

Search for quantum spin liquids in real materials

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Outline

- Introduction to quantum spin liquids
- Materials' survey: failed and promising candidates for quantum spin liquids
- Summary and outlook

i will discuss one failed and one promising candidate for QSLs

Physical systems **usually** order at low enough temperatures

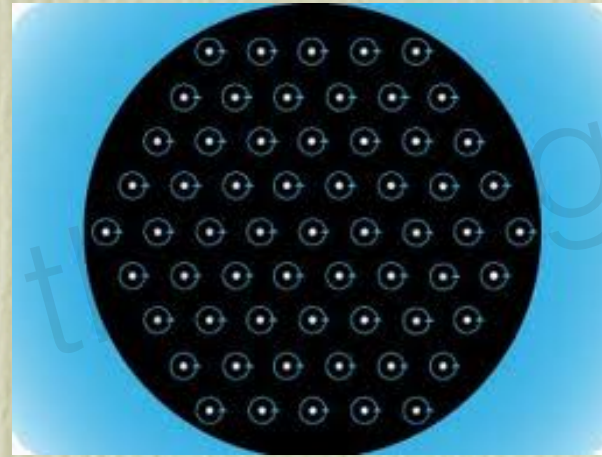
One important goal of condensed matter is to understand different phases of matter.

We know the matter usually orders in some way at low enough temperature. e.g. in crystal, atoms develop crystal order, He-4, the system develops SF order, spin system, spin develops magnetic order.

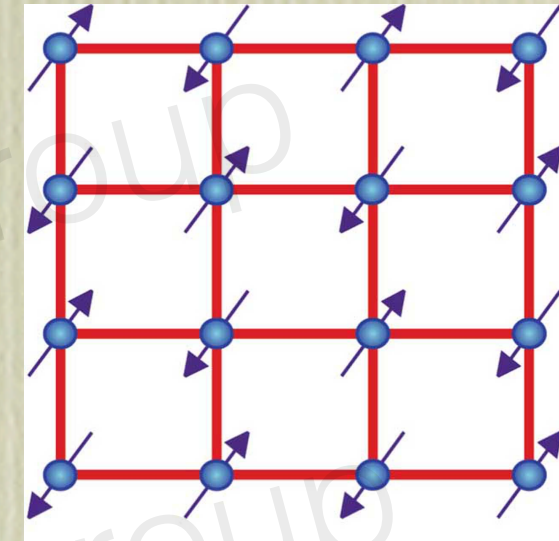
As pointed out by Landau, all these ordered phases can be understood from symmetry breaking. For example, He-4 SF breaks internal $U(1)$ symmetry, and spin system breaks translational spin and time reversal.



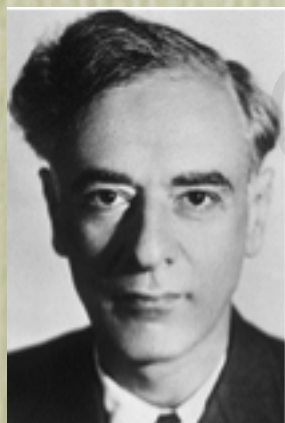
Atoms develop crystal order



He-4 liquid develops superfluid order



Spins develop magnetic order



Landau

Break
translation symmetry
rotational symmetry
etc

Break
an internal
 $U(1)$ symmetry

Break
spin rotation
translation symmetry
time reversal symmetry
etc

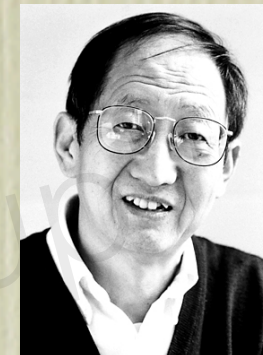
Modern **exception**: FQHE



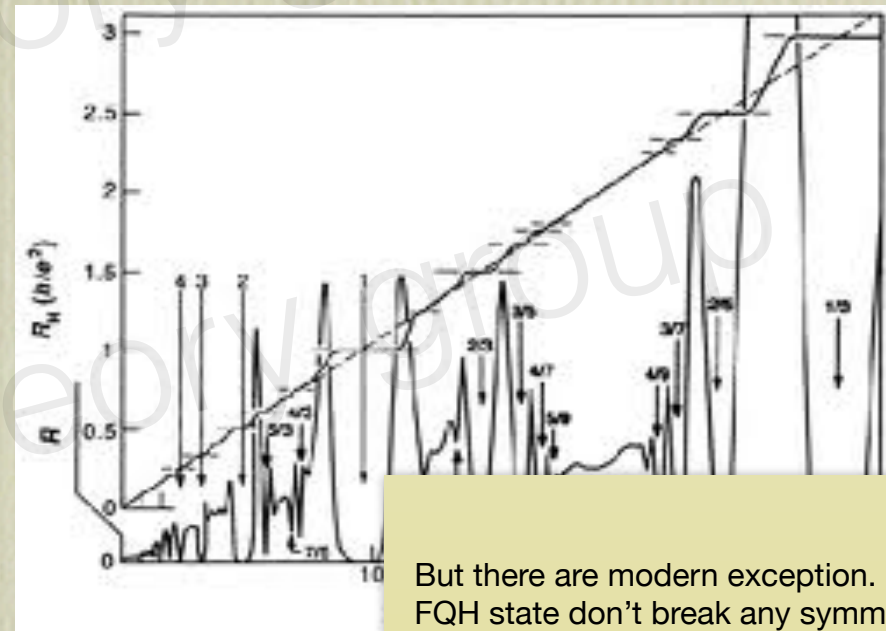
Laughlin



Stormer



Tsui



Spin exceptions: quantum spin liquids

Motivation:

Look for spin states/phases that

- * do not break any symmetry (more precisely, symmetry is not essential to define the phase),
- * do not have long-range spin order.
- * have emergent gauge field and fractional excitation.

This novel phase is called “quantum spin liquid”.

QSL is an example of this new class of matter that cannot be characterized by Landau symmetry breaking theory.

QSLs don't have spin long-range order, have emergent gauge field and fractional excitation.

The name “liquid” comes from simple analogy with water liquid. In water liquid, there is density short range order, but there is no density long range order. Similarly, in spin liquid, there is spin short range order, but not spin long range order. This is the only analogy they have.

QSL and a classical liquid (e.g. water):
no long range order but no long range order

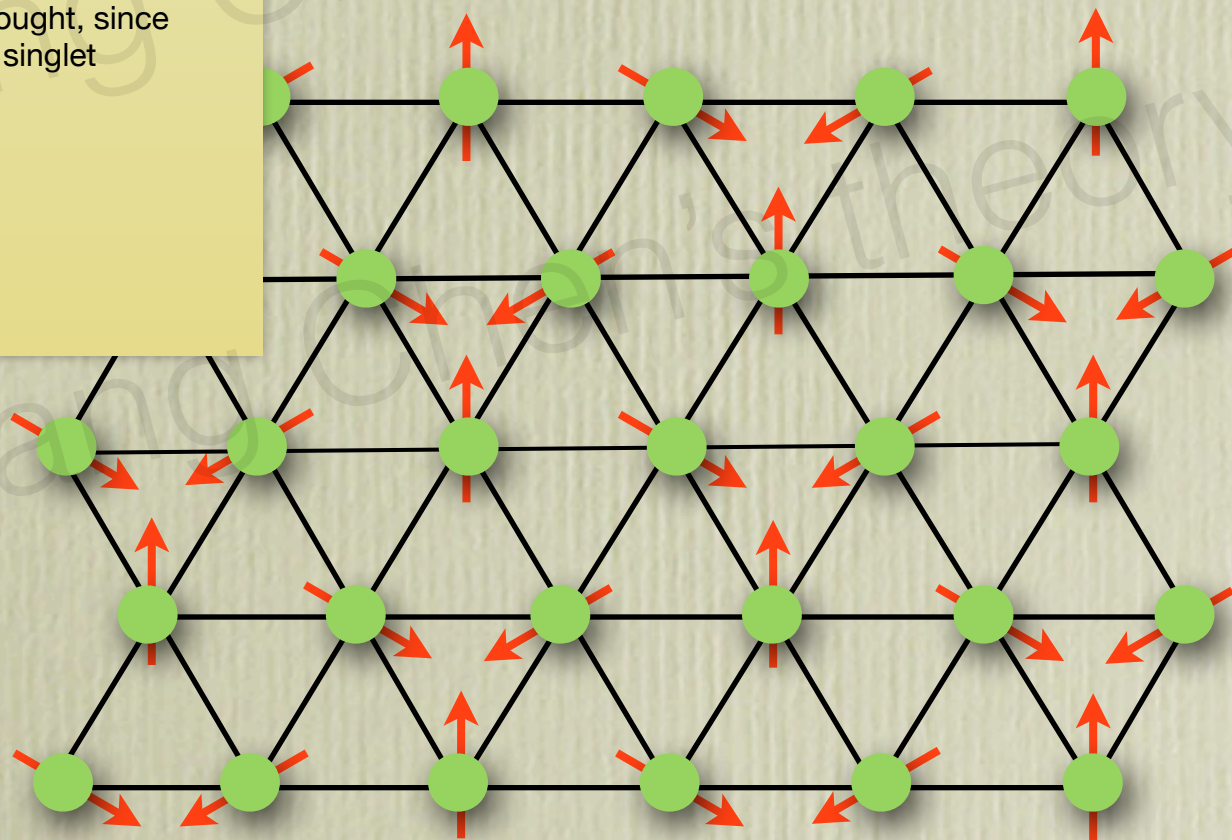
snapshot of molecules
in liquid water

1973 Anderson's resonant valence bonds

Nearest-neighbor antiferromagnetic Heisenberg model on triangular lattice

$$H = J \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j, \quad J > 0, S = \frac{1}{2}$$

let me start with some history of QSL. 1973, anderson was thinking about the gs of NN AFM heisenberg model on triangular lattice with spin 1/2. now we know it has 120 degree long range order. but that time, he did not know. he thought, since spin is quantum, they tend to form a singlet



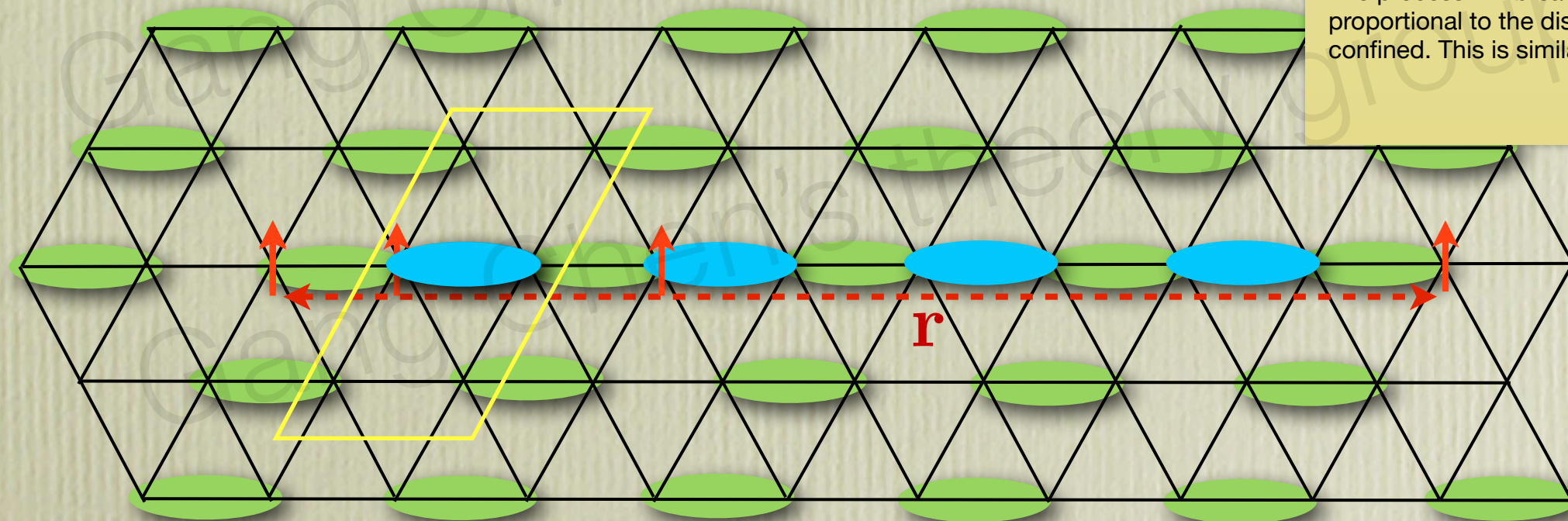
Long-range order
120-degree state

1973 Anderson's resonant valence bonds

dimer/singlet/ valence bond

$$\text{green oval} = \frac{1}{\sqrt{2}} \left(\begin{array}{c} \uparrow \\ \downarrow \end{array} \right)$$

Valence bond solid: columnar dimer state (break tra



$$E \propto |\mathbf{r}|$$

“with a finite string tension”,
spinons (carrying spin-1/2) are linearly confined.

he thought, since spin is quantum, they tend to form a s
often called dimer or valence bond in literature. Let's fir
in which, the dimers develop a crystal order. If we break
create a triplite excitation.

The spin are carried by
two spinons (each spinon carry spin -1/2), and then sep

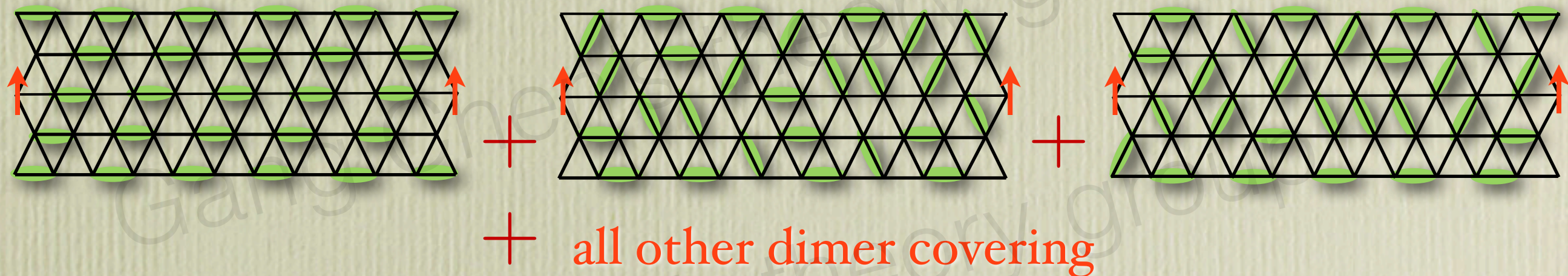
This process creates domain wall, it will cost a finite en
spinons further, it will disrupt a lot of dimer in between.
be proportional to the separation between two spinons.
spinons are linearly confined. This is reminiscent of the c
confinement in qcd. One can imagine that the two spin
a string, and the string has a finite tension.

(one way to see this, is to compute the expectation valu
with respect to the excited state.)

The process will break a lot of dimer in between, the en
proportional to the distance between the spinons. As a
confined. This is similar to the quark matter confinement

1973 Anderson's resonant valence bonds

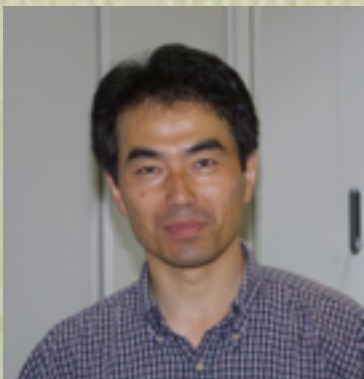
With a RVB state (Moessner, Sondhi, PRL2001),



dimers are strongly fluctuating, the “string tension” vanishes and the spinons are *deconfined*.

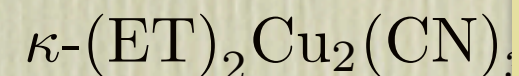
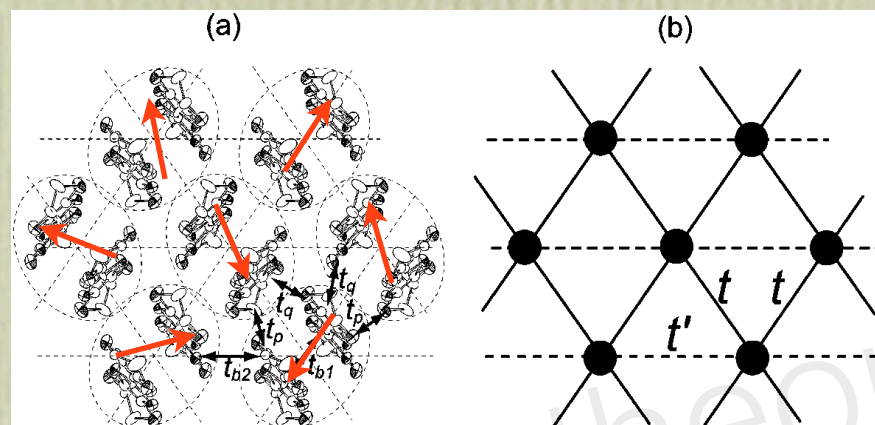
1987, Anderson further proposed that RVB/spin liquid state might be relevant to high- T_c superconductor. Cuprates don't have such a QSL regime. The Mott insulator has AFM Neel order.

but if we have state which is a linear superpositions of all possible dimer



Kanoda

2003 Kanoda's organics

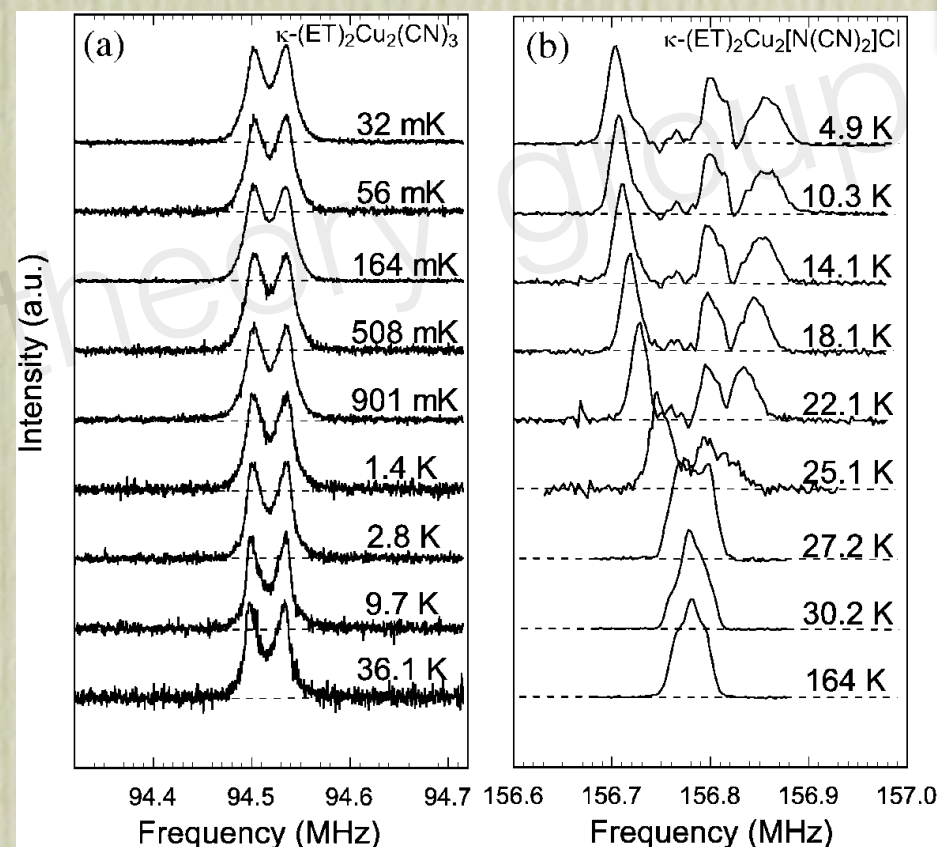
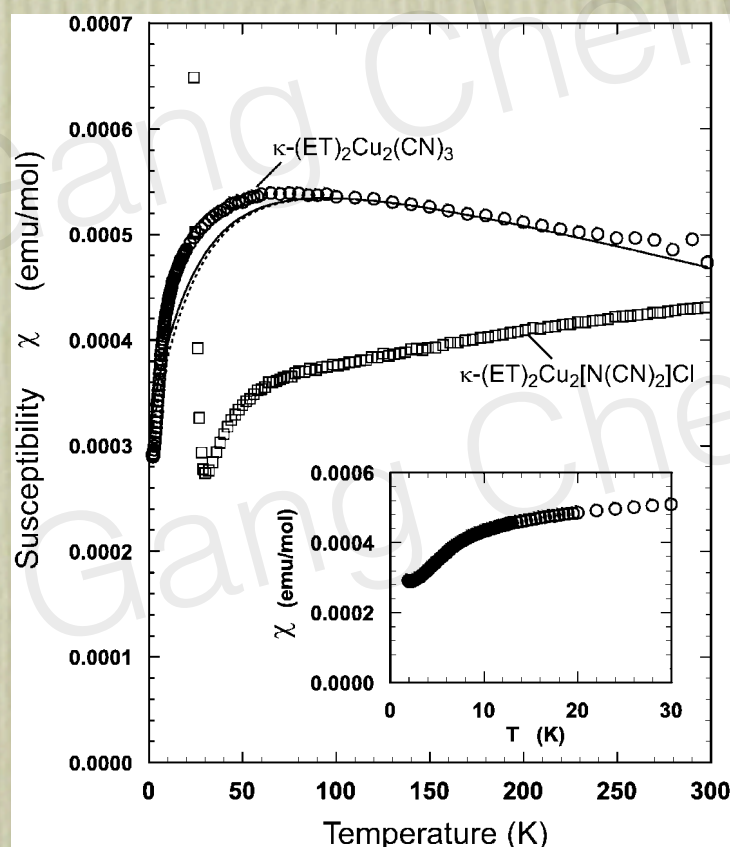


- * molecular ET₂ dimer
- * triangular lattice, spin
- * close to metal-insulator

For a long time, there is on

Experimental breakthrough
kanoda discovered an org
molecular dimer carries sp
the system is close to met
side.

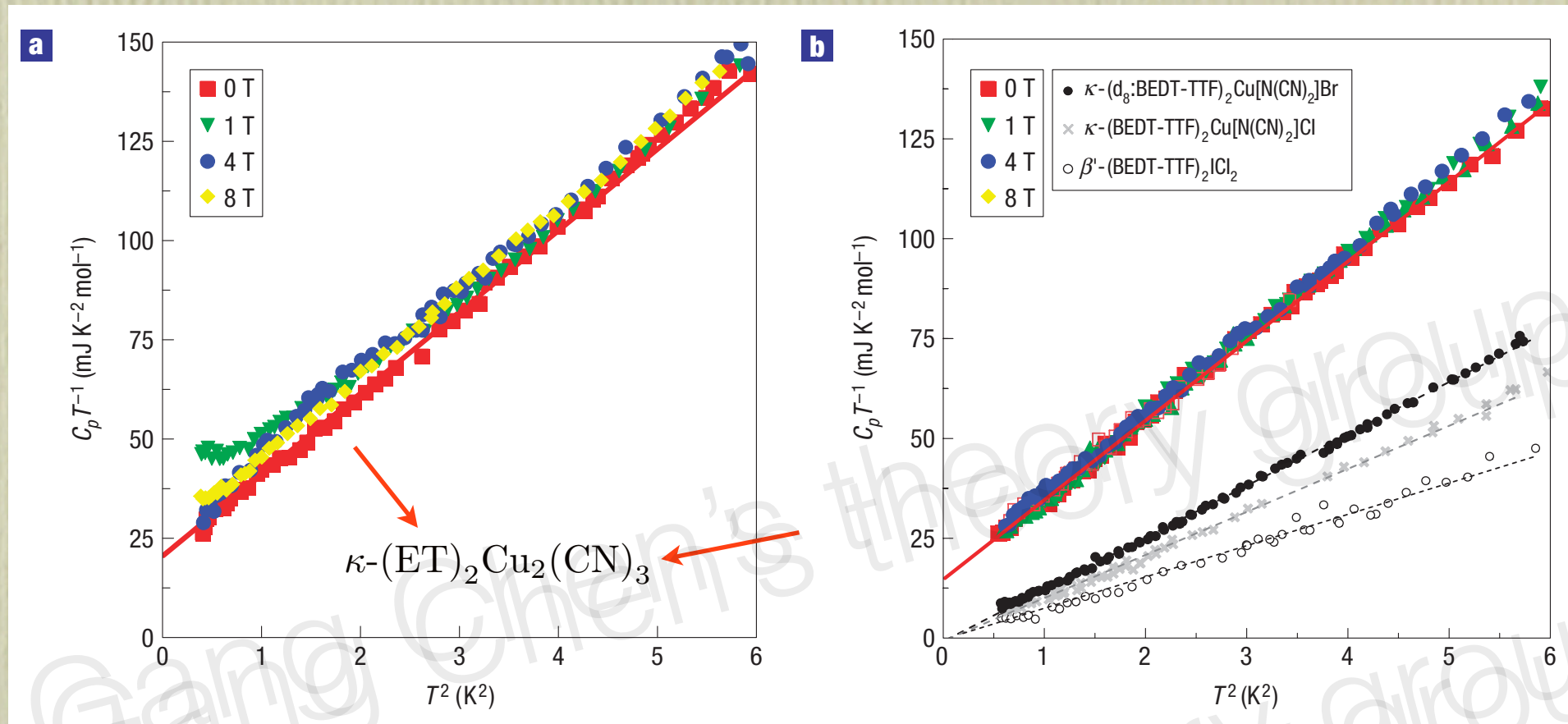
Both spin susceptibility and
spin suscep is constant at



- * No magnetic order down to 32mK
- * constant spin susceptibility at zero temperature

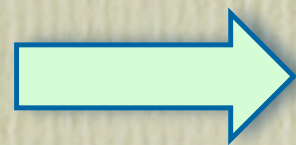
Shimizu, etc, PRL, 91,107001

* Heat capacity



Yamashita, etc, Nature Physics, 4, 459, (2008)

$$\begin{aligned} * & C_v \propto T \\ * & \chi \propto \text{const} \end{aligned}$$



**QSL with a spinon
Fermi surface?**

the heat capacity measurement obtain a linear-T dependence at low temperature limit.

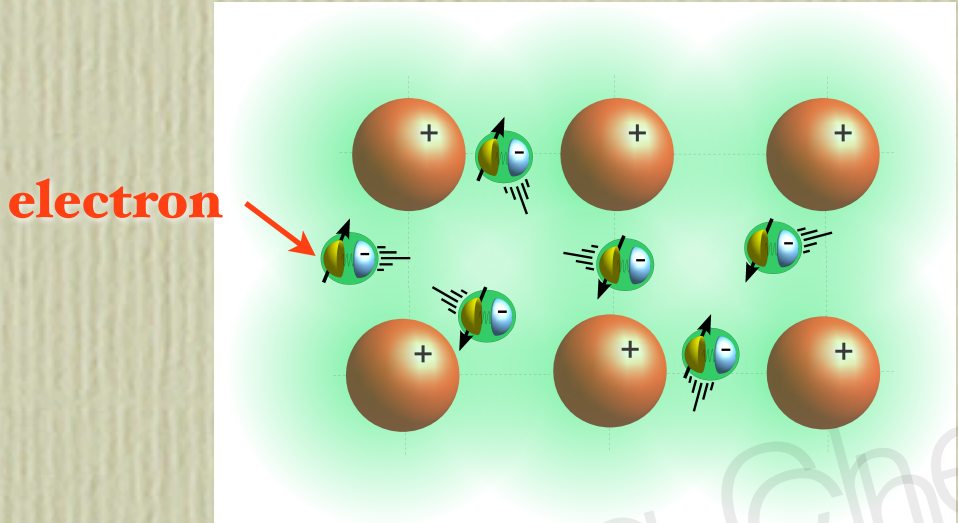
Constant spin suscep and linear-T heat capacity suggest the large density of low energy state. It is postulated to be spinon fermi surface.

QSL with spinon Fermi surface

To describe the state, we split the electron operator into the electron in this way enlarges the physical Hilbert space is to project out the unphysical states. The other spinon and charge back into an electron. I am going to

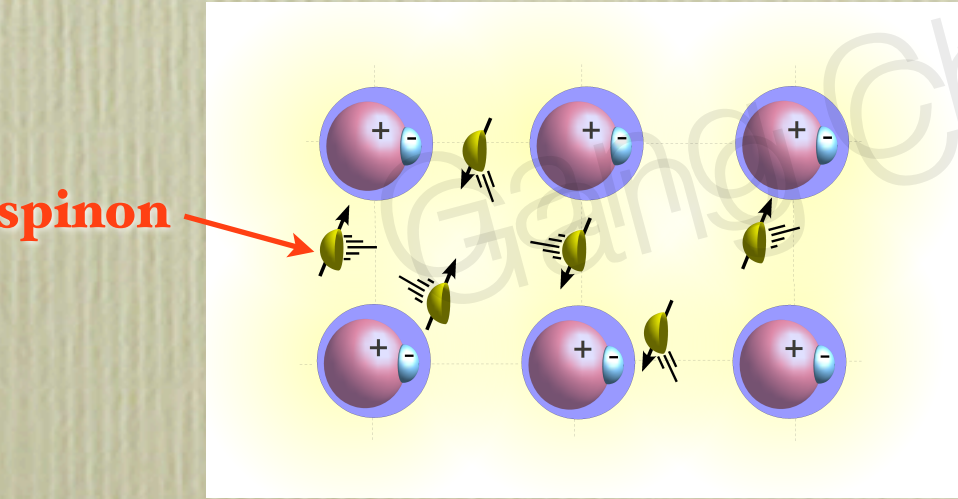
In the metallic phase, charge boson is condensed, gauge in the mott insulator, boson are not condensed, the gauge charge are deconfined. The charge is localized and the

The low energy theory of this QSL is described by spin



Metal

“electrons swimming in the background of positively charge ions.”



Mott insulator: QSL (spinon metal)

“electron charge is pinned to the ion site while the spin still swims freely.”

split the electron into charge

$$c_{r\sigma} = b_r f_{r\sigma}$$

but glue them back to electron with gauge fields.

phases	charge boson	gauge field	spin-charge separation
metal	$\langle b_r \rangle \neq 0$	higgsed	$c_{r\sigma} = \langle b_r \rangle f_{r\sigma}$
Mott-QSL	$\langle b_r \rangle = 0$	strongly fluctuating	Yes

Low-energy theory of Mott QSL
fermionic spinons coupled to U(1) gauge field.

theory: Motrunich, Lee, Lee, Senthil, etc

Many QSLs with many different low energy theories

QSLs	low-energy theory
U(1) QSL	QED (w/ monopole)
Dirac QSL	Dirac spinon couple to QED
nodal QSL	nodal spinon couple to Z_2 gauge
Majorana QSL	Majorana spinon couple to Z_2 gauge
Fermi surface QSL	spinon FS couple to U(1) or Z_2 gauge
.....

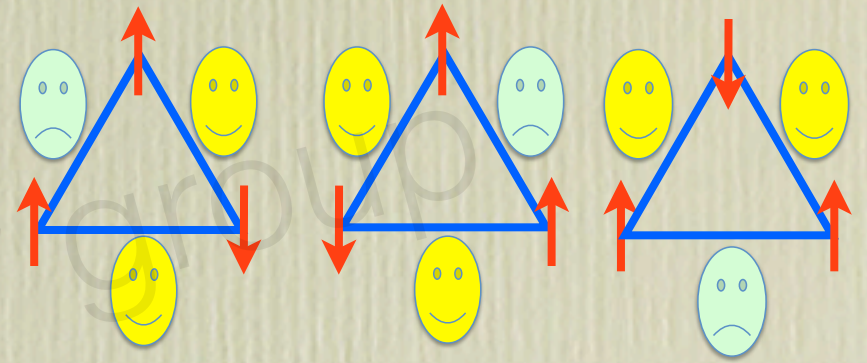
What's remarkable is the low-energy theory has little to do with the microscopic theory, which is just some bosonic spin exchange model.

Now we know there are many different QSLs with quite different low energy theory. What's remarkable is that, the low energy theory has little to do with the microscopic theory, which is just some bosonic spin exchange model.

even though all come, the emergent low-E theory is completely different.

Where to search for QSL

- system with frustration (competing interaction)
- quantum spins, e.g. $S=1/2$
- proximate to metal-insulator transition: large charge fluctuation
- others: strong spin-orbit coupling, quenched disorder, etc



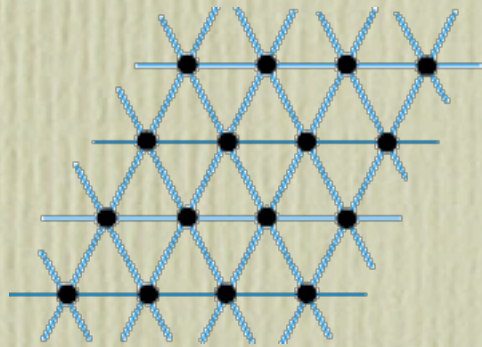
Since qsl is stabilized by quantum fluctuation, we need to search among the systems with strong quantum fluctuation. The following are some guidance.

The first one is frustrated system. frustration means competing interaction cannot be optimized simultaneously. A classical example is AFM ising model on triangular lattice. No matter how you arrange the spin, there is always one unhappy bond.

the second one is system with small spin moment, the most quantum one is spin $1/2$.

the third is system near metal-insulator transition, where the charge fluct are

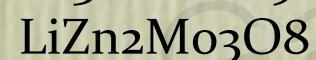
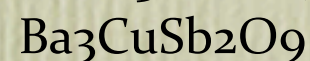
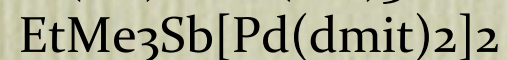
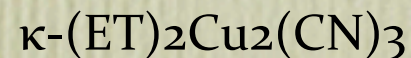
Many candidate materials now!



triangular lattice



He-3 layers on graphite

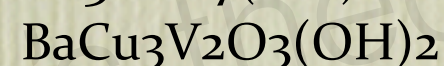
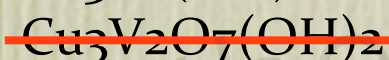
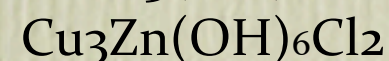
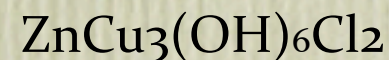


since 2003, experimentalists have discovered many QSL candidates.

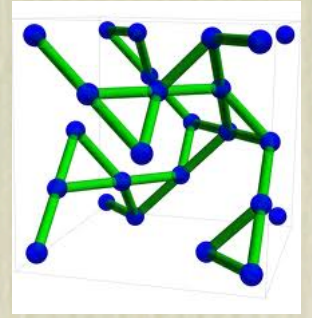
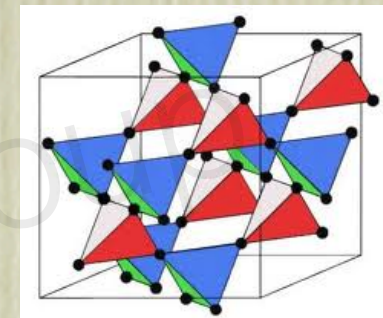
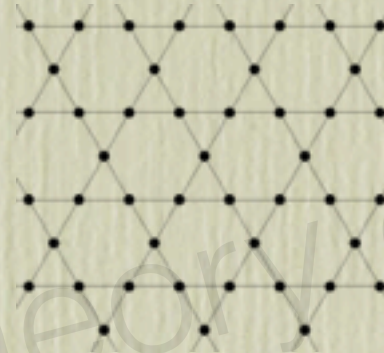
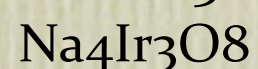
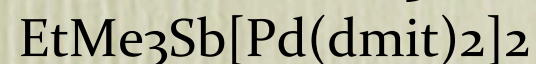
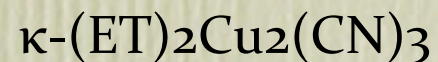
Some of them have already been ruled out to be QSL.



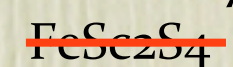
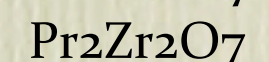
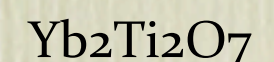
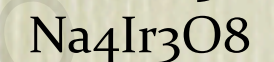
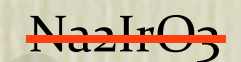
kagome lattice



Proximate to Mott transitions

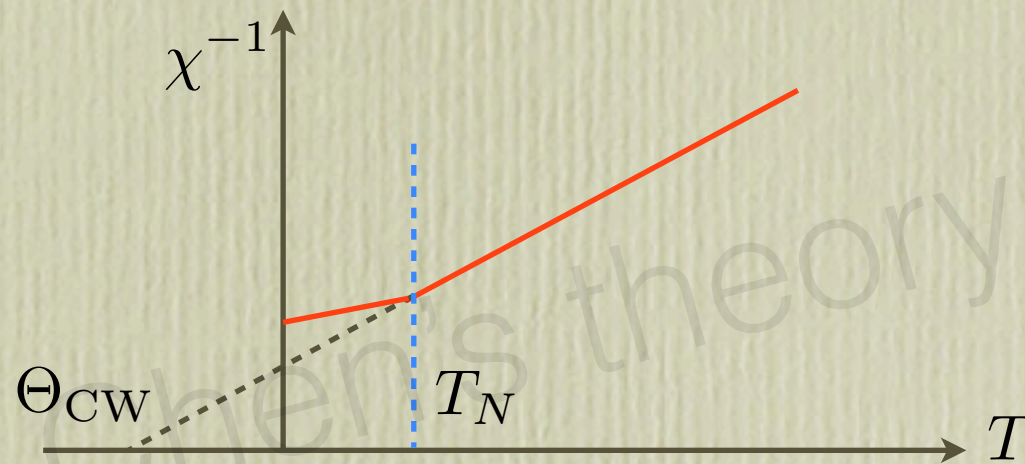


Strong spin-orbit coupling



* Some common phenomenology

- No ordering down to lowest measurable temperature, i.e. a large frustration parameter $f \equiv \frac{|\Theta_{CW}|}{T_N}$



- Constant $T = 0$ spin susceptibility.
- Power-law heat capacity. $C_v \sim T^\alpha$

* Challenge

Many materials have very similar phenomenology.

Are they all quantum spin liquid?

How to connect the experiments to the theory?

We need mutual feedback between theory and experiment.

There are some common phenomenology of these QSL can. At high temp, the spin suscep obey curie-weiss law. There is no ordering down to lowest temp.

It is often useful to introduce an empirical experimental parameter, the frustration parameter, which is given by the ratio between C and T_N . In real QSL, f is infinity. In exp, we cannot reach the lowest temperature.

For instance, if CW is 100K, and lowest temp in exp is 1K, the frustration parameter is greater than 100.

the spin suscep is often const at low temp. the heat capacity shows a power-law behavior in temp at low T .

Although many materials have similar pheno, it does not mean they are all QSL.

this is like biology.

you know,

whales and dolphin look like fish, but they are not fish.

they are more interesting and advanced creatures.

The challenge is to tell which material is qsl and the type of qsl. It is also to tell which material is not qsl and if it is not, what is it. The last part needs careful examination of the experiments and material.

failed examples

candidate materials	spin	lattice	f	explanation
Cs_2CuCl_4	1/2	triangle	$f \sim 8$	dimensional reduction
$\text{Cu}_3\text{V}_2\text{O}_7(\text{OH})_2$	1/2	kagome	$f > 30$	magnetic order
Na_2IrO_3	1/2	honeycomb	$f \sim 10$	magnetic order
NiGa_2S_4	1	triangle	$f \sim 10$	spin nematics
FeSc_2S_4	2	diamond	$f > 900$	spin-orbital singlet
.....				

If any one is interested in any of the materials, we can talk after the talk.

promising ones

Candidate QSL	spin	lattice	susceptibility	Cv	f	possible QSL
$\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$	1/2	triangle	constant	$C_v \sim T$	$f > 1000$	spinon FS
$\text{EtMe}_3\text{Sb}[\text{Pd(dmit)}_2]_2$	1/2	triangle	constant	$C_v \sim T$	$f > 1000$	spinon FS
$\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$	1/2	kagome	-----	-----	$f > 1000$	Dirac QSL
$\text{Cu}_3\text{Zn}(\text{OH})_6\text{Cl}_2$	1/2	kagome	constant	$C_v \sim T$	$f > 475$	Majorana QSL
$\text{Na}_4\text{Ir}_3\text{O}_8$	1/2	hyperkagome	constant	$C_v \sim T$	$f > 300$	U(1) QSL with FS
$\text{Pr}_2\text{Zr}_2\text{O}_7$	1/2	pyrochlore	constant	-----	$f > 70$	U(1) (quantum spin ice)
.....						

Experimental work by C. Broholm's group, H. Takagi's group, Kanoda's group, Y. Lee's group, Lhuillier's group.

In the following part of the talk, I will discuss two materials, one is probably not QSL but still very interesting. The other is probably a QSL.

The first work is in collaboration w/

The second work is in collaboration w/

Plan

- A probably failed but very interesting QSL candidate: $6\text{H-B-Ba}_3\text{NiSb}_2\text{O}_9$

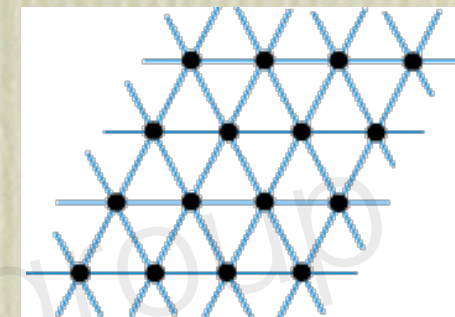
Collaborators: * Michael Hermele (Univ of Colorado Boulder)
* Leo Radzihovsky (Univ of Colorado Boulder)

Refs: GC, Hermele, Radzihovsky, PRL 109, 016402, 2012

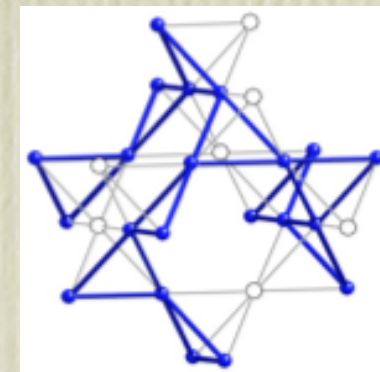
- A very promising QSL candidate:
 $\text{Na}_4\text{Ir}_3\text{O}_8$

Collaborators: * Yong-Baek Kim (Univ of Toronto)

Refs: GC, Kim, unpublished



triangle



hyperkagome

last year, Dr. Balicas from high magnetic lab discovered three different structures of this material under high pressure. It is a spin-1 system. These are the exp data.

$\text{Ba}_3\text{NiSb}_2\text{O}_9$ -a spin-1 AFM



Balicas

J. Cheng, etc, PRL, 107,197204 (2011)

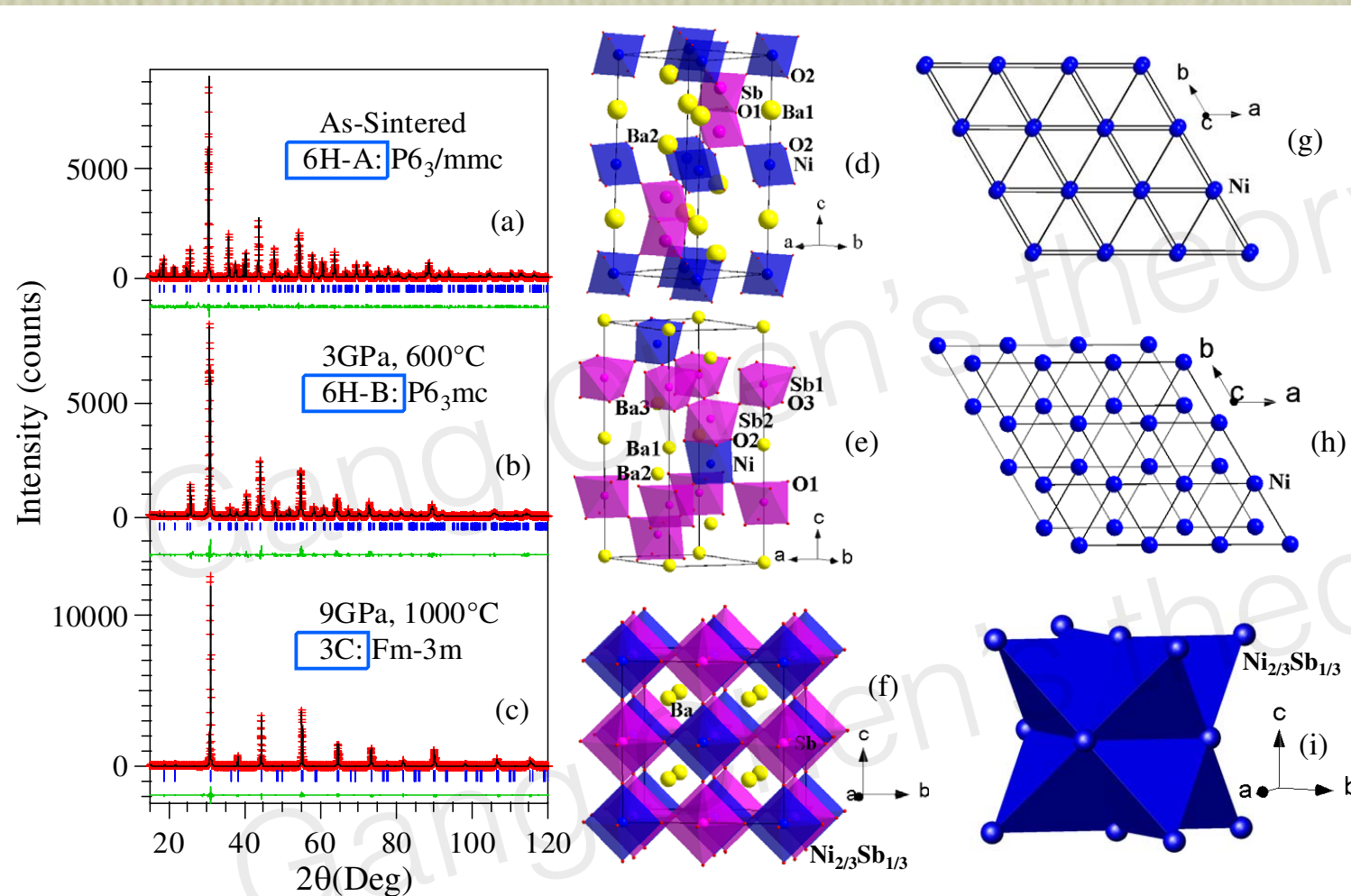
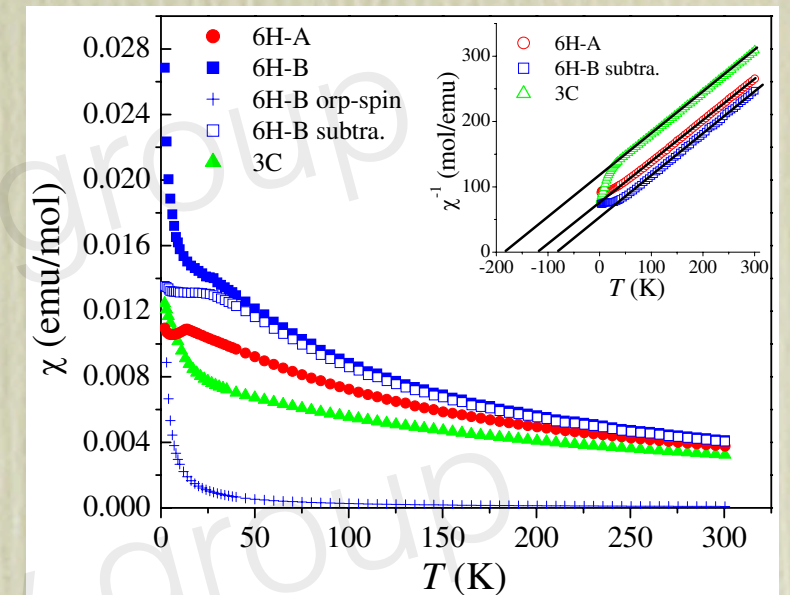
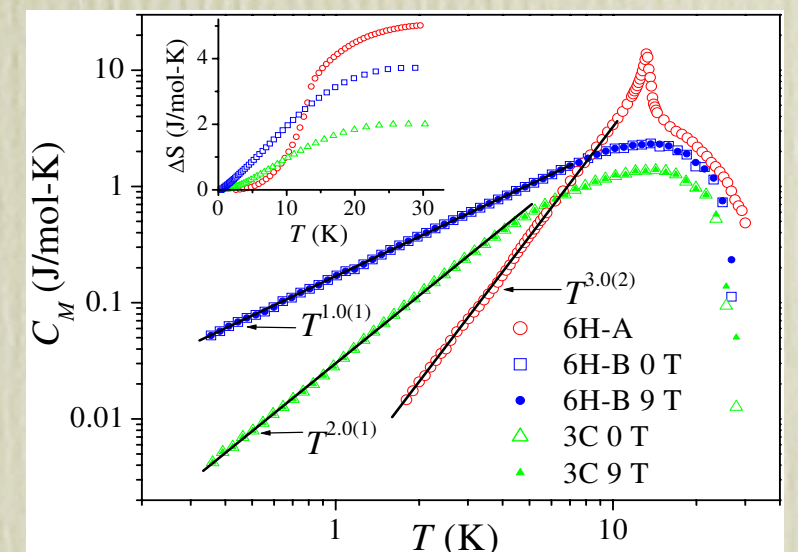


FIG. 1: Powder XRD patterns (crosses) at 295 K for the $\text{Ba}_3\text{NiSb}_2\text{O}_9$ polytypes: (a) 6H-A, (b) 6H-B, and (c) 3C. Solid curves are the best fits obtained from Rietveld refinements using FullProf. Vertical marks indicate the position of the Bragg peaks, with the curves at the bottom showing the difference between the observed and the calculated intensities. Schematic crystal structures for the $\text{Ba}_3\text{NiSb}_2\text{O}_9$ polytypes: (d) 6H-A, (e) 6H-B, and (f) 3C. Magnetic lattices composed of Ni^{2+} ions for the $\text{Ba}_3\text{NiSb}_2\text{O}_9$ polytypes: (g) 6H-A, (h) 6H-B, and (i) 3C.

three high-pressure structures

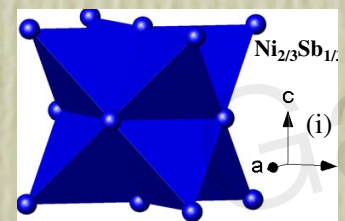
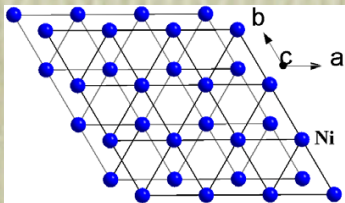
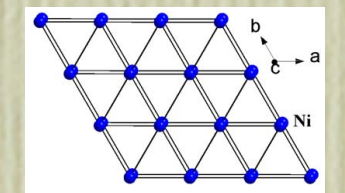


spin susceptibility



heat capacity

Summary of experiments on Ba₃NiSb₂O₉



spin-1 system	structure	$T=0$ susceptibility	heat capacity	explanation
6H-A	A-A stacking	const	$C_v \propto T^3$	magnetic order
6H-B	A-B stacking	const	$C_v \propto T$	QSL?
3C	FCC with 1/3 dilution	const	$C_v \propto T^2$	QSL?

Other's work

Serbyn, Senthil, P. Lee, PRB 84,180403, 2011

- * Z₂ QSL with spinon Fermi surface
- * Rely on **large and positive** biquadratic exchange $K(\mathbf{S}_i \cdot \mathbf{S}_j)^2$

Xu, Wang, Qi, Balents, Fisher, PRL 108, 087204, 2012

- * Z₂ QSL with quadratic dispersive spinons
- * Spinon MFT only has pairing
- * Energetically favorable with **negative** ring exchange

$$[(\mathbf{S}_1 \cdot \mathbf{S}_2)(\mathbf{S}_3 \cdot \mathbf{S}_4) - (\mathbf{S}_1 \cdot \mathbf{S}_3)(\mathbf{S}_2 \cdot \mathbf{S}_4) + (\mathbf{S}_1 \cdot \mathbf{S}_4)(\mathbf{S}_2 \cdot \mathbf{S}_3)]$$

$$-(\mathbf{S}_1 \cdot \mathbf{S}_3)(\mathbf{S}_2 \cdot \mathbf{S}_4)$$

Let me summary his experimental results in this table. In all the triangular layers are identical. 6H-B has A-B stacking shifted like graphite. 3C is a FCC lattice with 1/3 site dilution.

All the spin suscpt is constant at zero temp limit. The heat capacity exponent. 6H-A has AF LRO, T^3 heat capacity is due to AF LRO. It is hard to understand. Here I will focus on the 6H-B material.

There are already two other works on 6H-B material.

the first is by Mit group. senthil and patrick are proposing a state with 's gutts feeling when they see const and linear T. But this state needs a large and postive biquaer , and negative.

the other is from SB, by CenKe Xu, L Balent, M Fisher. It has spinon dispersion. But their state requires the a negative ring exchange. But

Minimal model

* Exchange interaction

$$\mathcal{H}_{\text{ex}} = J_1 \sum_{\langle ij \rangle \in \text{AB}} \mathbf{S}_i \cdot \mathbf{S}_j + J_2 \sum_{\langle ij \rangle \in \text{AA or BB}} \mathbf{S}_i \cdot \mathbf{S}_j,$$

Exchange is already frustrated, the magnetic order would be very weak if there is any.

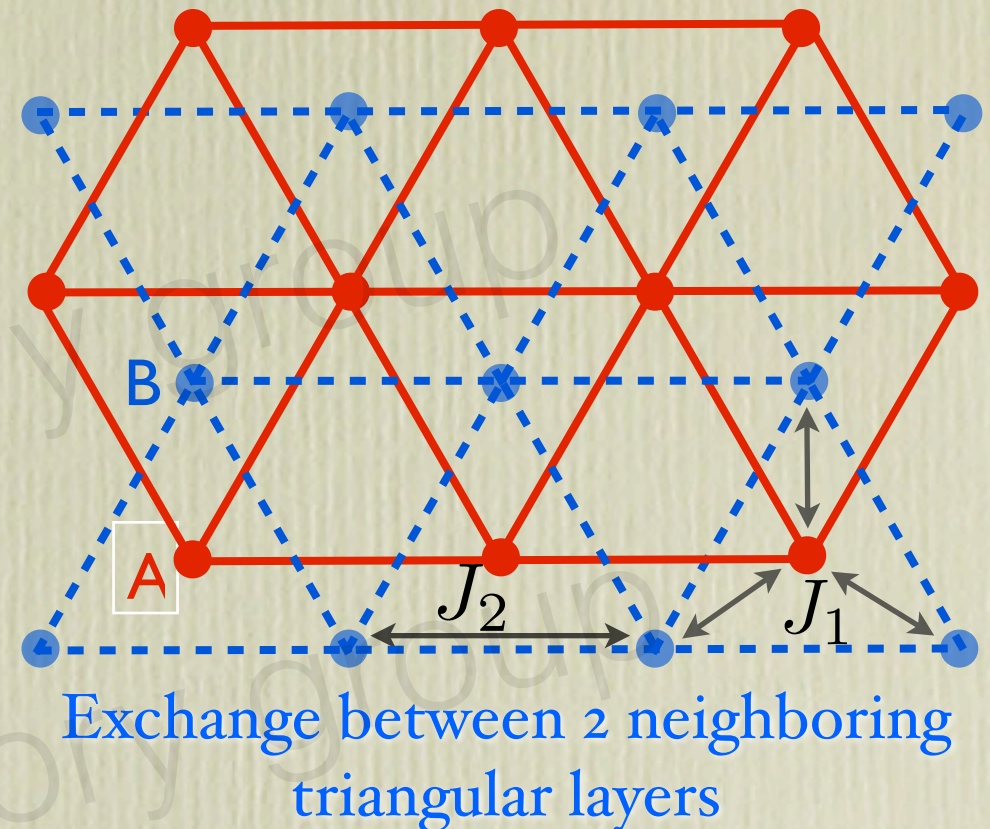
* Single-ion anisotropy allowed by symmetry and $S=1$

$$\mathcal{H}_{\text{ani}} = D \sum_i (S_i^z)^2$$

* Single-ion anisotropy would suppress the weak magnetic order and favors a trivial quantum paramagnetic state

$$\prod_i |S_i^z = 0\rangle$$

* Expect: $J_1, J_2 \gg D$ weakly ordered state
 $J_1, J_2 \ll D$ quantum paramagnetic



Here, we explain the seemingly QSL phenomenology by a conventional mechanism. Linear-T heat capacity is quite challenging as it requires a constant DOS at low T. To have a constant low energy DOS without introducing spinons. Here I provide such an explanation without introducing spinons.

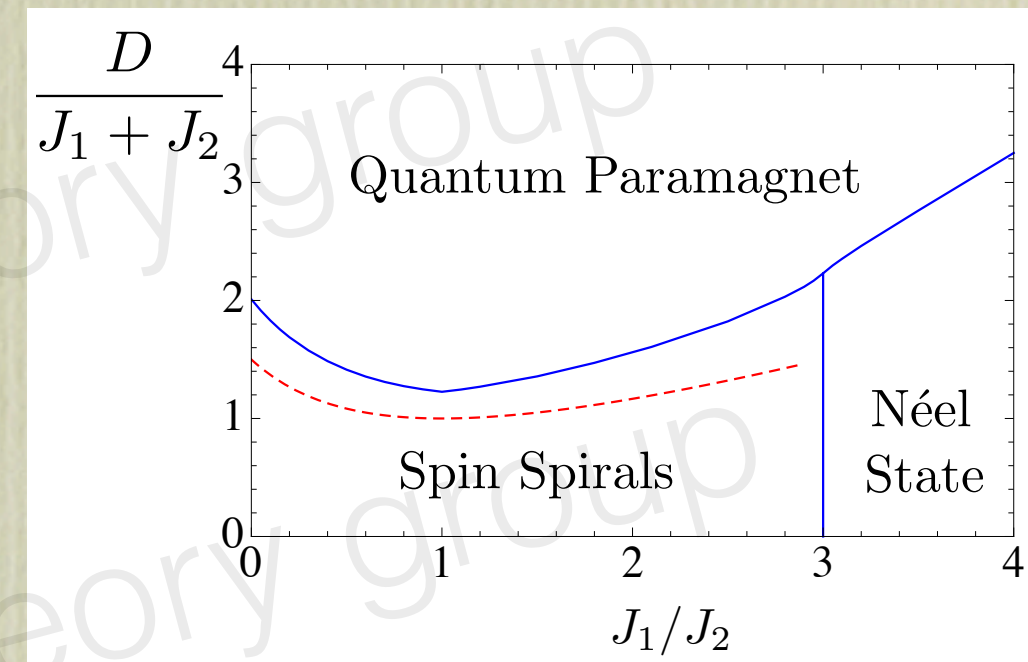
In our theory, we consider a minimal model. The first interaction is the spin exchange both intra and inter layer exchange. This exchange is frustrated, if it is ordered, the order is going to be small.

Then we add single-ion anisotropy allowed by symmetry. If anisotropy is large, the paramagnetic state is favored with the $S_z=0$ at every site.

So we expect, when exchange is dominant, we obtain a weakly ordered state, when anisotropy is dominant, we obtain a quantum paramagnetic state.

Map spin to rotor

spin	rotor
S_i^z	n_i (integer valued)
S_i^+	$\sqrt{2}e^{i\phi_i}$
$[S_i^+, S_i^-] = 2\delta_{ij}S_i^z$	$[\phi_i, n_j] = i\delta_{ij}$
XY spin order, $\langle S^+ \rangle \neq 0$	condensed boson, $\langle e^{i\phi} \rangle \neq 0$
quantum paramagnet, $S^z = 0$	uncondensed boson, $\langle e^{i\phi} \rangle = 0$



Phase diagram

At dashed curve, quadratic dispersion is obtained, so is constant DOS.

Equivalent rotor Hamiltonian

$$H_{\text{rotor}} = \frac{1}{2} \sum_{ij} J_{ij} \left[2 \cos(\phi_i - \phi_j) + n_i n_j \right] + \sum_i D n_i^2$$

This is essentially an extended boson-Hubbard model and can be solved by standard methods.

To solve our minimal model, we simplify the problem and map the spin to a rotor variable.

S_z map to rotor, S_+ map to this phase variables. Spin ordering corresponds the boson condensation of rotor. The quantum paramagnet corresponds to a uncondensed rotor.

This is the equivalent rotor Hamiltonian. This is essentially a Bose-Hubbard model and can be solved by standard methods.

Both the phase diagram and low energy spin excitation can be calculated.

The presence of inter-site density-density interaction modifies the phase diagram.

Prediction

* Spin susceptibility

field in the plane, $\chi_0^\perp = \frac{2\mu_0(g\mu_B)^2}{D + 12(J_1 + J_2)}$

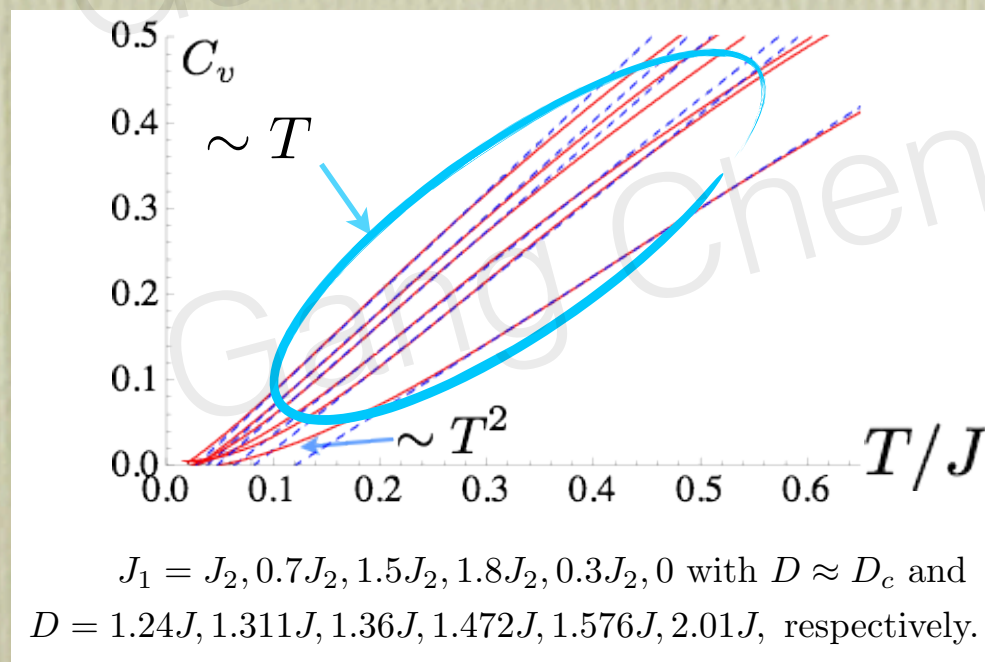
field normal to the plane, $\chi^z = 0$

Powder average

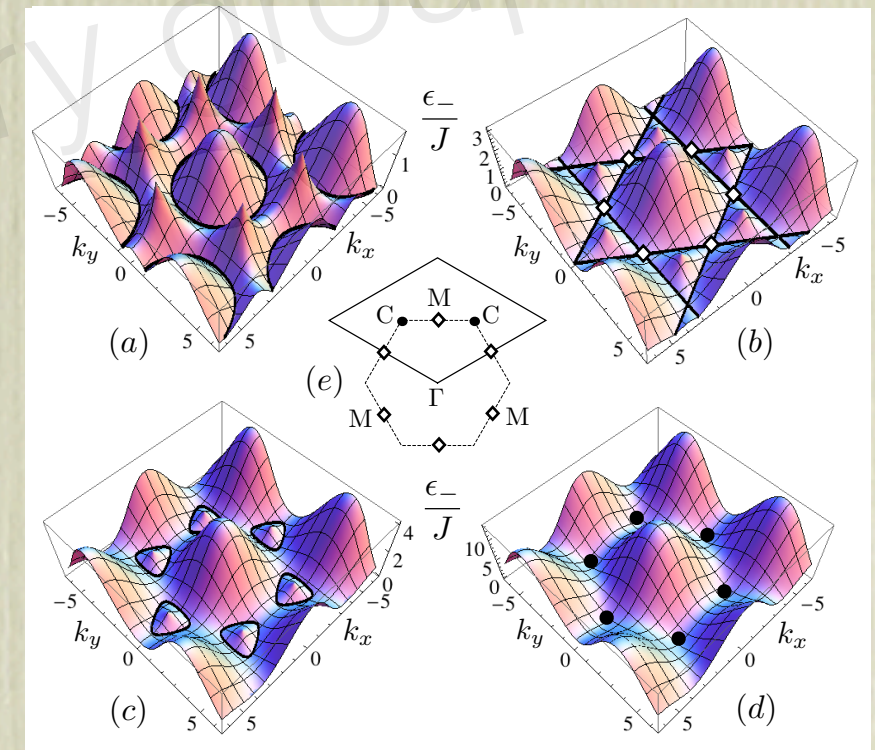
$$\chi_{av} = \frac{2}{3}\chi_0^\perp$$

Experimental check: susceptibility on single-crystal sample.

* Linear- T heat capacity: due to an emergent quadratic spin excitation near the criticality



Experimental check: dynamical spin structure factor from inelastic neutron scattering.



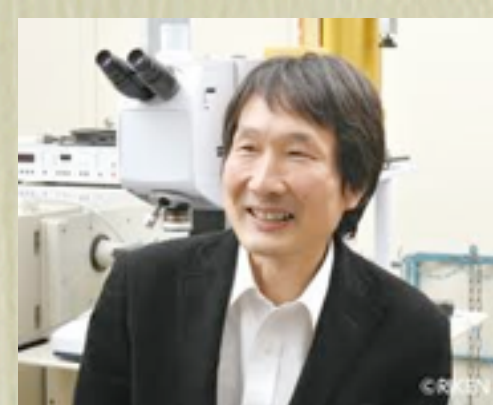
Evolution of low energy spin excitation at the critical point as J_2/J_1 increases.

Since the model still has U(1) symmetry, the spin susceptibility along z direction is zero. However, if the powder sample, so spins susceptibility is constant in single crystal sample and measure susceptibility.

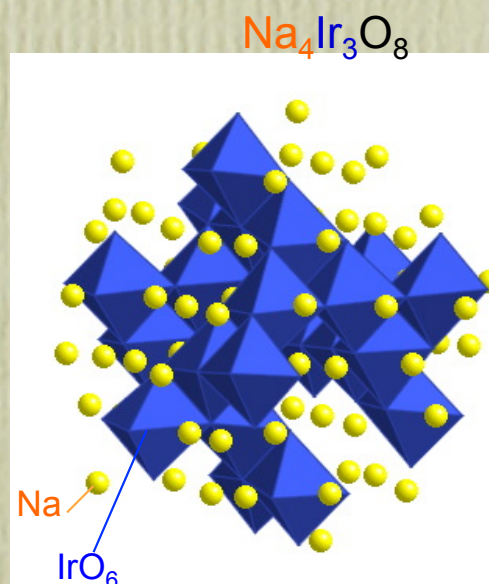
From the low-energy spin excitation, we can see the linear- T heat capacity at the quantum criticality. There is a crossover to quadratic behavior at intermediate temperature. That's due to the quadratic spin excitation at very low temperature, the dispersion becomes quadratic. The crossover temperature is constant.

This is a plot of low energy spin excitation dispersion. And these contours have been measured by neutron scattering.

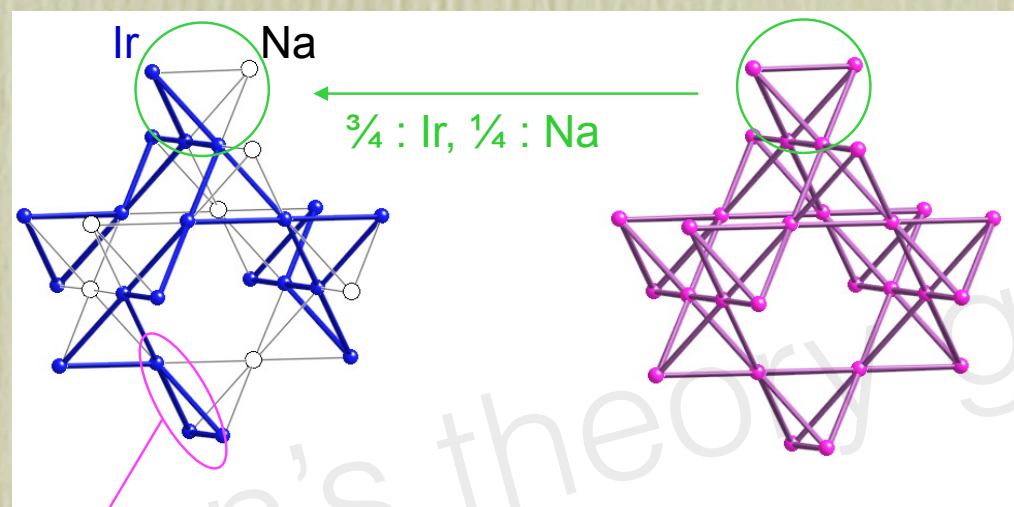
Na₄Ir₃O₈-a promising QSL candidate



Takagi



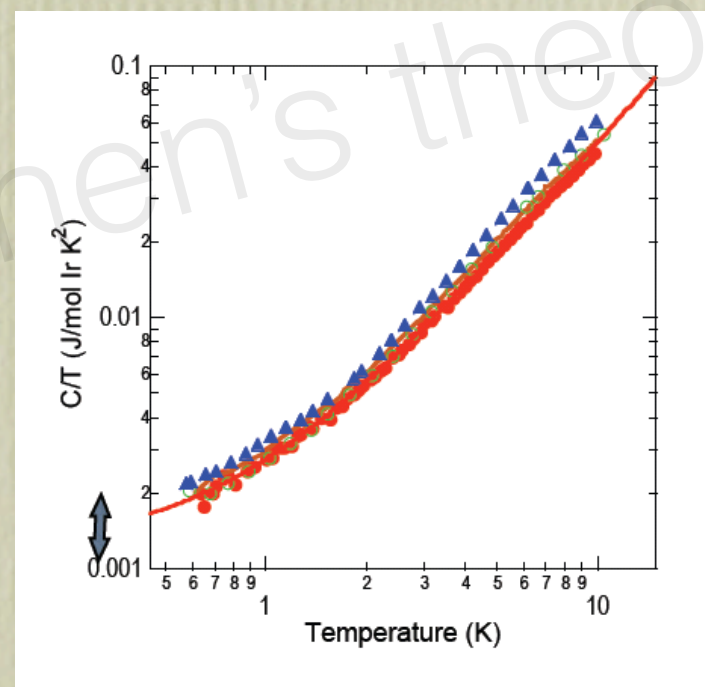
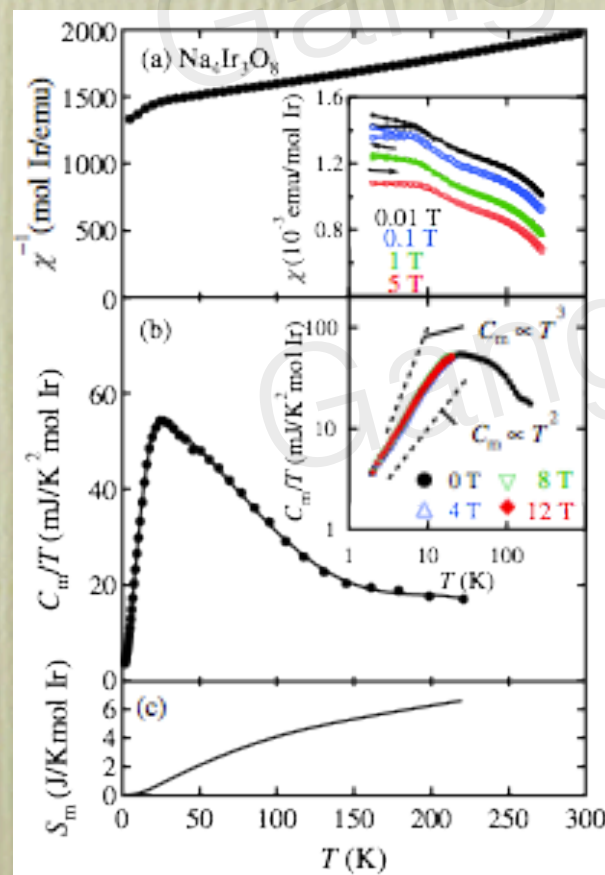
very little disorder



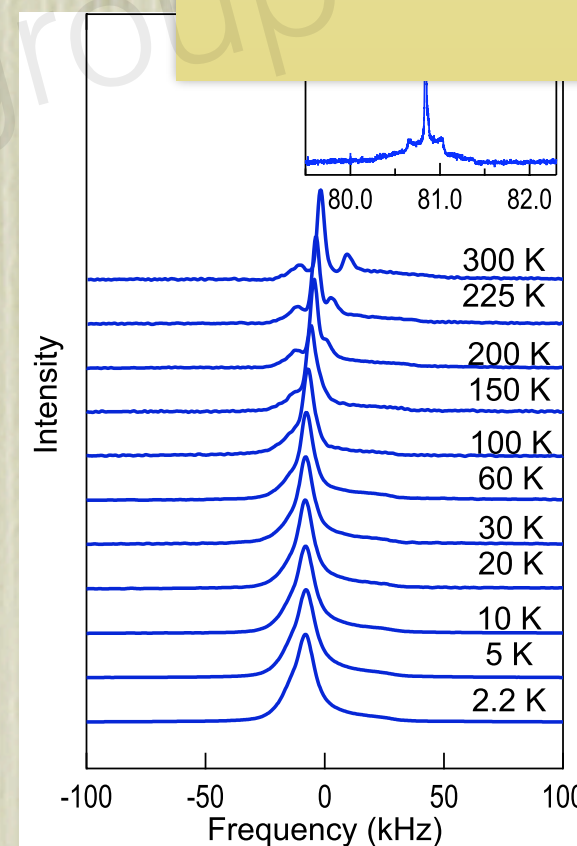
hyperkagome
corner-sharing triangles in 3D



Now I want to discuss this material Na₄Ir₃O₈ candidate for qsl. Ir atom carries the magnetic moment. The hyperkagome, which is a corner sharing triangles in 3D. Kagome is a corner sharing triangles in 2D. It is spin susceptibility, heat capacity, and NMR found.



Okamoto, etc, Phys. Rev. Lett. **99**, 137207 (2007)



Na-NMR

Experiments on polycrystal sample

- * spin-1/2 moment on hyperkagome lattice
- * $\Theta_{CW} = -650K$, no ordering down to 2K, $f > 325$
- * very *large* T=0 spin susceptibility
- * linear-T heat capacity

Wilson Ratio $\gamma \equiv \frac{C_v}{T} \Big|_{T \rightarrow 0}$ $W \equiv \frac{\pi^2}{3} \frac{\chi / \mu_B^2}{\gamma / k_B^2}$ $W = 35$ in polycrystal

Wilson Ratio quantifies spin fluctuations that enhance the sus

Table 1 Some experimental materials studied in the search for QSLs				Wilson Ratio
Material	Lattice	S	Θ_{CW} (K)	R^*
κ -(BEDT-TTF) ₂ Cu ₂ (CN) ₃	Triangular†	½	-375‡	1.8
EtMe ₃ Sb[Pd(dmit) ₂] ₂	Triangular†	½	-(375-325)‡	? ~1.0-3.0
Cu ₃ V ₂ O ₇ (OH) ₂ •2H ₂ O (volborthite)	Kagomé†	½	-115	6
ZnCu ₃ (OH) ₆ Cl ₂ (herbertsmithite)	Kagomé	½	-241	?
BaCu ₃ V ₂ O ₈ (OH) ₂ (vesignieite)	Kagomé†	½	-77	4
Na ₄ Ir ₃ O ₈	Hyperkagomé	½	-650	70 30-40
Cs ₂ CuCl ₄	Triangular†	½	-4	0

- Free electron gas $W = 1$
- He-3 (almost localized fermi liquid) $W = 4$
- Fe-Superconductor (Fe_{1.04}Te_{0.67}Se_{0.33}) $W = 5.7$

Basic physics in Na₄Ir₃O₈

- Strong spin-orbit coupling (Z=77)
- Multi-orbital bands, 3 t_{2g} orbitals
- Close to metal-insulator transition (true for almost all iridates under current investigation)

L. Balents, Nature **464**, 199 (2010)
GC, et al, Phys. Rev. Lett. **102**, 096406 (2009)
D. Vollhardt, Rev. Mod. Phys. **56**, 99 (1984)
J. Yang, et al, JPSJ, **79**, 074704, (2010)

Any reasonable modeling should capture these three physics!

the spin moment is spn 1/2, CW temp i
parameter is avery large. spins scuspt i
temperature.

Using the heat capacity and spin scusp
Which is quite large W=35. To give you
ratio, let's look at wilson ratio of some o
other qsl candiate is of order of unity.

Let's also look at some other systems.
He-3, which is interpret as
an almost localized fL has wilson ratio
Fe-SC, which is believed to be a mutli

What distinguish NIO from these other
are the following three basic physics.

it has strong soc
it is mutli-orbital band, all 3 t2g bands a
it is close to metal-insualtor xtion.

Other qsl candidates are described eith
heisenberg model with spin-rotational s

He-3 is close to Mott insulator xiton, bu
believed to be a multi-band system, bu

Iridium is very heavy!

PRODUCED BY THE FOUNDATION FOR EDUCATION, SCIENCE AND TECHNOLOGY FOR NATIONAL SET WEEK 2003

PERIODIC TABLE of the ELEMENTS

DMITRI MENDELEEV (1834 - 1907)

The Russian chemist, Dmitri Mendeleev, was the first to observe that if elements were listed in order of atomic mass, they showed regular (periodic) repeating properties. He formulated his discovery in a periodic table of elements, now regarded as the backbone of modern chemistry.

The crowning achievement of Mendeleev's periodic table lay in his prophecy of those, undiscovered elements. In 1869, the year he published his periodic classification, the elements gallium, germanium and scandium were unknown. Mendeleev left spaces for them in his table and soon predicted their atomic masses and other chemical properties. Six years later, gallium was discovered and his predictions were found to be accurate. Other discoveries followed and their chemical behavior matched that predicted by Mendeleev.

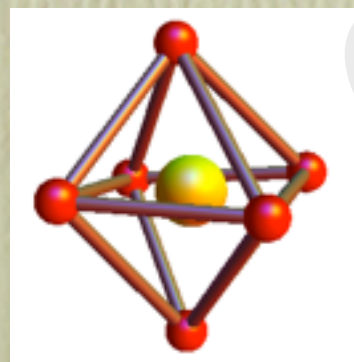
This remarkable man, he jumped in a family of 17 children, has left the scientific community with a classification system so powerful that it became the cornerstone in chemistry teaching and the prediction of new elements ever since. In 1905, element 101 was named after him: Mendelevium.

Ir is very heavy, so there is a large SOC, the local moment in the mott regime was first pointed out in this work.

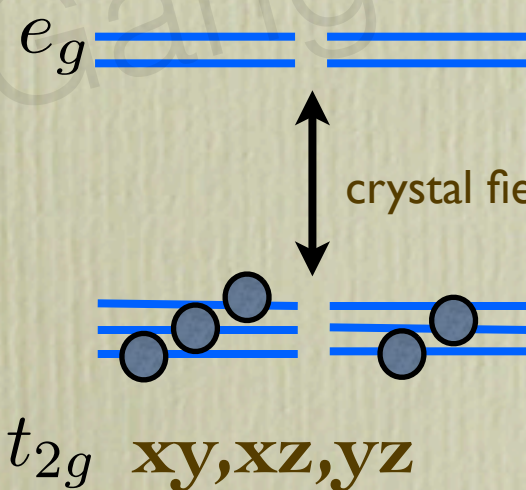
d electron orbital split into upper e_g and lower t_{2g} . The lower t_{2g} is further split by SOC into upper spin $j=1/2$ and lower $j=3/2$. Four electrons completely fill $j=3/2$, and one electron fill $j=1/2$ and give a spin-orbital local moment.

GC, Balents, PRB 2008

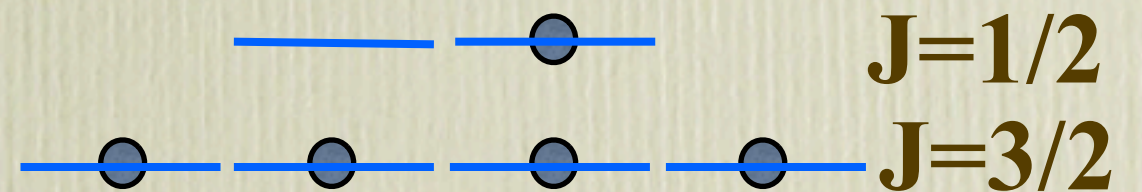
Formation of local moment in the strong Mott regime



IrO_6
 Ir^{4+}, d^5

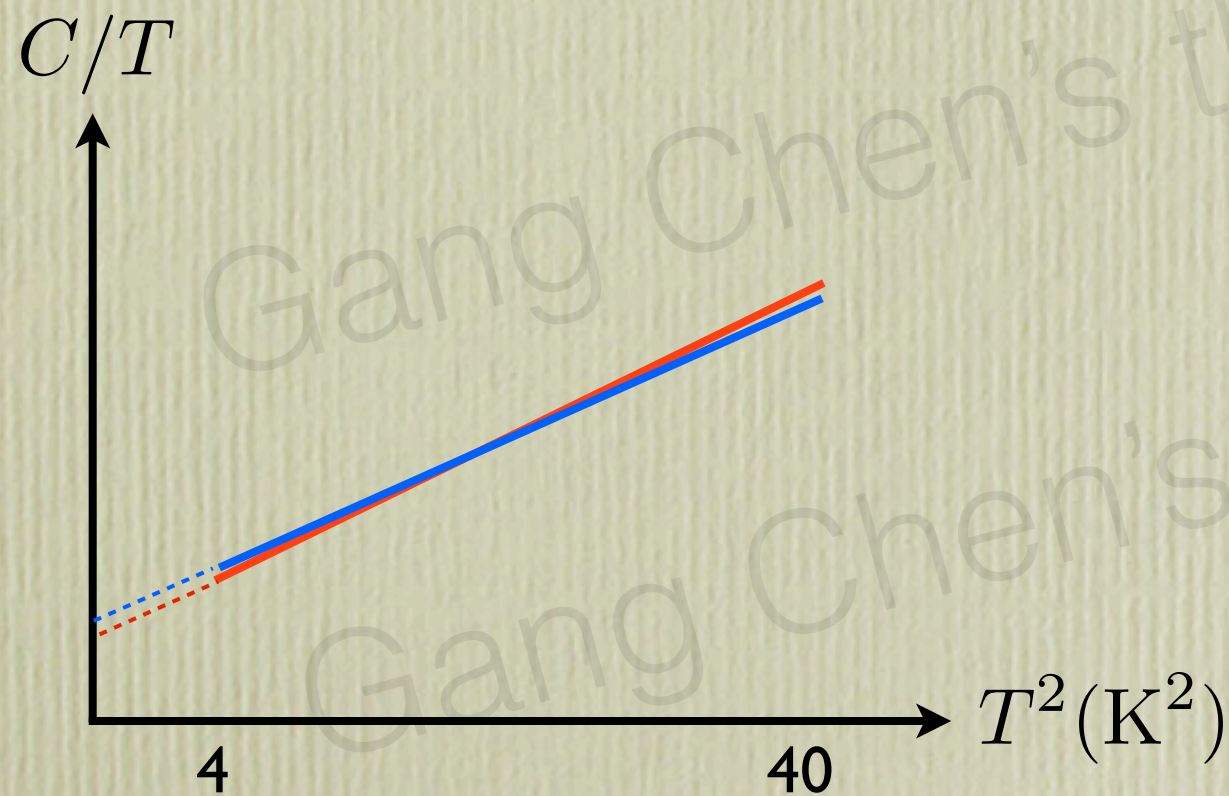


SOC

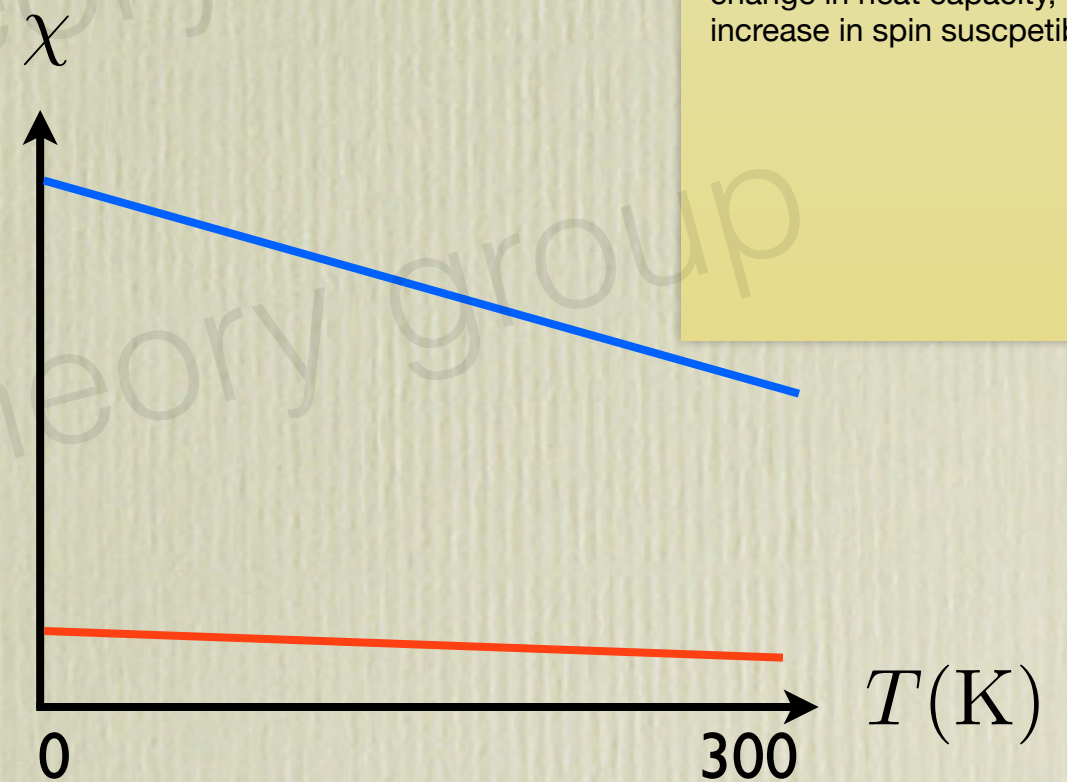


Unpublished new expts

- Single-crystal metallic sample (R. Perry, et al, unpublished, Prof. Takagi's group)
- Polycrystal insulating sample (Okamoto, et al, PRL 2007)



Small change ($\sim 18\%$) in linear- T heat capacity



Large enhancement of magnetic susceptibility.
Susceptibility increases with resistivity
(several other single-crystal samples)

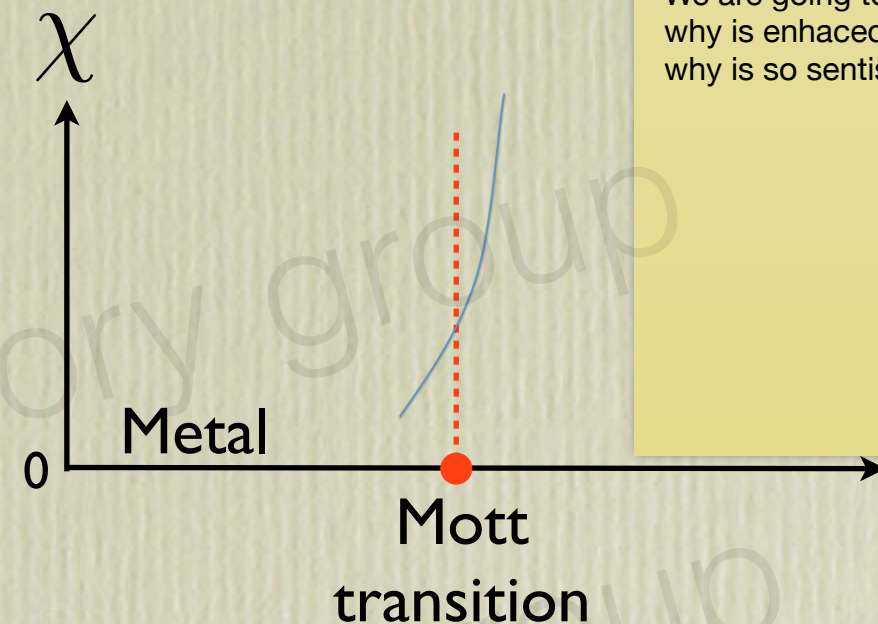
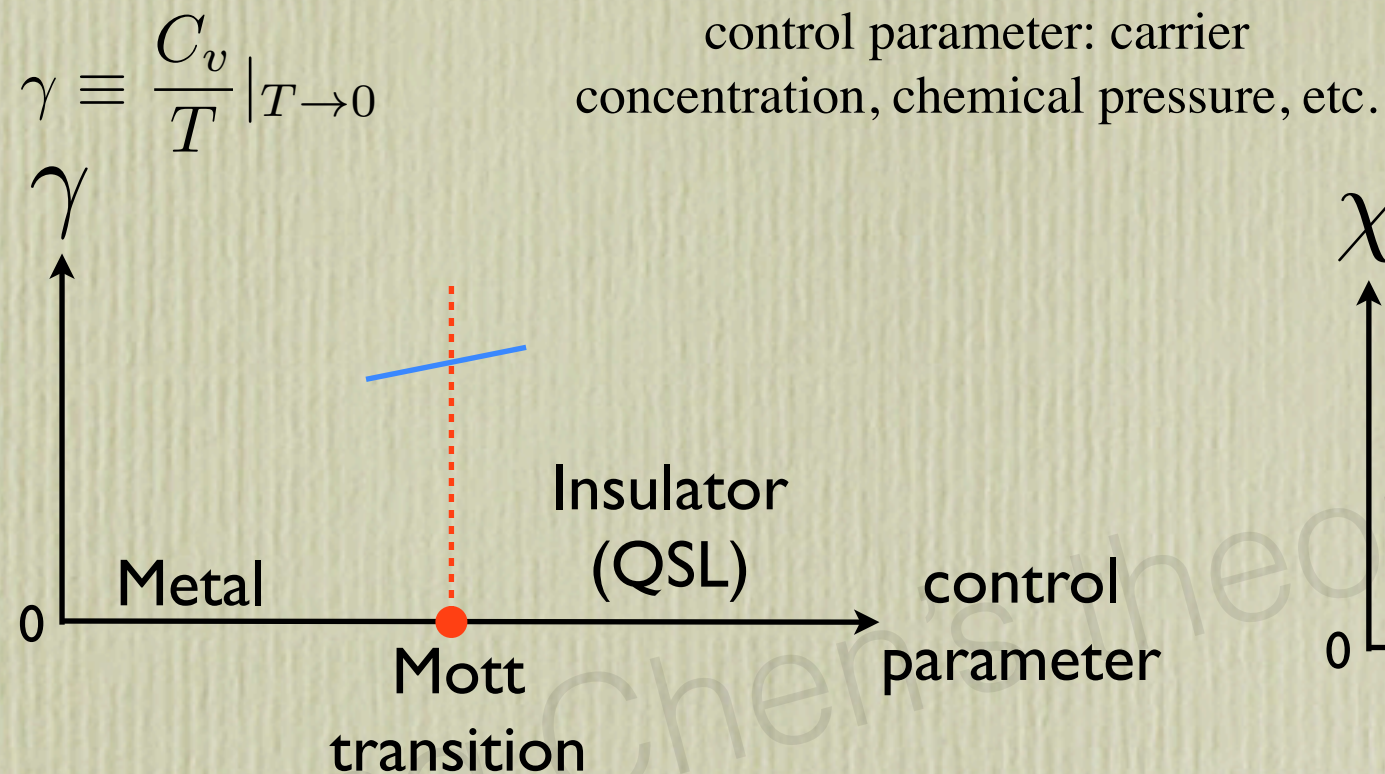
Now we have single crystal sample. During the preparation, this single crystal is metallic, some time is insulator. And experimental list found, as the system changes from metal to insulator, there is a very small change in heat capacity, but there is a large increase in spin susceptibility.

Summary of the new expts: schematic plots

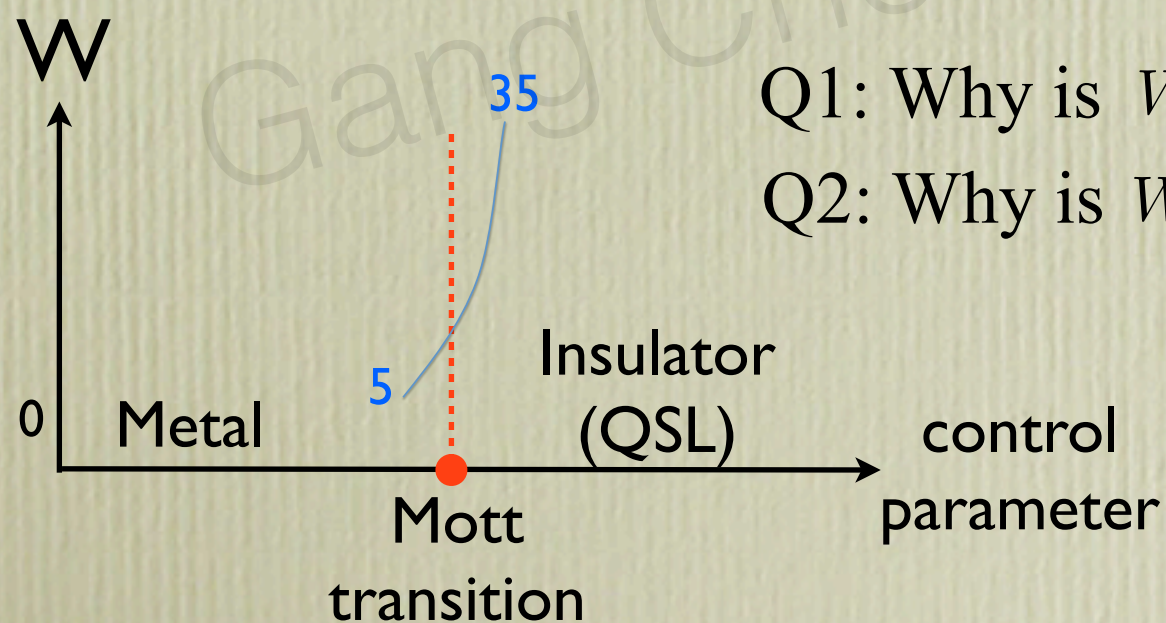
Let me summarize the new expts with the plots. I imagine there is a control parameter insulating transition. this parameter can be changed by something else which we don't know.

As the system crosses the metal insulating transition, the susceptibility has little change, but susceptibility is strongly enhanced, so it goes from 5 to 35.

We are going to address the following questions: why is susceptibility enhanced in the insulating phase? why is susceptibility so sensitive to the Mott transition?



Wilson Ratio $W \equiv \frac{\pi^2}{3} \frac{\chi / \mu_B^2}{\gamma / k_B^2}$



Q1: Why is W (or χ) enhanced in the insulating phase?

Q2: Why is W (or χ) so sensitive to Mott transition?

Theoretical proposals

U(1) QSL? M. Lawler, Kim, Balents, etc Phys. Rev. Lett. **101**, 197202 (2008)

Spinon fermi surface: (nearly) linear-T Cv, constant χ (Heisenberg model)²⁰⁰

If other interactions are included to break spin-rotational symmetry, large W might be obtained for this state.

Z2 QSL (less likely) Y. Zhou, P. Lee, etc Phys. Rev. Lett. **101**, 197201 (2008)

Suppress Cv by spinon pairing to enhance W (interesting)

Explain the susceptibility remaining constant by large SOC $\lambda \gg \Delta$

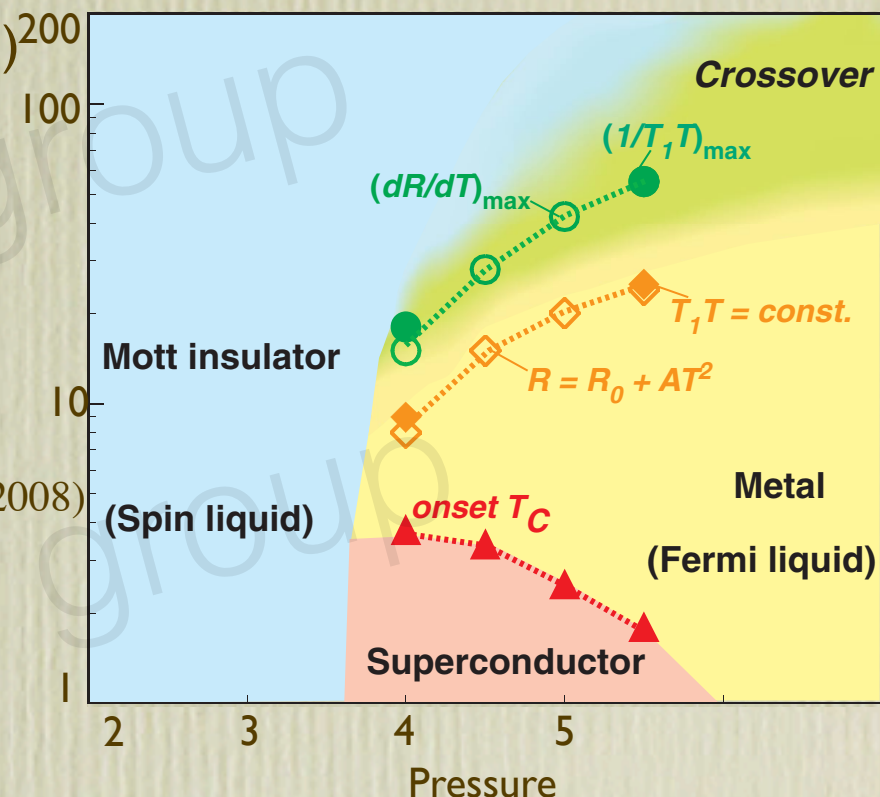
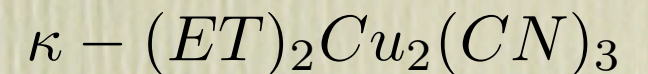
Expect superconductivity in conducting side just like kappa-ET organics if no SC, expect suppressed Cv from metal to QSL.

VBS (less likely) R. Moessner, etc. Phys. Rev. Lett. **105**, 237202 (2010)

Similar series expansion like Huse+Singh's work on kagome

Complicated ground state: 72 sites in one cell

a bit hard to explain power-law Cv and constant χ over a large temperature



Kanoda's group 2003-

all the three proposals are based on Heisenberg model. Heisenberg model is not appropriate for this material. In first proposal (given by my collaborator, YBKim and L E a U(1) QSL with SF. This state should have Wilson ratio

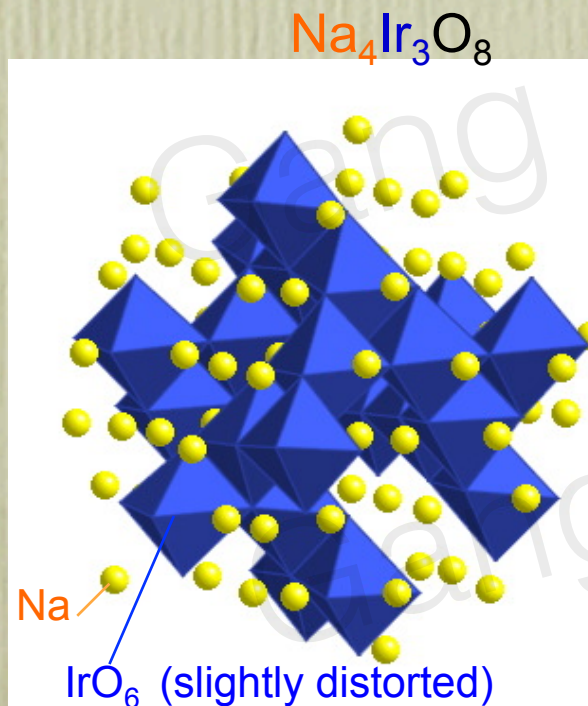
The second proposal is given Patrick Lee and his collaborator. It is a Z2 QSL, with spinon pairing. The proximate conducting state should have electron spinon binds charge boson., which means superconductivity. However, this proximate SC phase was observed in kappa-ET organics.

Extended Hubbard model

Basic physics in $\text{Na}_4\text{Ir}_3\text{O}_8$

- Strong spin-orbit coupling ($Z=77$)
- Multi-orbital bands, 3 t_{2g} orbitals
- Close to metal-insulator transition
(true for almost all iridates under current investigation)

Here, we want to write down a honest model to capture the three basis physics of NaIO. We consider an extended Hubbard model. in the hamiltonian. kinetic term, describing hopping, soc coupling single ion anisotropy due to the distortion of IrO6 octahedron.



$$\mathcal{H} = \mathcal{H}_{hop} + \mathcal{H}_{soc} + \mathcal{H}_{ion} + \mathcal{H}_{int}$$

\mathcal{H}_{hop} - Tight-binding model

\mathcal{H}_{soc} - Atomic spin-orbit coupling

\mathcal{H}_{ion} - single-ion (crystal field) term due to IrO₆ distortion
(drive transition from TBI to metal in 227 iridates)

\mathcal{H}_{int} - Multiorbital interactions

Wilson ratios in non-interacting

Let's first look the non interacting limit

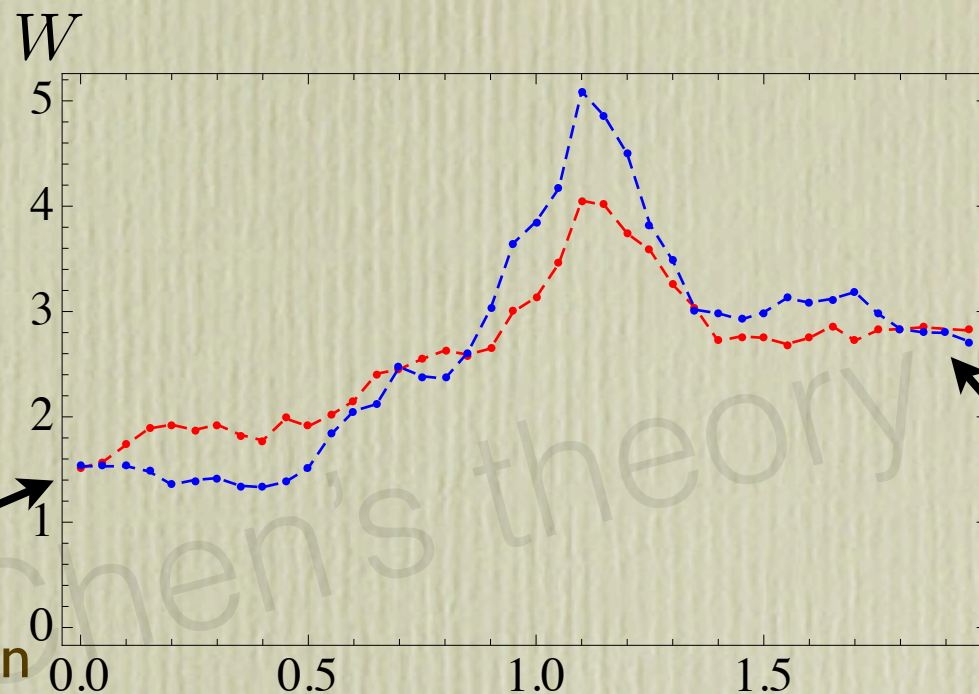
Wilson ratio against spinon orbit, t simple hopping parameter

spin susc not only has contribution from non-FS contribution.

$$\mathbf{M}_i \equiv \mu_B (\mathbf{L}_i + 2\mathbf{S}_i)$$

$$W \neq 1$$

is because of the hybridization of different orbitals



two an

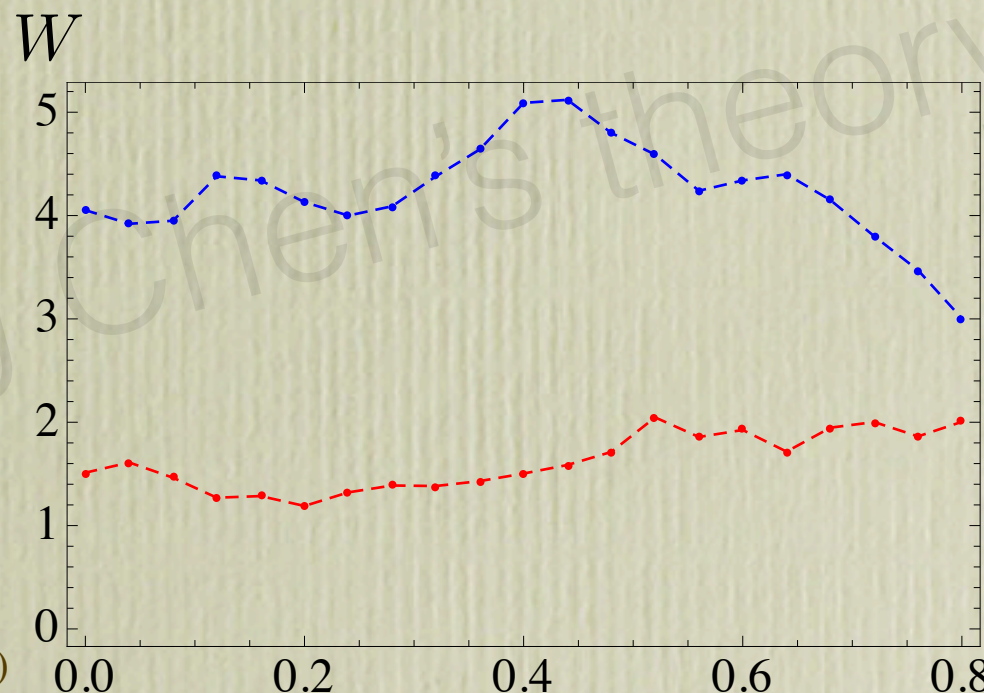
..... $D = 0.4$

Same reason why Heisenberg model is relevant for Sr_2IrO_4

λ/t_σ

λ -SOC

t_σ -hopping parameter



..... $\lambda = 0$

..... $\lambda = 1.1$

D/t_σ

G. Chen, et al Phys. Rev. B **78**, 094403, (2008)

G. Jackeli, et al Phys. Rev. Lett. **102**, 017205, (2009)

F. Wang, et al Phys. Rev. Lett. **106**, 136402, (2011)

Wilson Ratio is 5 at most.

Multi-orbital interaction

$$H_{int} = U \sum_{i,m} \hat{n}_{i,m,\uparrow} \hat{n}_{i,m,\downarrow} + \frac{U'}{2} \sum_{i,m \neq m'} \hat{n}_{i,m} \hat{n}_{i,m'} + \frac{J}{2} \sum_{i,m \neq m'} d_{im\sigma}^\dagger d_{im'\sigma}^\dagger d_{im\sigma} d_{im'\sigma} + \frac{J'}{2} \sum_{i,m \neq m'} d_{im\uparrow}^\dagger d_{im\downarrow}^\dagger d_{im'\downarrow} d_{im'\uparrow}$$

i is a position index.

m is an orbital index.

In atomic limit,

$$U = U' + J + J'$$

$$J = J'$$

Rewrite interaction, $\mathcal{H}_{int} = \mathcal{H}_{c-int} + \mathcal{H}_{ex-int}$

$$\mathcal{H}_{c-int} = \frac{U}{2} \sum_i (\hat{n}_i - 5)^2$$

$$\mathcal{H}_{ex-int} = -J \sum_{i,m \neq m'} \hat{n}_{i,m} \hat{n}_{i,m'} + \frac{J}{2} \sum_{i,m \neq m'} d_{im\sigma}^\dagger d_{im\sigma} d_{im'\sigma}^\dagger d_{im'\sigma} + \frac{J}{2} \sum_{i,m \neq m'} d_{im\uparrow}^\dagger d_{im\downarrow}^\dagger d_{im'\downarrow} d_{im'\uparrow}$$

There are four terms in the multi-orbital interaction. m is the orbital index, i is the lattice site. σ is the spin.

intraorbital coulomb
interorbital coulomb
hunds
pair hopping

in atomic limit, we have this relation. I am going to

I rewrite the interaction into two parts, the charge interaction and the exchange. The two terms have different physics. The first part is the charge interaction. U is the energy scale for excessive electron occupation while the second part is the spin/orbital interaction.

Since these two parts describe different physical processes differently.

U is the energy scale for excessive electron/charge occupation.

J is the energy scale for electron distribution among different spin and orbital states.

\mathcal{H}_{ex-int} is like an onsite exchange interaction in the *Kugel-Khomskii* picture.

Strong-coupling MFT: slave-Rotor

Slave-rotor approach to obtain fermionic spinons

$$d_{im\alpha} = e^{-i\theta_i} f_{im\alpha} \quad \text{vs} \quad d_{im\alpha} = b_i f_{im\alpha}$$

$$L_i(R) = \sum_{m\sigma} f_{im\alpha}^\dagger(R) f_{im\alpha}(R) - 5$$

$$[\theta_i, L_i] = i$$

$\langle e^{-i\theta_i} \rangle \neq 0$, $Z \neq 0$, spin and charge are confined, we have a “correlated FL”.

$\langle e^{-i\theta_i} \rangle = 0$, $Z = 0$, we have a “U(1) QSL”.

First I want to treat the charge interaction is the largest energy scale and is responsible for the metal-insulator transition.

To describe the metal-insulator transition approach, this is similar to the slave boson approach for organics discussed in the introduction. The charge spin. Rotor condensation corresponds to the QSL.

The Hubbard model can be solved by numerical calculation.

Original electron Hamiltonian (with the Hubbard-U interaction only)

$$H_{hop} = \sum_{Ri, R' i' m'} t_{mm'}^{ii'} d_{im\sigma}^\dagger(R) d_{im'\sigma}(R') + h.c.$$

$$H_{c-int} = \frac{U}{2} \sum_{Ri} \left(\sum_{m,\alpha} d_{im\alpha}^\dagger(R) d_{im\alpha}(R) - 5 \right)^2$$

$$H_{ion} = D \sum_{Ri\alpha} (L_i^\mu)_{mn}^2 d_{im\alpha}^\dagger(R) d_{in\alpha}(R)$$

$$H_{soc} = \frac{\lambda}{2} \sum_{Ri} \mathbf{L}_{mn} \cdot \boldsymbol{\sigma}_{\alpha\beta} d_{im\alpha}^\dagger(R) d_{in\beta}(R)$$

Slave-rotor mean field Hamiltonian

$$H_f = Q_f \sum_{Ri, R' i' m'} (t_{mm'}^{ii'} f_{im\sigma}^\dagger(R) f_{im'\sigma}(R') + h.c.)$$

$$+ \frac{\lambda}{2} \sum_{Ri} \mathbf{L}_{mn} \cdot \boldsymbol{\sigma}_{\alpha\beta} f_{im\alpha}^\dagger(R) f_{in\beta}(R) + D \sum_{Ri\alpha} (L_i^\mu)_{mn}^2 f_{im\alpha}^\dagger(R) f_{in\alpha}(R)$$

$$H_L = \frac{U}{2} \sum_{Ri} L_i^2(R) + \sum_{Ri} (h L_i(R) + 5h) + Q_r \sum_{Ri, R' i'} e^{i\theta_i(R) - i\theta_{i'}(R')} + h.c.$$

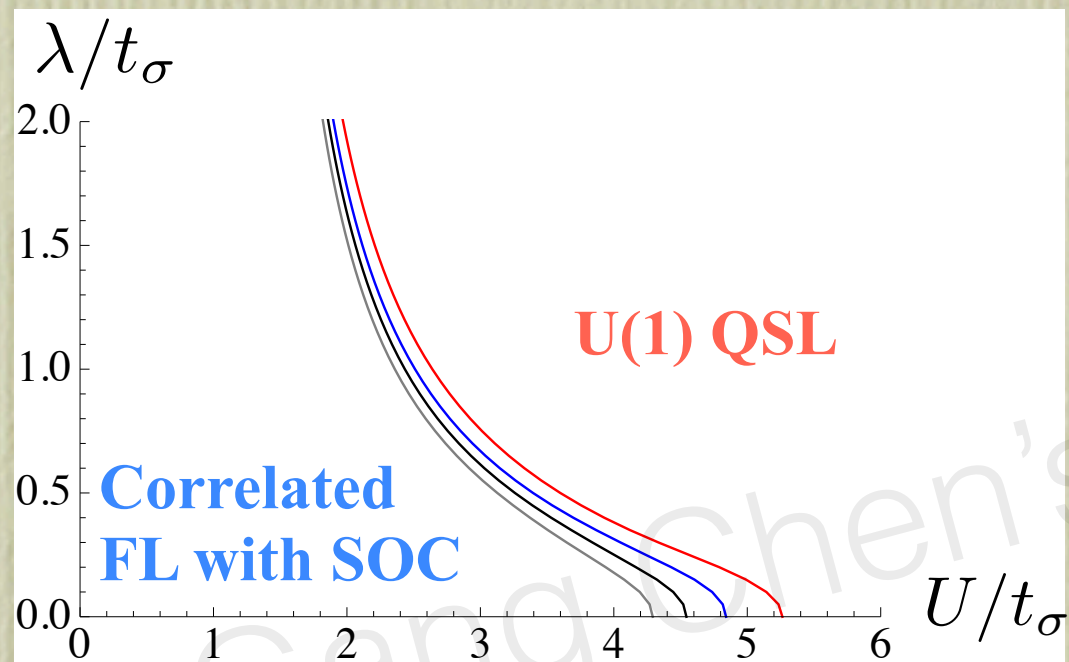
$$Q_f \equiv \langle e^{i\theta_i(R) - i\theta_{i'}(R')} \rangle_\theta \quad Q_r \equiv \sum_{mm'\sigma} t_{mm'} \langle f_{im\sigma}^\dagger f_{i'm'\sigma}(R) \rangle_f$$

S. Florens and A. Georges,

Phys. Rev. B. **70**, 035114 (2004)

D. Pesin, L. Balents, Nature Physics **6**, 376 (2010)

Phase diagram



From left to right, the single-ion anisotropies are

$$D = 0.8t_\sigma \quad D = 0.4t_\sigma \quad D = 0.2t_\sigma \quad D = 0$$

Three energy scales: SOC, correlation, bandwidth

Two observations:

1. SOC enhances correlation effects.

Strong correlation physics may be seen in 4d/5d electron system.

2. Correlation effects enhance SOC.

SOC may be also important even in 3d electron system in certain cases.

This is the mft phase diagram.

illustrate point 1,

4d,5d have strong soc, weak correlation, but soc suppress bw, and enhance correlation.

pt 2, soc is weak in 3d, correlation suppress bw and then enhance soc

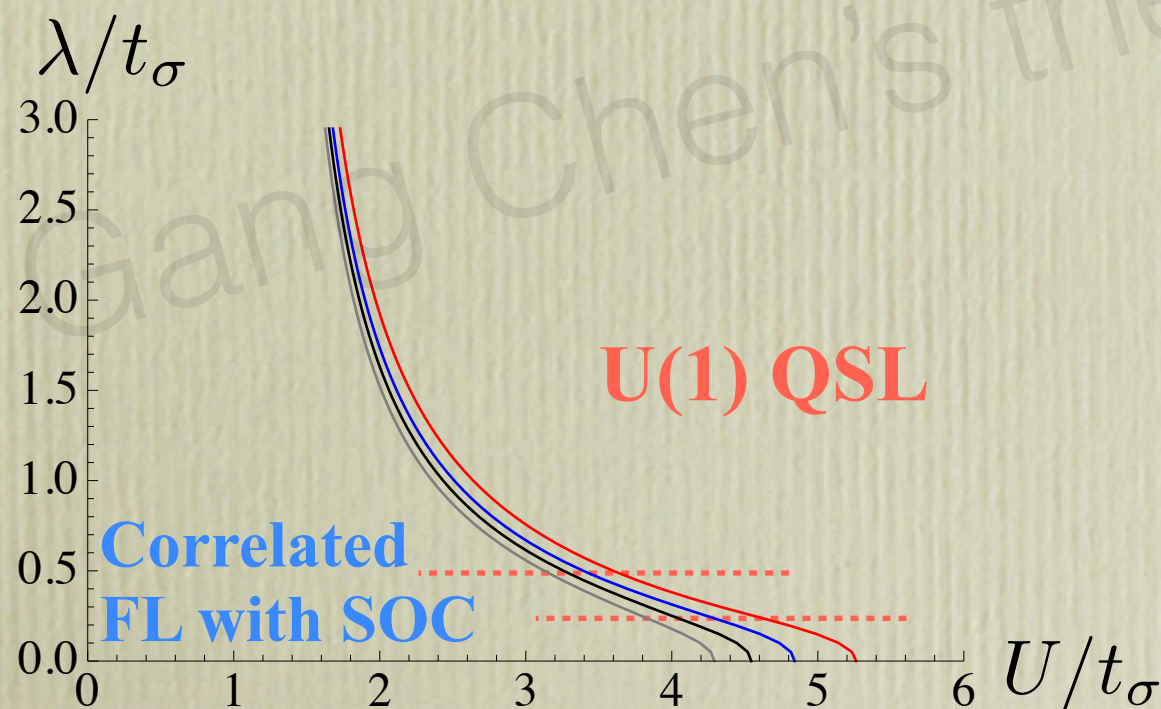
Onsite exchange

We put the onsite exchange interaction in the spinon mean field hamiltonian.

W. Ko, P.A. Lee, Phys. Rev. B. **83**, 134515 (2011)

$$H_{ex-int} = \sum_i \left[-J \sum_{m \neq m'} f_{im\sigma}^\dagger f_{im\sigma} f_{im'\sigma'}^\dagger f_{im'\sigma'} + \frac{J}{2} \sum_{m \neq m'} f_{im\sigma}^\dagger f_{im'\sigma'}^\dagger f_{im\sigma'} f_{im'\sigma} \right. \\ \left. + \frac{J}{2} \sum_{m \neq m'} f_{im\uparrow}^\dagger f_{im\downarrow}^\dagger f_{im'\downarrow} f_{im'\uparrow} \right]$$

$$H_f \rightarrow H_f + H_{ex-int}$$

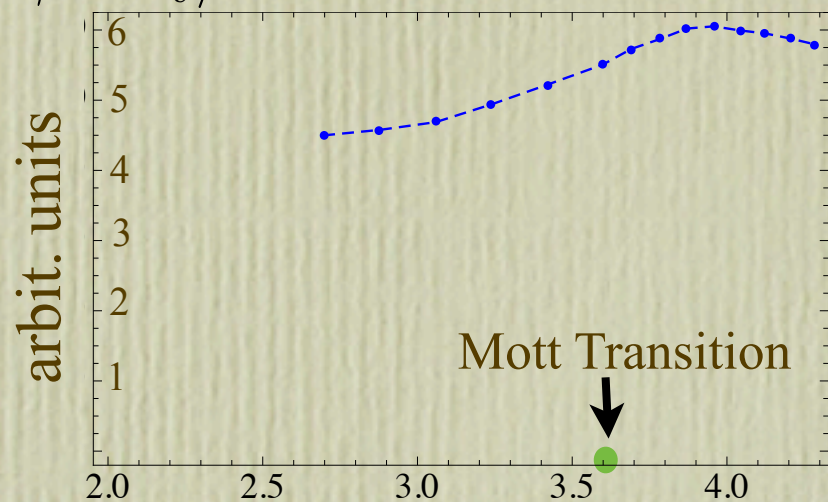


$$\mathbf{M}_i \equiv \mu_B (\mathbf{L}_i + 2\mathbf{S}_i)$$

Study Wilson ratio
along the dashed line

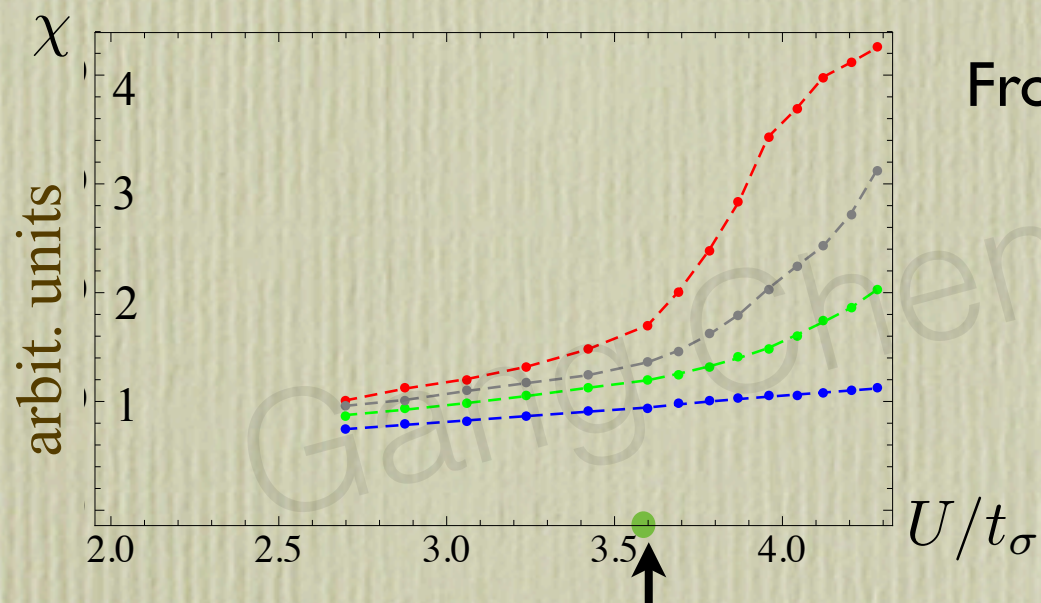
$$\lambda = 0.5t_\sigma$$

$$\gamma \equiv C_v/T$$



Both “effective mass”
and fermi surfaces are
changed due to SOC

$$J \lesssim 0.1U_c$$



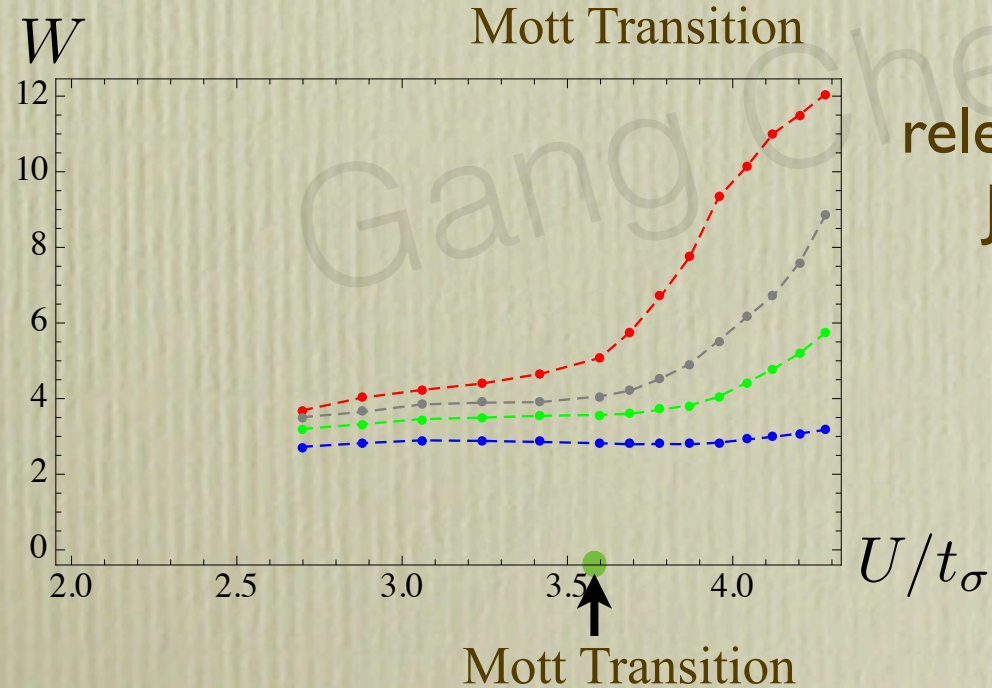
From top to bottom,

$$J = 0.4t_\sigma$$

$$J = 0.3t_\sigma$$

$$J = 0.2t_\sigma$$

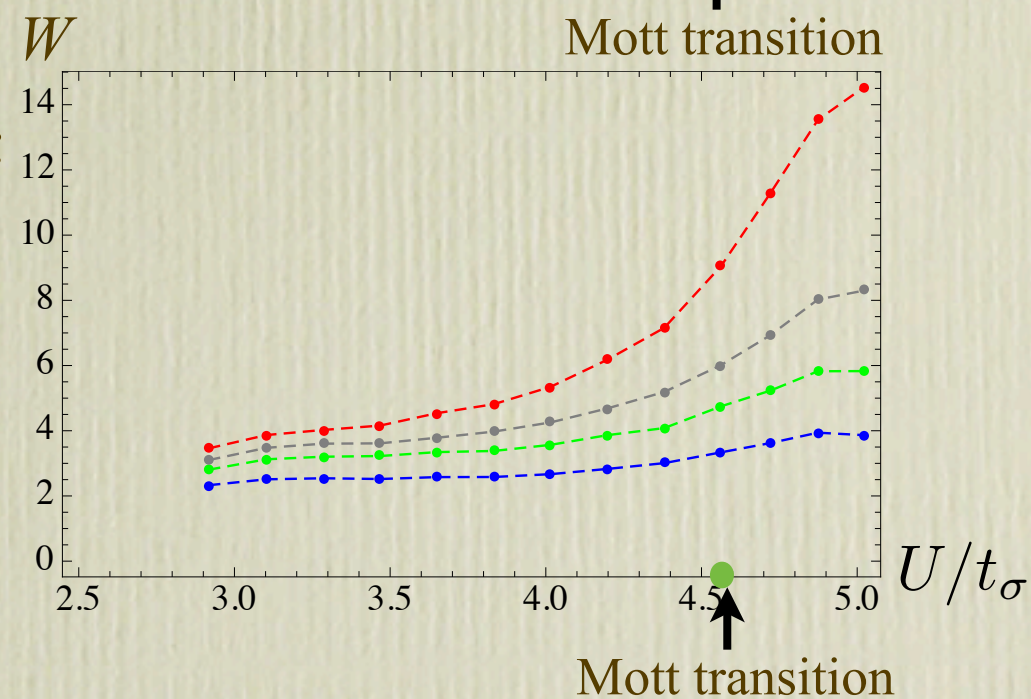
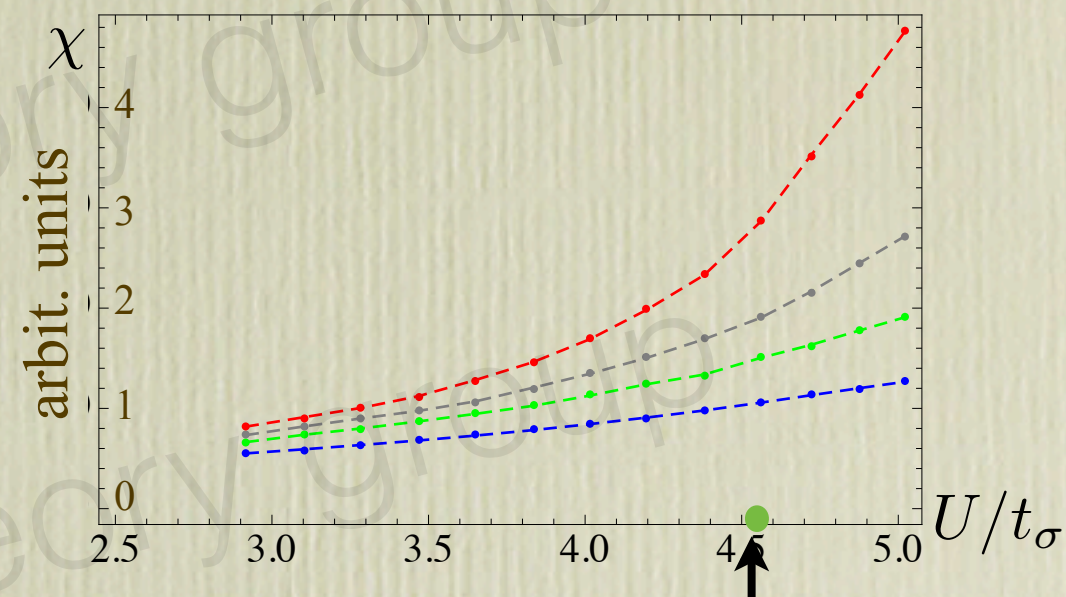
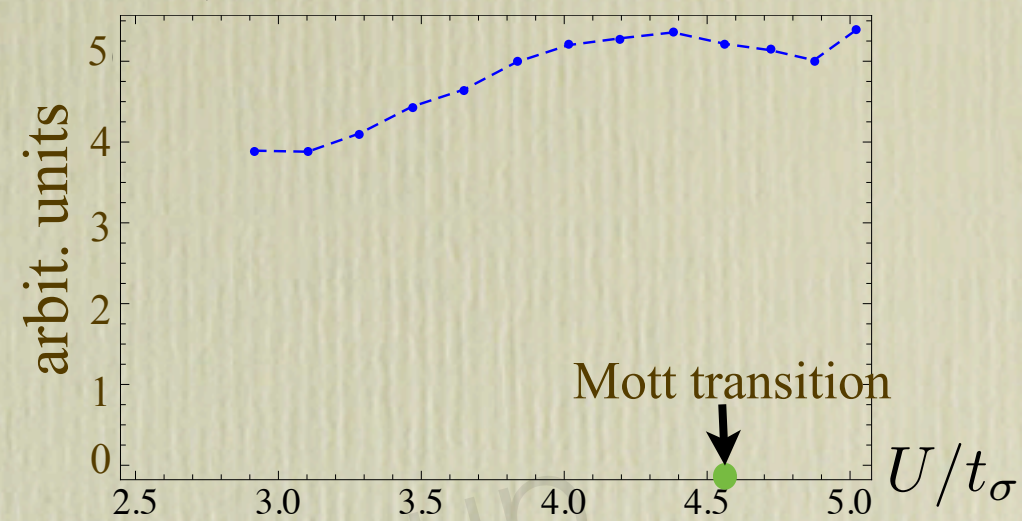
$$J = 0.1t_\sigma$$



relevant energy scales:
J and bandwidth

$$\lambda = 0.25t_\sigma$$

$$\gamma \equiv C_v/T$$



Summary for $\text{Na}_4\text{Ir}_3\text{O}_8$

- * $\text{Na}_4\text{Ir}_3\text{O}_8$ is likely to be a U(1) quantum spin liquid with spinon fermi surfaces.
- * The large Wilson ratio might arise from the combined effect of spin-orbit coupling, correlation and onsite spin-orbital exchange.

For experiments,

- * Other experiments: resonant inelastic x-ray scattering (planned), thermal conductivity (seems like a metal), quantum oscillations (too soft gauge field? O. Motrunich, PRB 2005)
- * Can similar physics be observed in related materials?
e.g. nonmagnetic $\text{R}_2\text{Ir}_2\text{O}_7$ (pyrochlore lattice), etc

Summary and outlook

- I introduce the basis theoretical concepts and experiments related to QSLs.
- I review QSL candidate materials and explain the physics in both failed and promising examples.
- Searching for QSL in real materials provides a lot of opportunities for theoretical innovation, material synthesis, and experimental efforts.