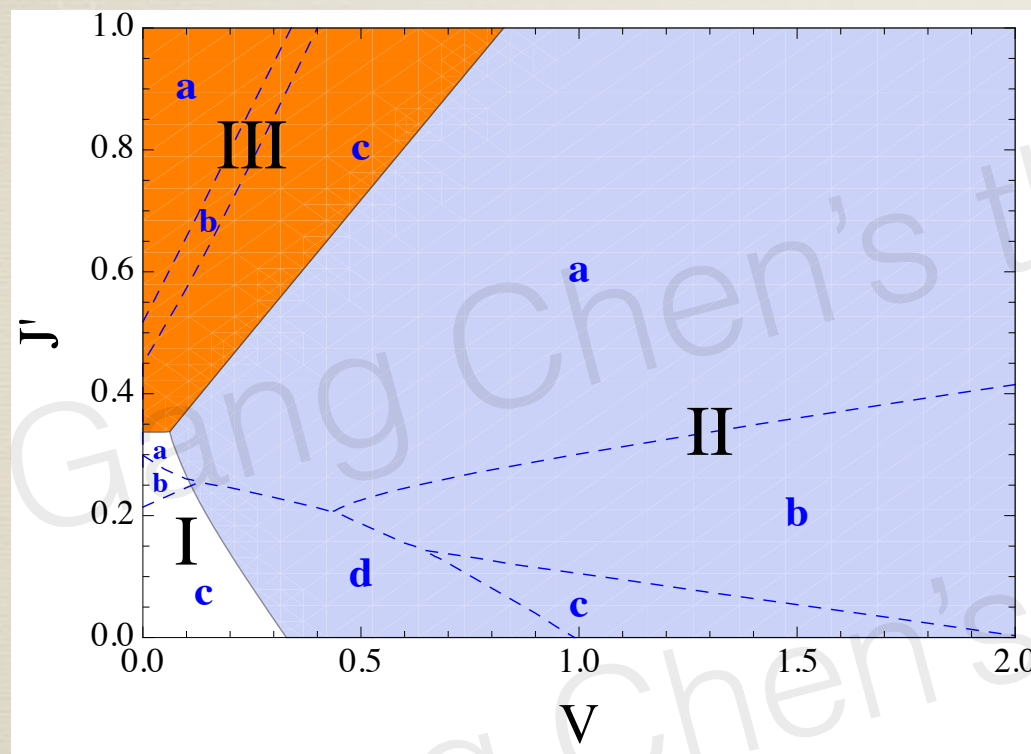
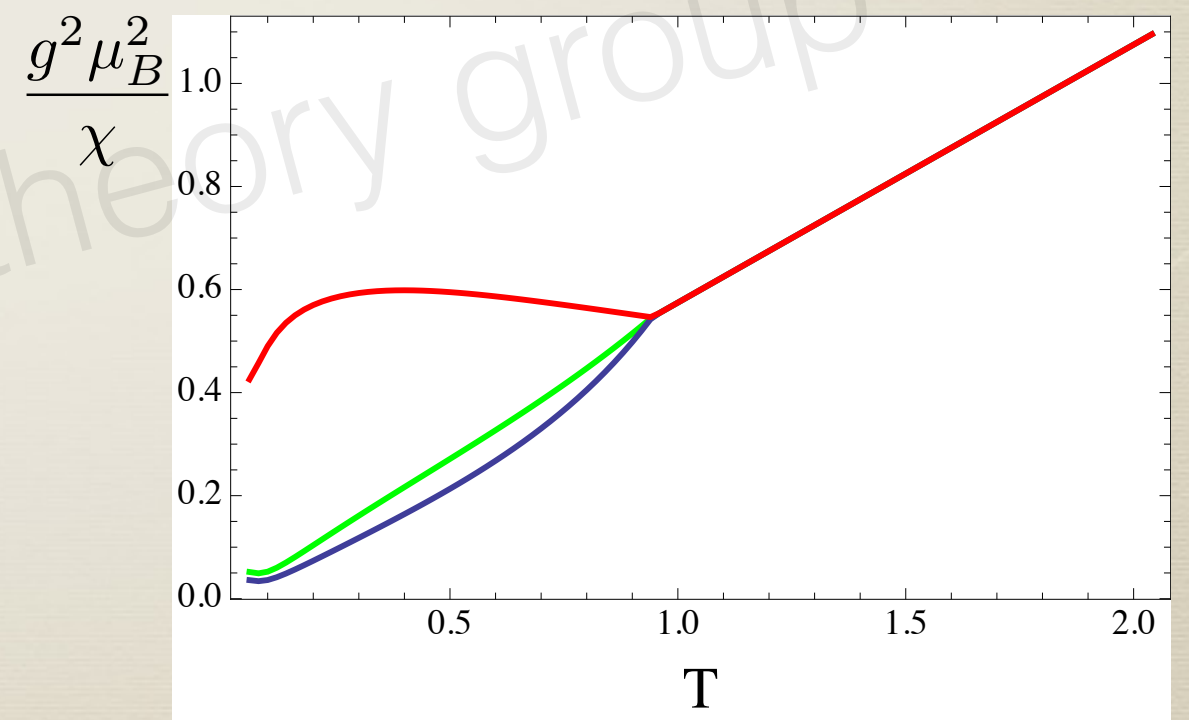


FIG. 3. (Color online) Finite temperature phase diagram. Region I (white) corresponds to a thermal transition from/to paramagnetic phase at $T_m(\mathbf{p} = 2\pi(001))$, region II (blue) corresponds to a thermal transition from/to paramagnetic phase at $T_Q(\mathbf{p} = 2\pi(001))$, region III (red) corresponds to a thermal transition from/to paramagnetic phase at $T_m(\mathbf{p} = 0)$. Dashed curves are phase boundaries of the ground state phases taken from Fig. 1. “a, b, c, d” label the low temperature phases of each region. $J = 1$ in the phase diagram.

10 subregions in total!
Region II (light blue): **spin nematic phase** at intermediate temperatures



(b) $J' = 0.2J$, $V = 0.55J$ in Π_b

Chen and Balents, (in preparation)

Experiments

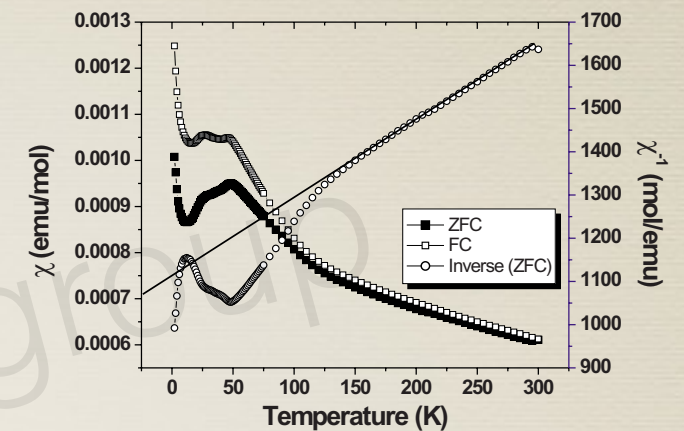
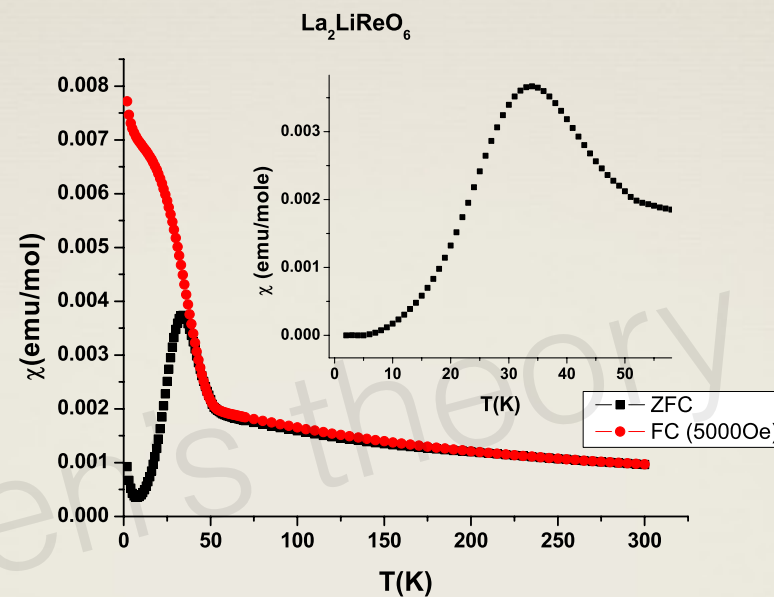
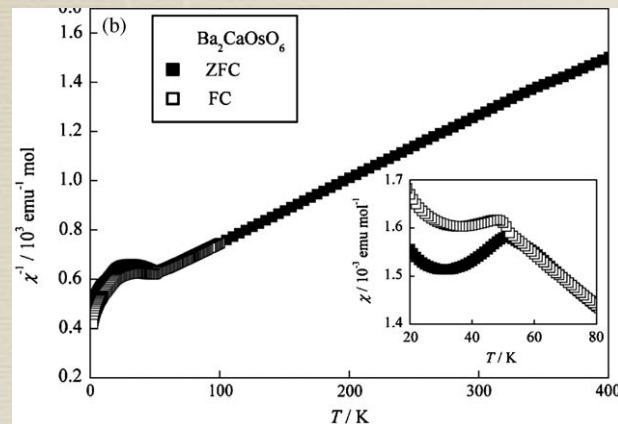
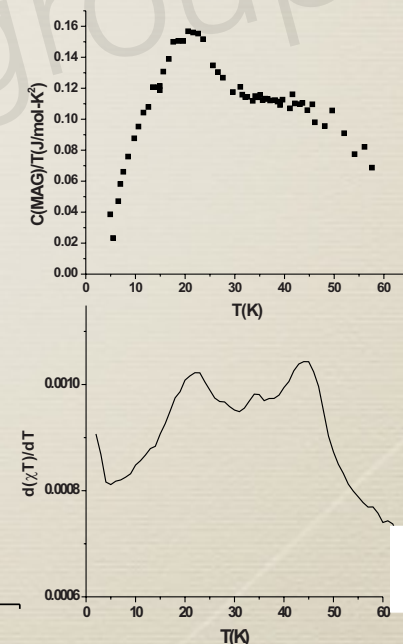
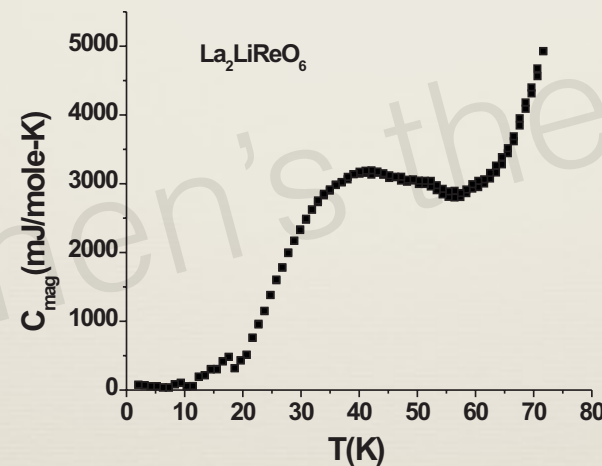
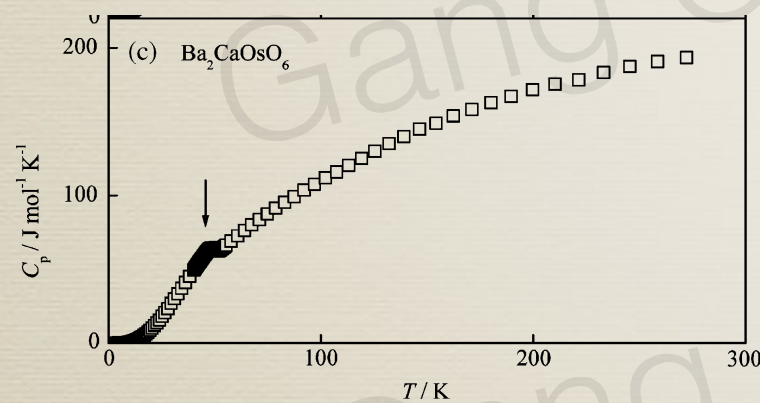


FIG. 12. (Color online) The magnetic susceptibility of Ba_2YReO_6 . A Curie-Weiss fit of the inverse susceptibility data, solid line, yields the parameters $C=0.554(5)$ (emu/mole K) and $\theta=-616(7)$ K.



$\text{Ba}_2\text{CaOsO}_6$

Single AFM phase transition corresponds to phases in region I

$\text{La}_2\text{LiReO}_6$ and Ba_2YReO_6

Seem to suggest **two** thermal transitions: two Curie regime!

Experiments: Aharen, et al PRB 81,064436, (2010)
Yamamura, et al JSSC 179 (2006) 605–612

Summary

- * We study a geometrically frustrated magnetic system with strong SOC
- * We find various zero temperature ground states and finite temperature phases in ordered double perovskites
- * Single crystal samples and NMR+Neutron are required to identify these phases.